



A Verification Framework Designed to Automate Separation Logic

Thibault Dardinier

ETH zürich

Program Verifiers Based on Separation Logic

Foundational



Automated

Program Verifiers Based on Separation Logic



Program Verifiers Based on Separation Logic



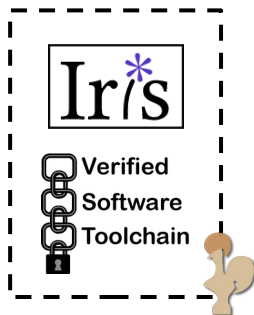
Program Verifiers Based on Separation Logic



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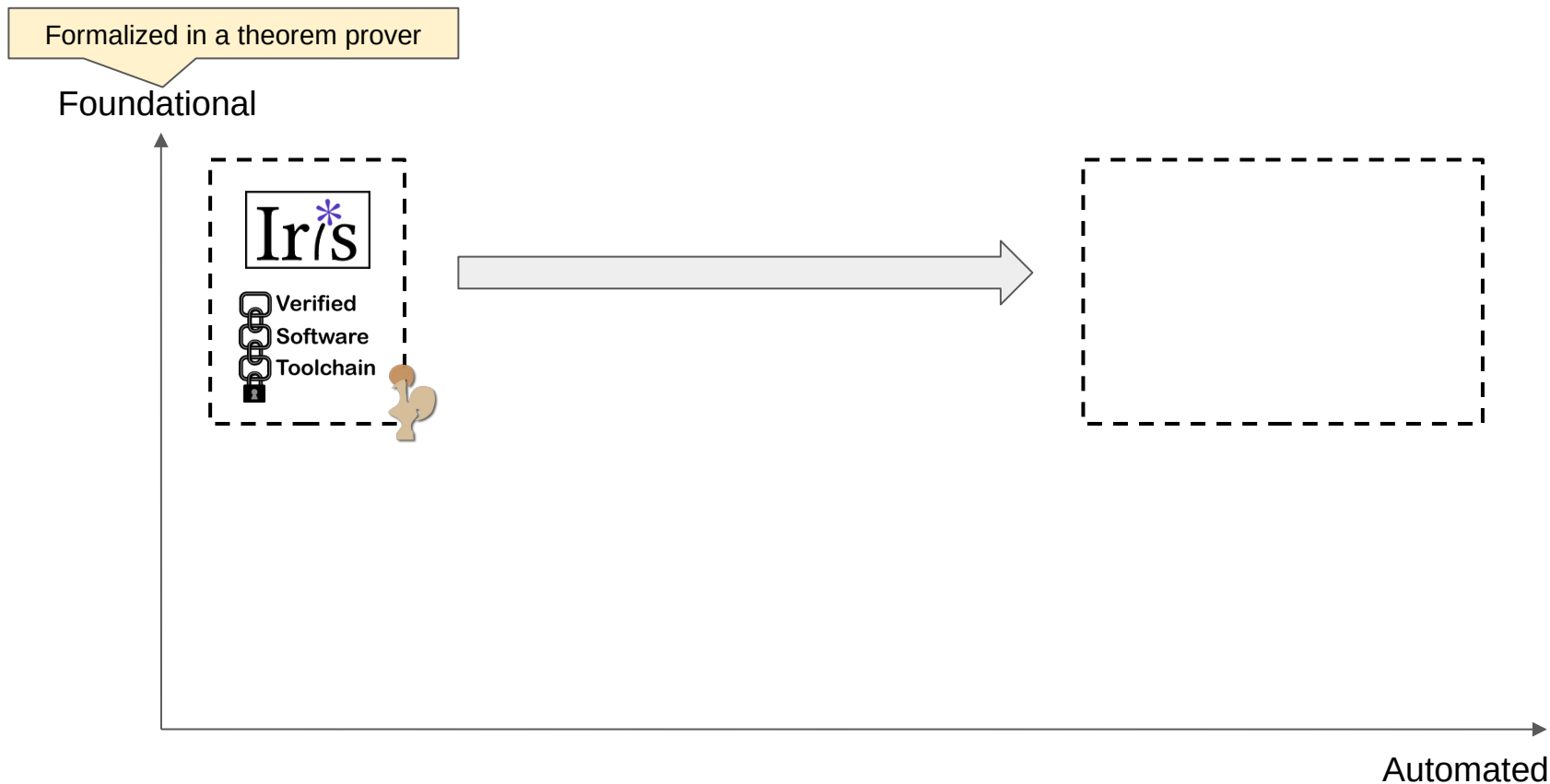
Formalized in a theorem prover

Foundational

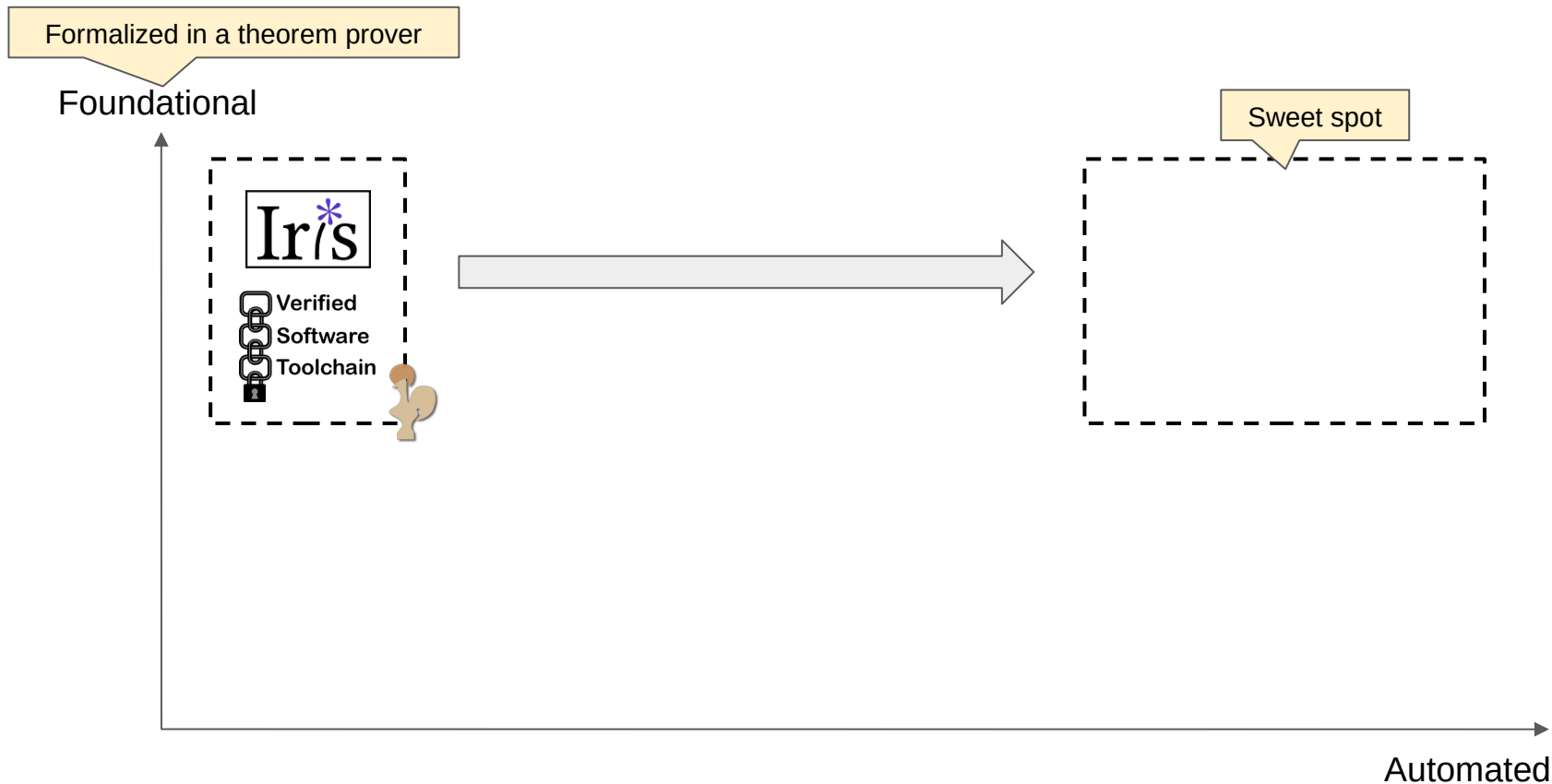


Automated

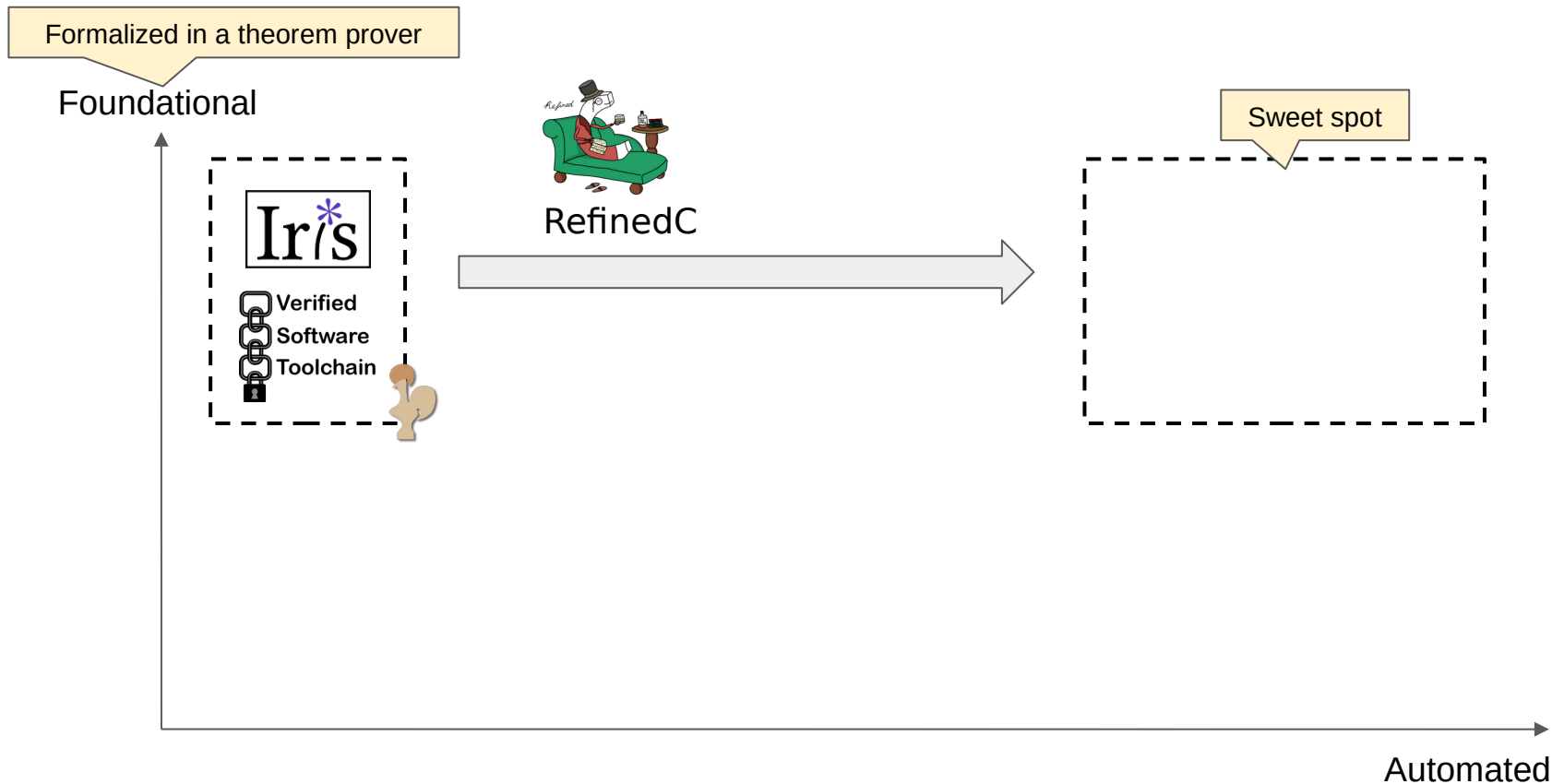
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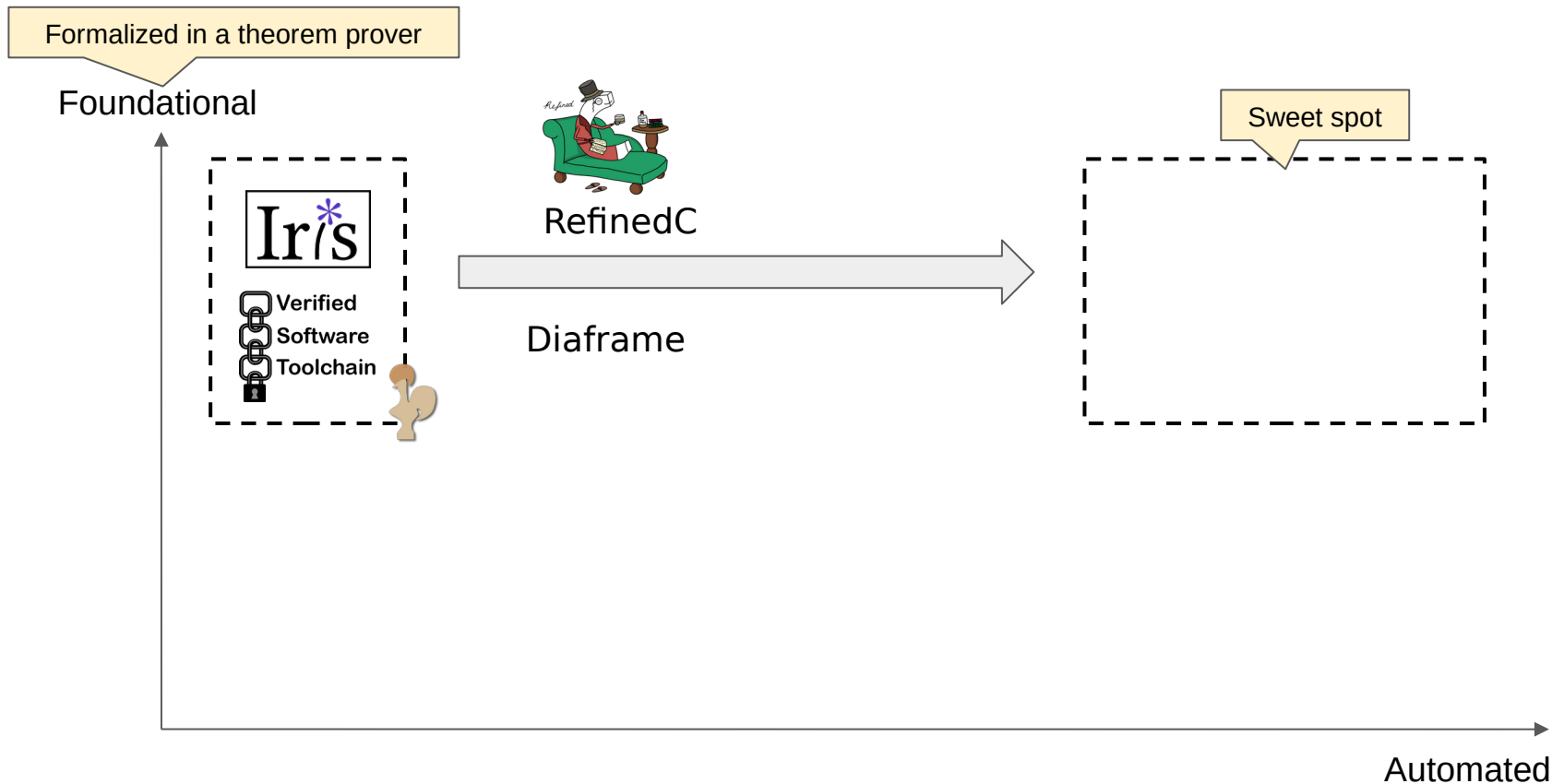
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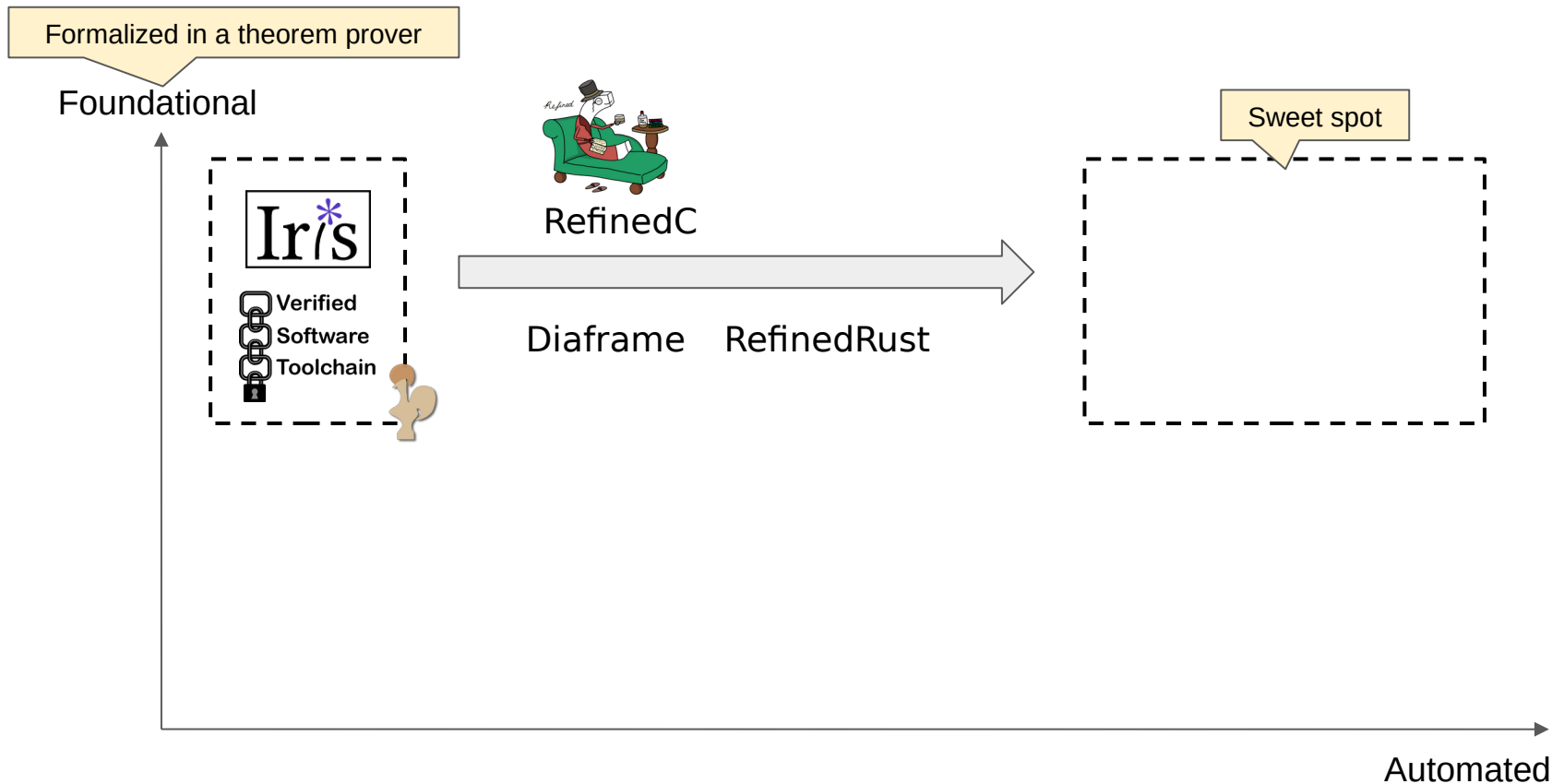
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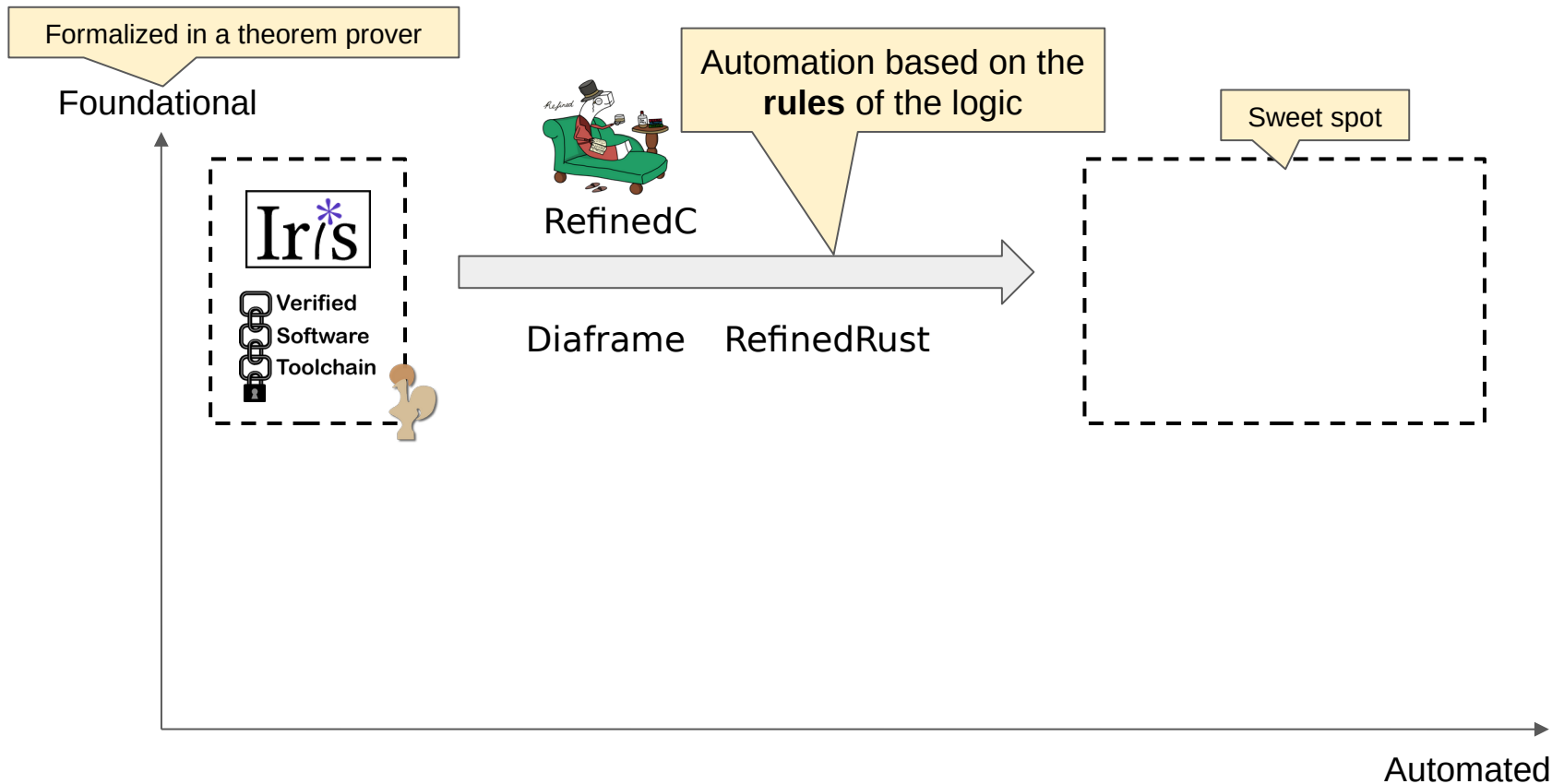
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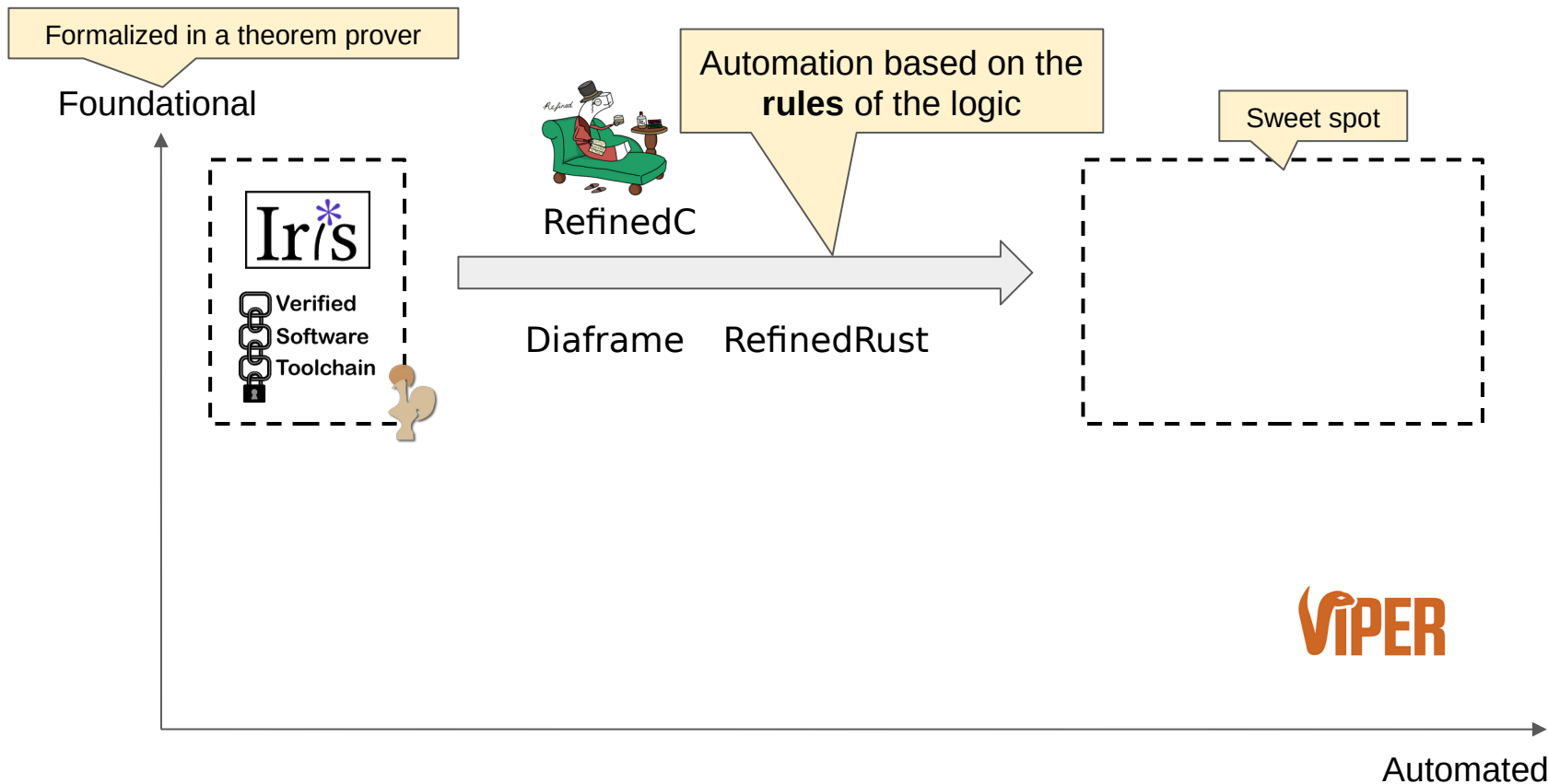
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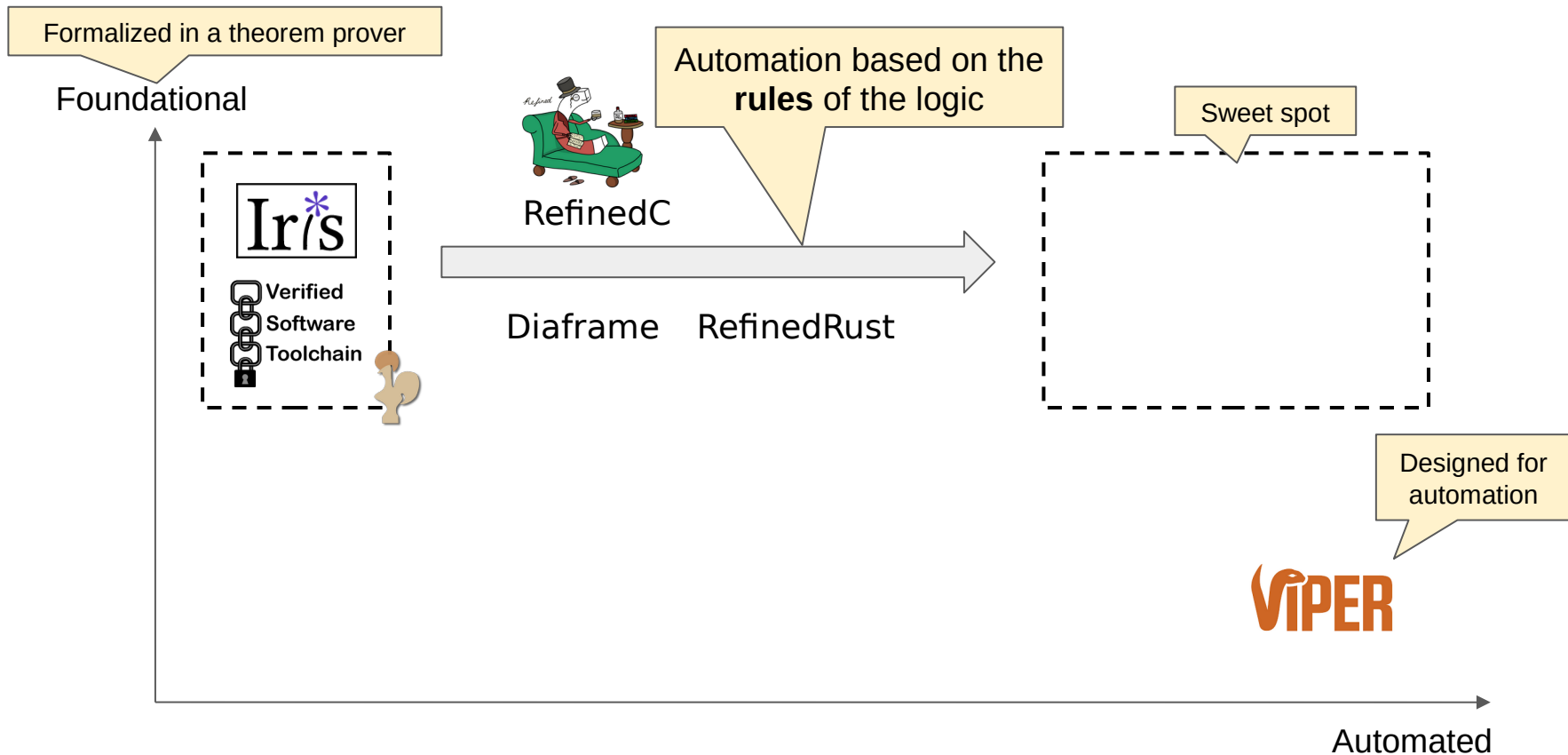
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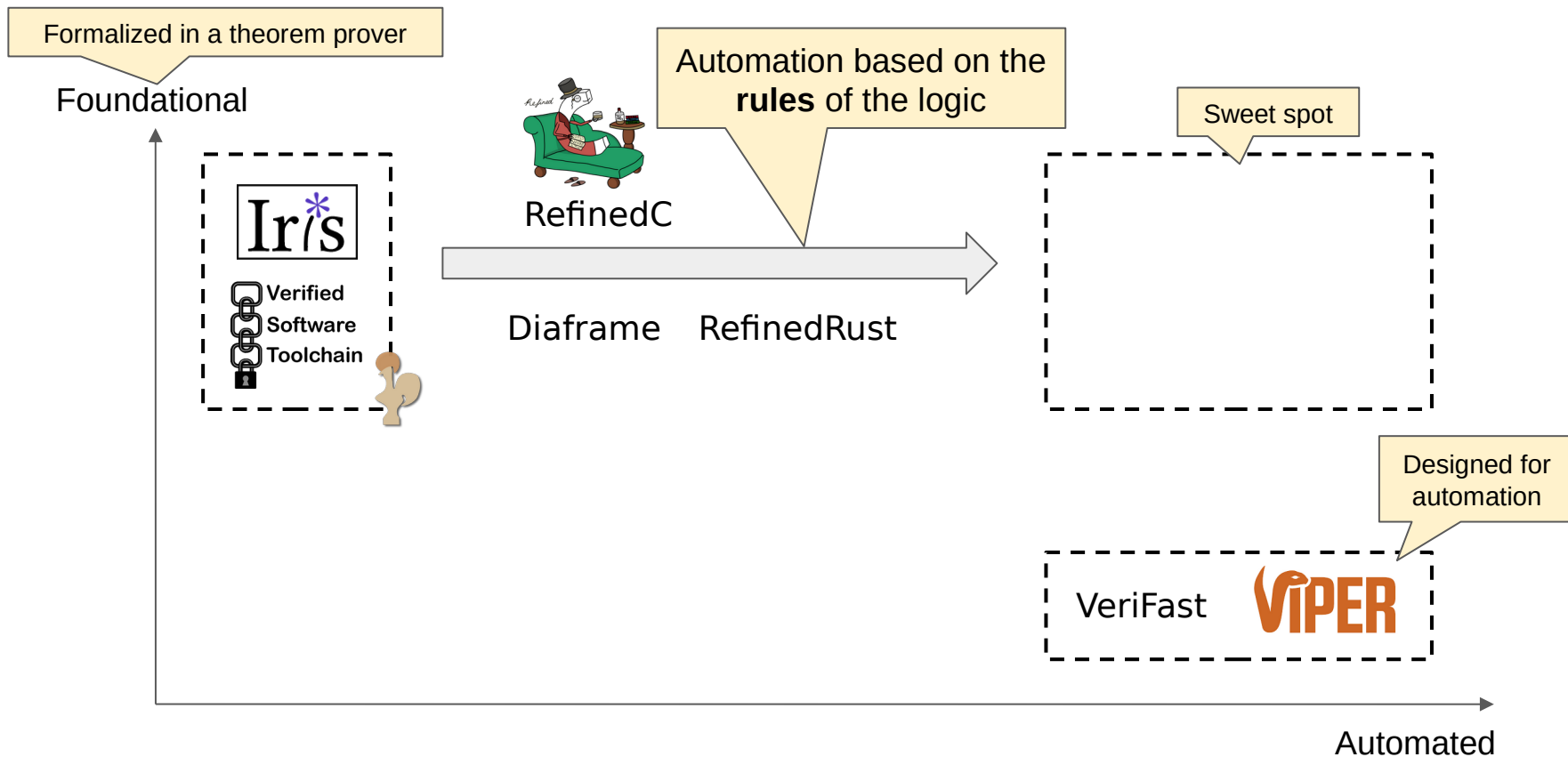
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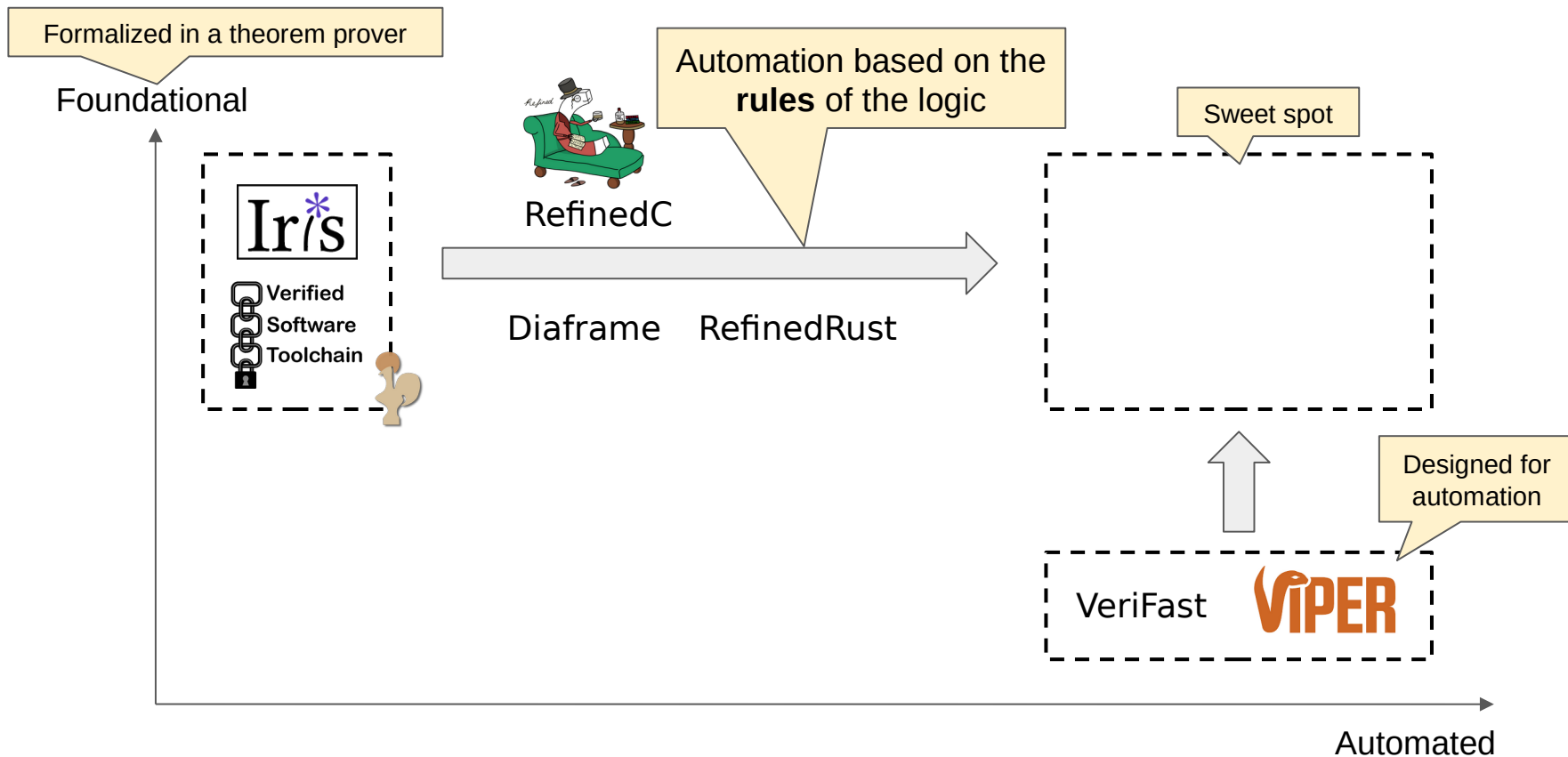
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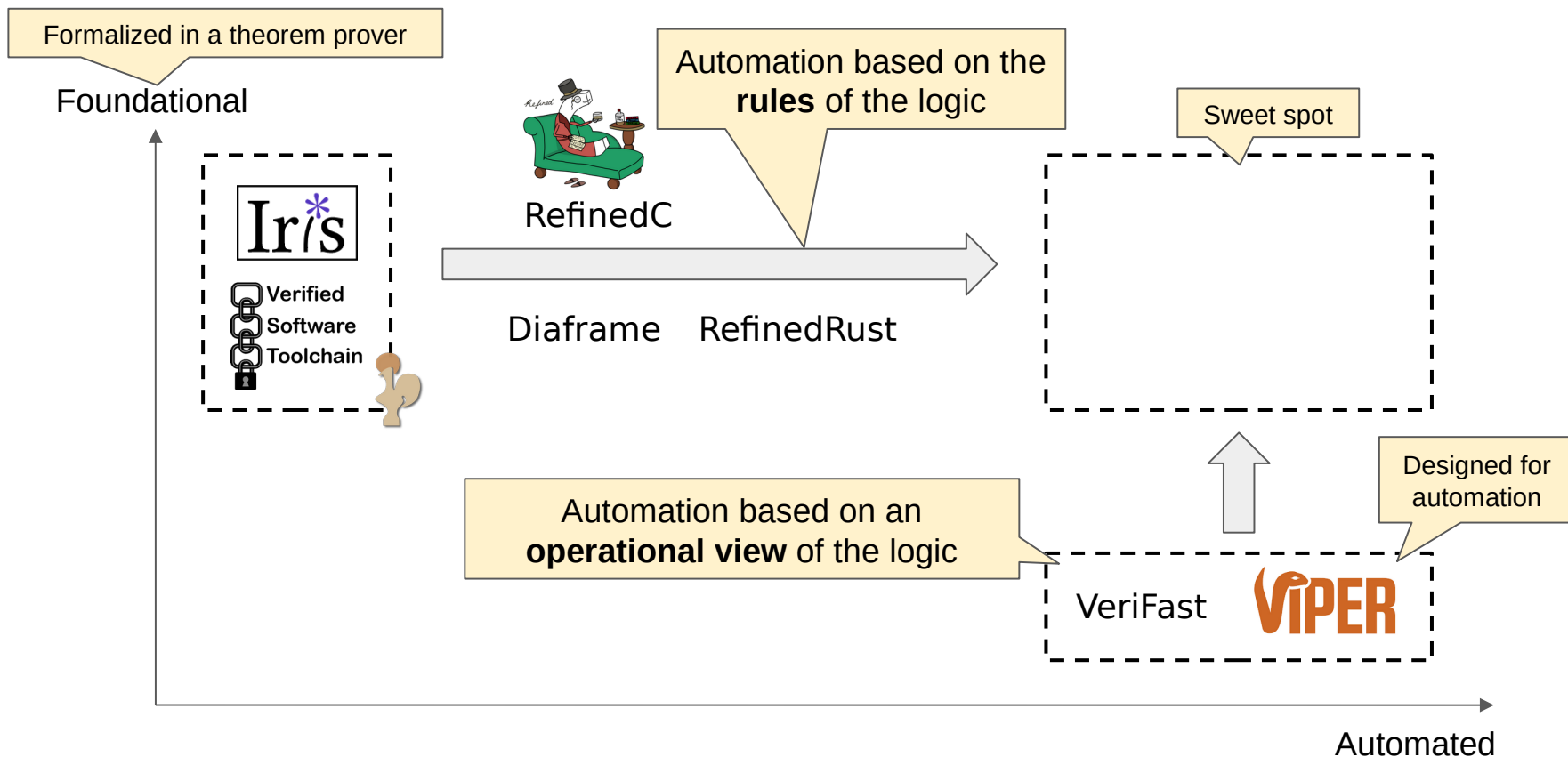
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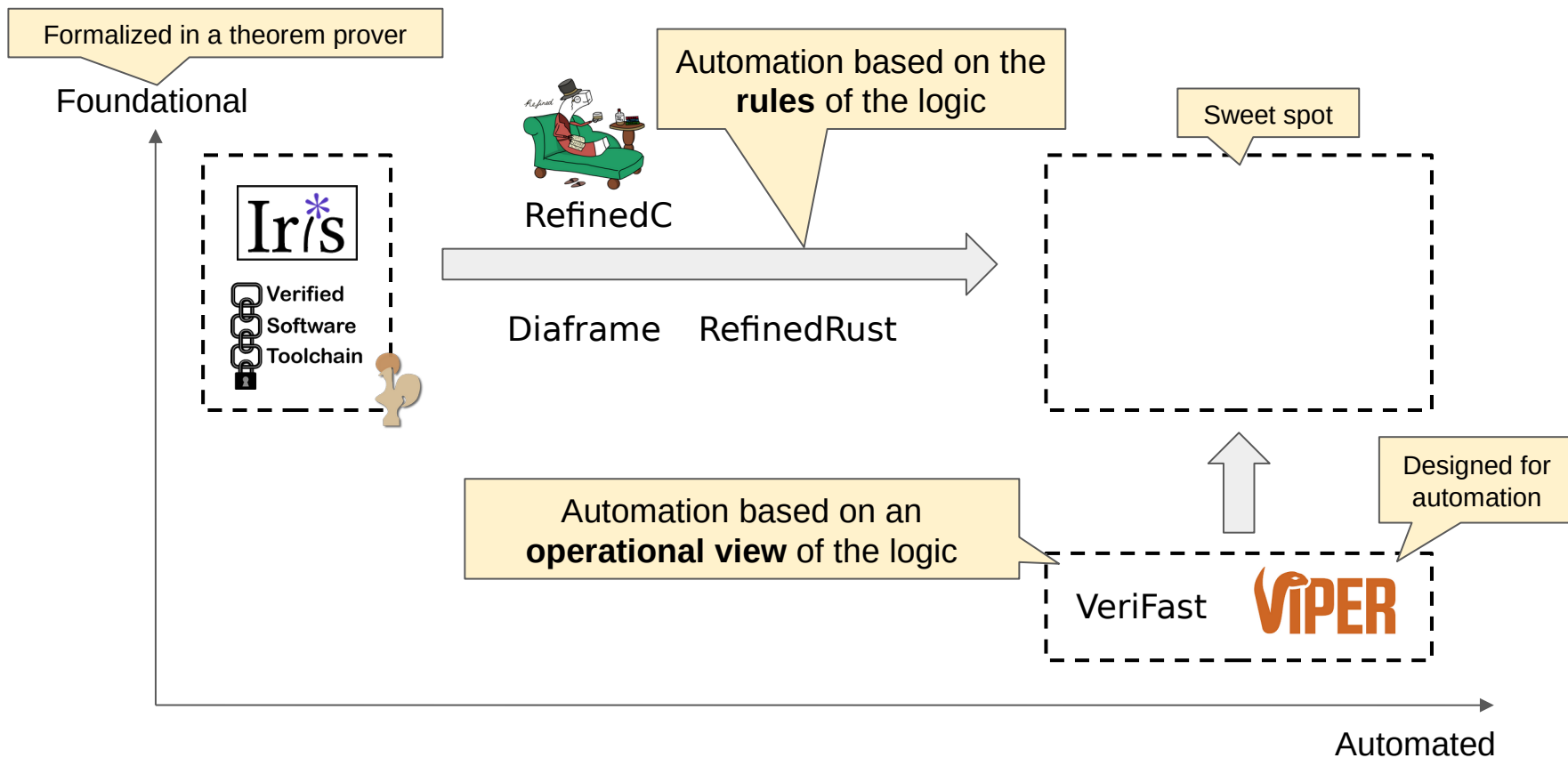
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Program Verifiers Based on Separation Logic



*highly non-exhaustive (missing Steel, GRASShopper, Gillian, ...)

Outline of the Talk

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1. Overview of Viper

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2. Inhale and Exhale: An Operational View of Separation Logic

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4. Toward a Foundational Viper

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Demo

```
1 field x: Int
2 field y: Int
3
4 method main(point: Ref)
5   requires acc(point.x) && acc(point.y)
6   // point.x |-> _ * point.y |-> _
7   {
8     point.x := 5
9     point.y := 7
10    add(point)
11    assert point.x == 5
12    assert point.y == 12
13  }
14
15 method add(p: Ref)
16   requires acc(p.x, 1/2) && acc(p.y)
17   ensures acc(p.x, 1/2) && acc(p.y)
18   // ensures p.y == old(p.x + p.y)
19   {
20     p.y := p.x + p.y
21   }
```

The Viper Verification Framework

The Viper Verification Framework

front-end
program



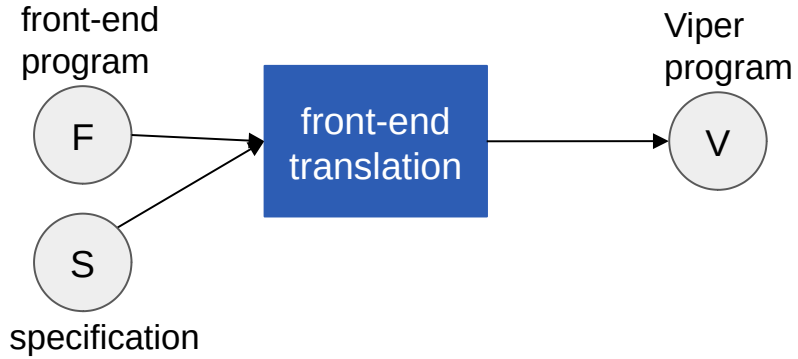
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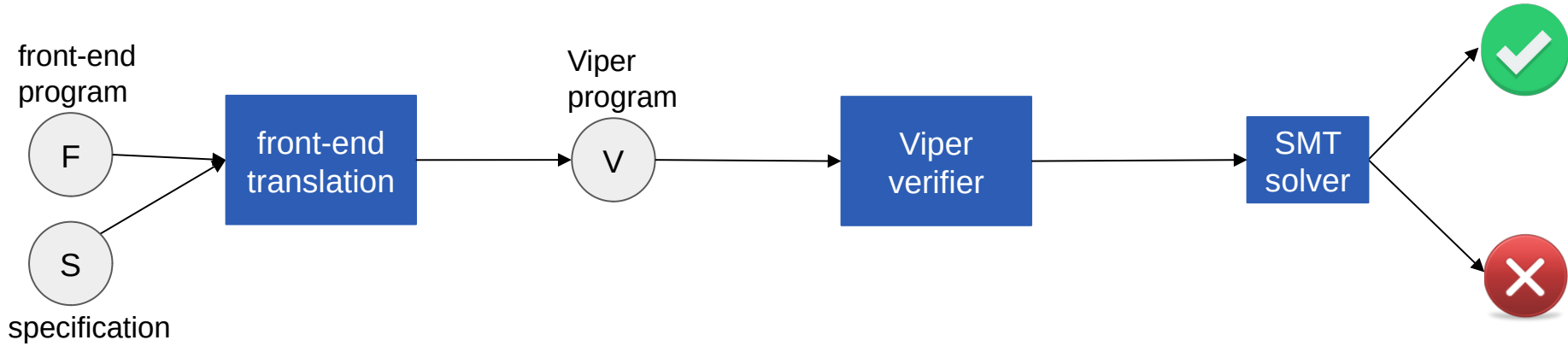


specification

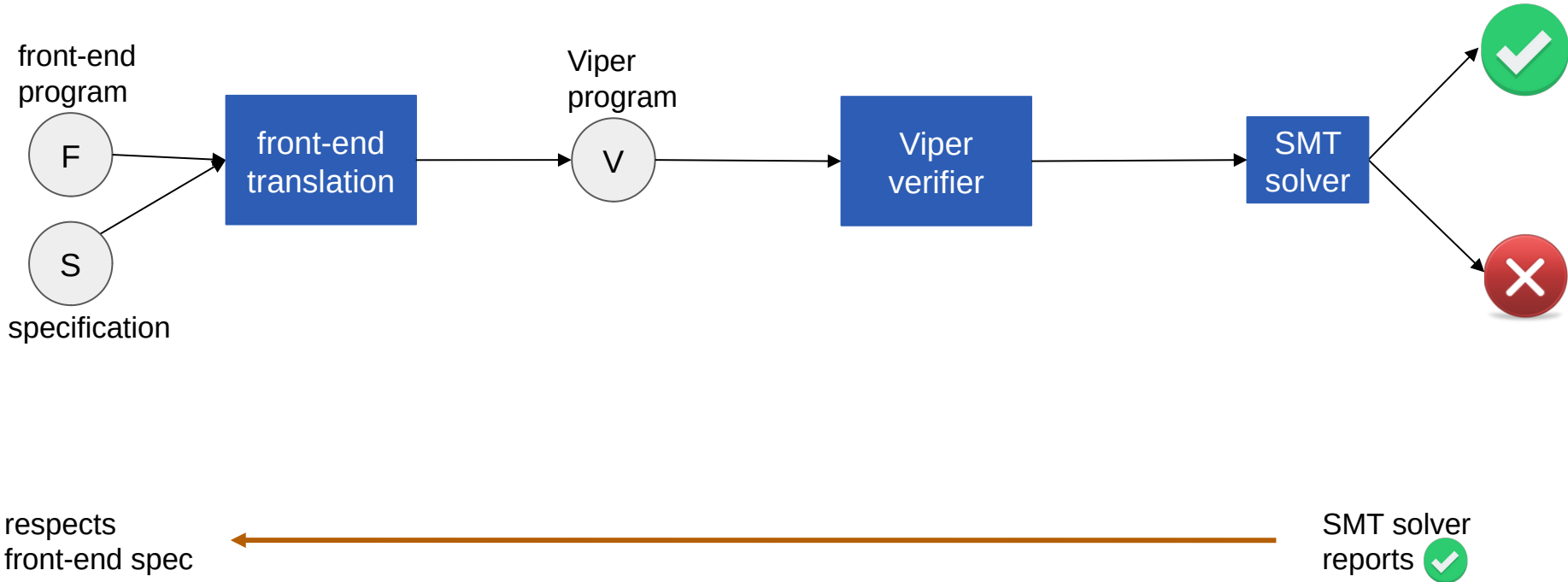
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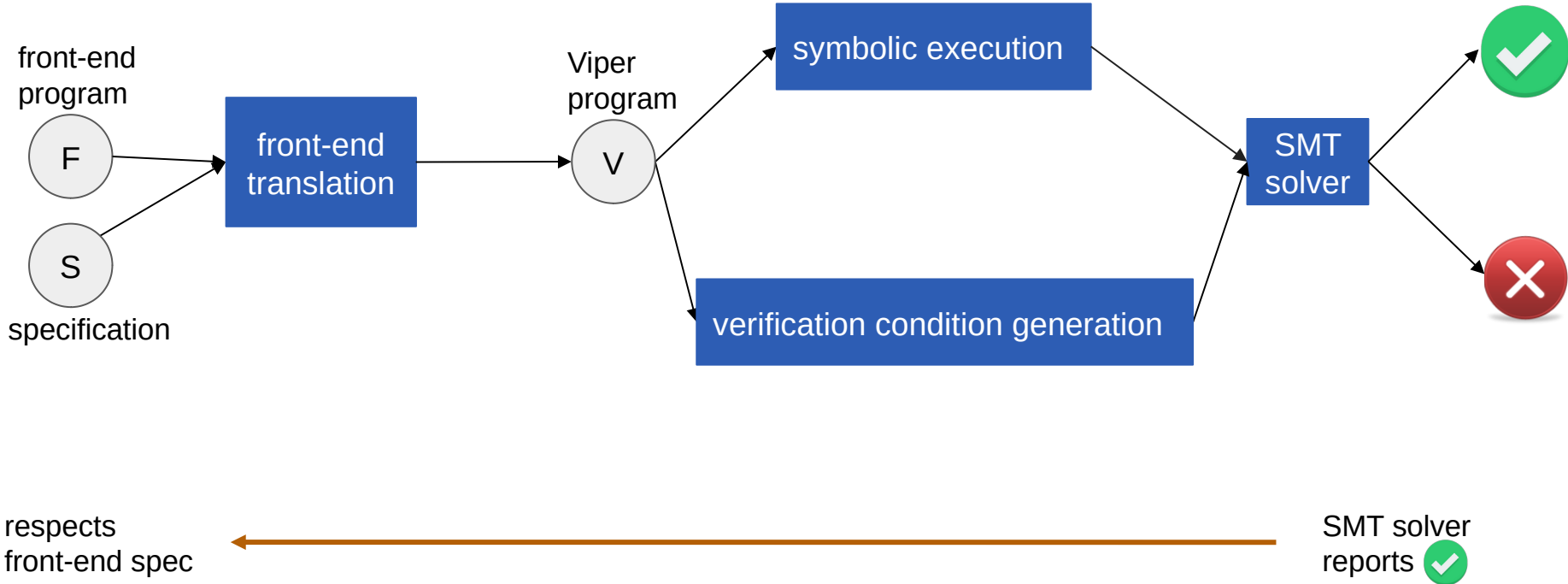
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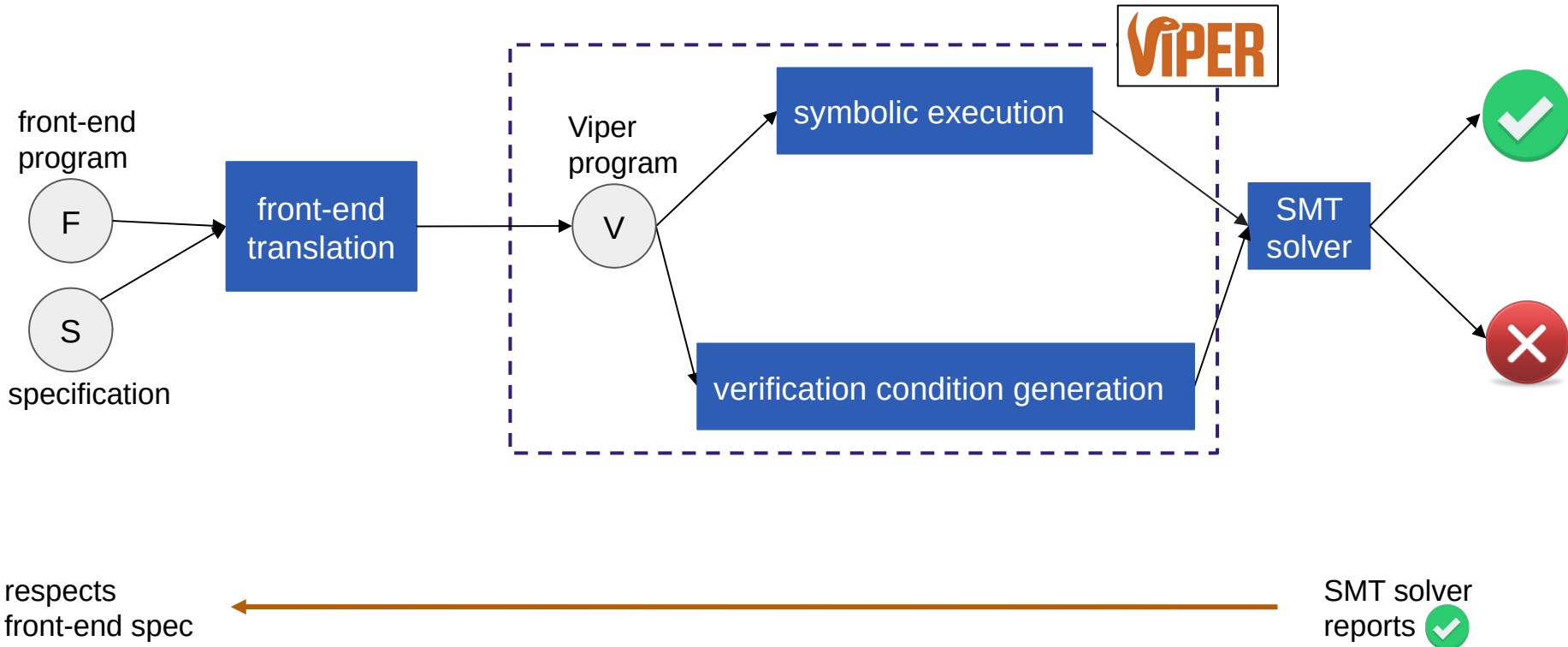
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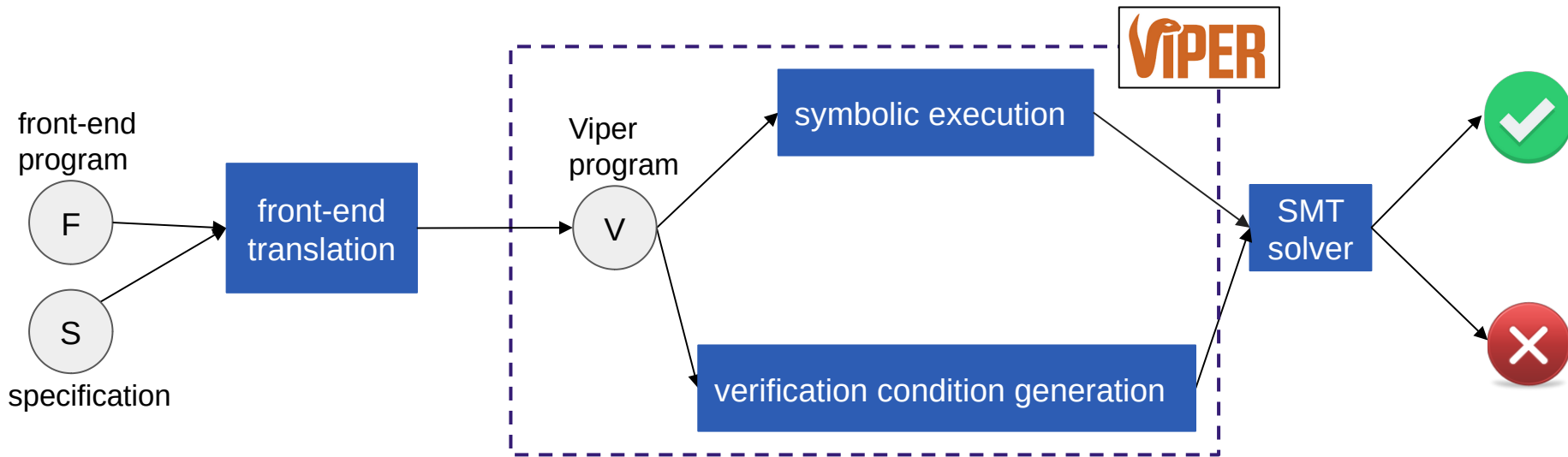
The Viper Verification Framework



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The Viper Verification Framework



Program verifiers built on top of Viper

Rust (*Prusti*)

Go (*Gobra*)

Python (*Nagini*)

Java, C, OpenCL, OpenMP (*VerCors*)

Smart contracts

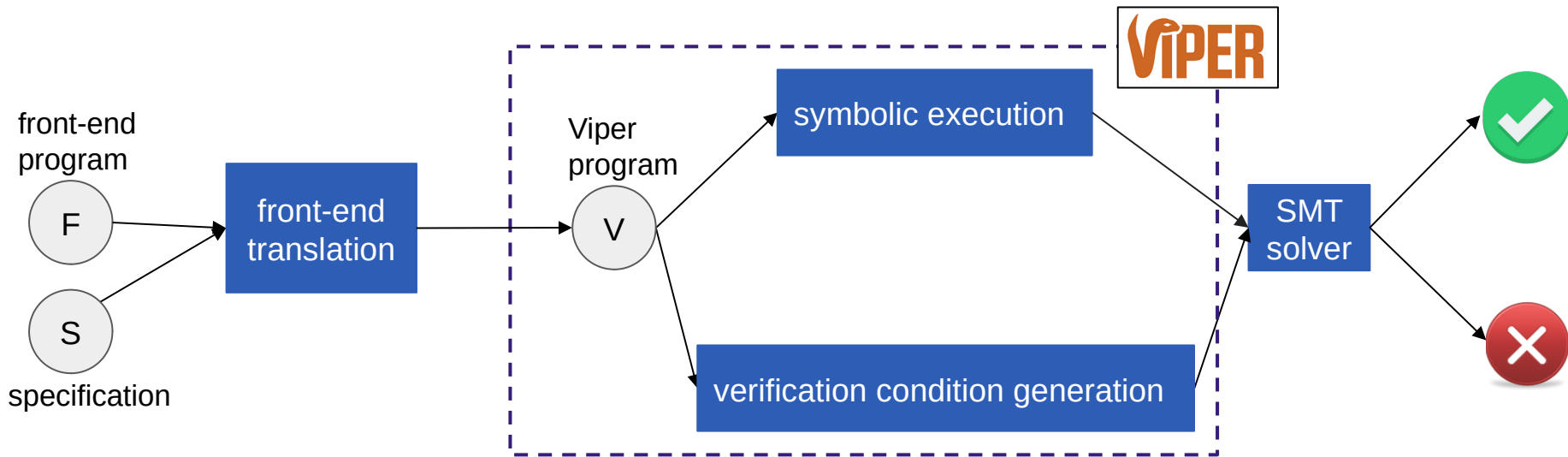
RSL, FSL, FSL++

Secure information flow

Gradual verification

...

The Viper Verification Framework



Program verifiers built on top of Viper

Verification of the SCION Internet architecture
(existing router implementation ~5k LOC)

Rust (*Prusti*)

Go (*Gobra*)

Python (*Nagini*)

Java, C, OpenCL, OpenMP (*VerCors*)

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RSL, FSL, FSL++

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Overview of the Viper Language

Program Code

Assertion Language

Verification Features

Mathematical Background

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Program Code

- Sequential, imperative language
- Standard control structures
- Basic type system
- Built-in heap

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- Fractional permissions

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Assertion Language

- Fractional permissions
- Inductive predicates

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Verification Features

- Standard contract features
- Inhale and exhale
- ...

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Verification Features

- Standard contract features
- Inhale and exhale
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Mathematical Background

- Predefined and user-defined datatypes
- Uninterpreted functions
- Axioms

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- 2. Inhale and Exhale: An Operational View of Separation Logic**
3. Designed for Automation
4. Toward a Foundational Viper

Verification Primitives: Inhale and Exhale

Verification Primitives: Inhale and Exhale

inhale A

exhale A

Verification Primitives: Inhale and Exhale



Verification Primitives: Inhale and Exhale



Adds resources specified by A to the current context

Verification Primitives: Inhale and Exhale



Adds resources specified by A to the current context

Removes resources specified by A from the current context

Verification Primitives: Inhale and Exhale

	inhale A	exhale A
Intuitive meaning	Adds resources specified by A to the current context	Removes resources specified by A from the current context
Logically		
Operationally		

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Acting on a SL state
(e.g., $\text{Loc} \rightarrow (0, 1] \times \text{Val}$)

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SL analogue of	assume A	assert A

Verification Primitives: Inhale and Exhale

“A Basis for Verifying Multi-Threaded Programs” (Leino and Müller, ESOP 2009)

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Sometimes called
produce

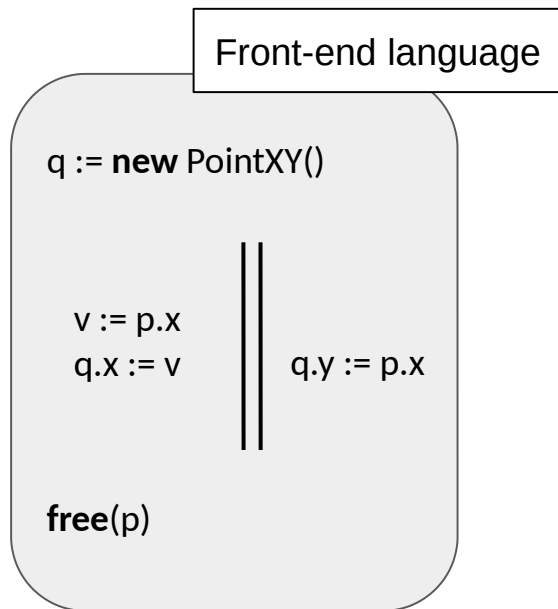
inhale A

Sometimes called
consume

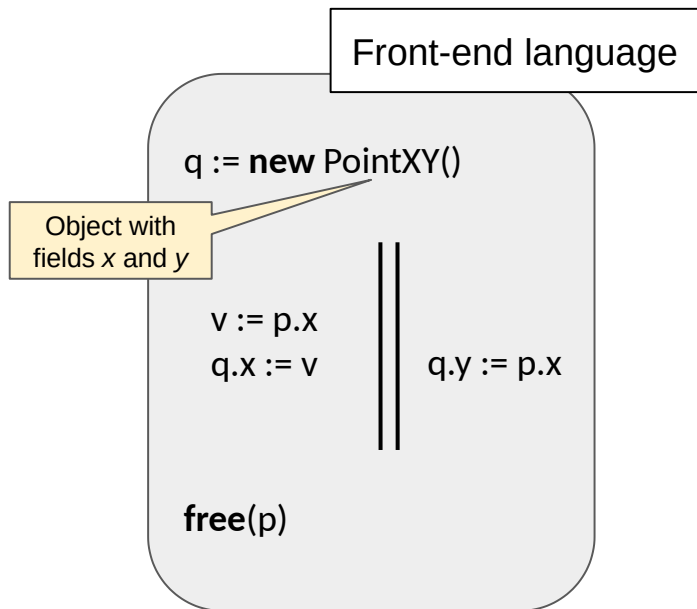
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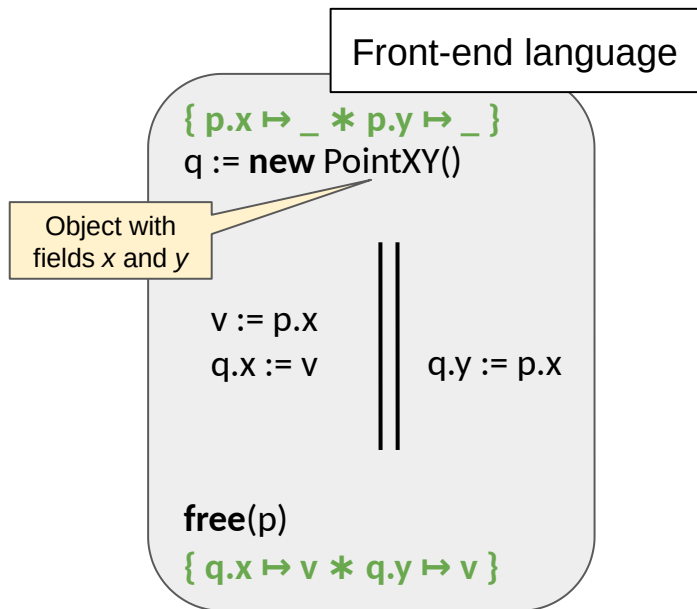
Example: Verifying a Parallel Composition (1/2)



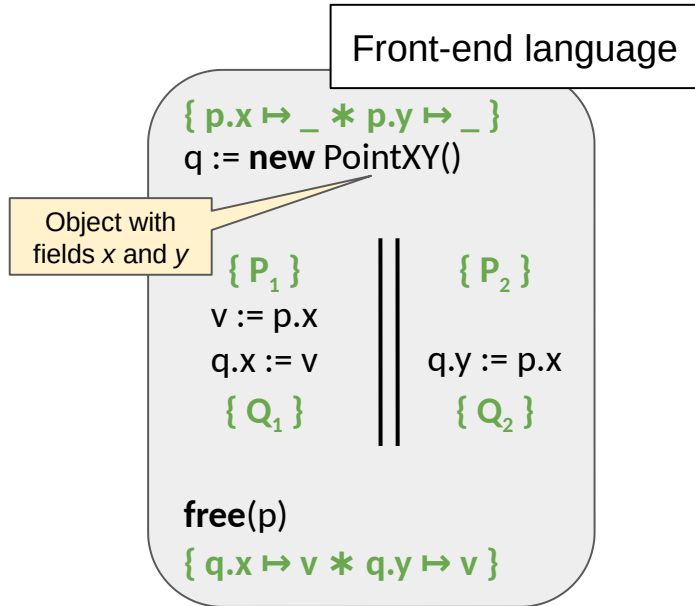
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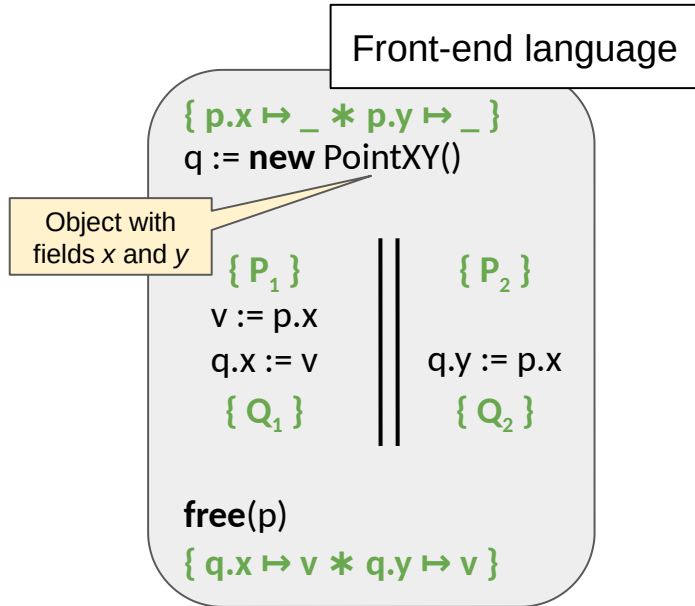
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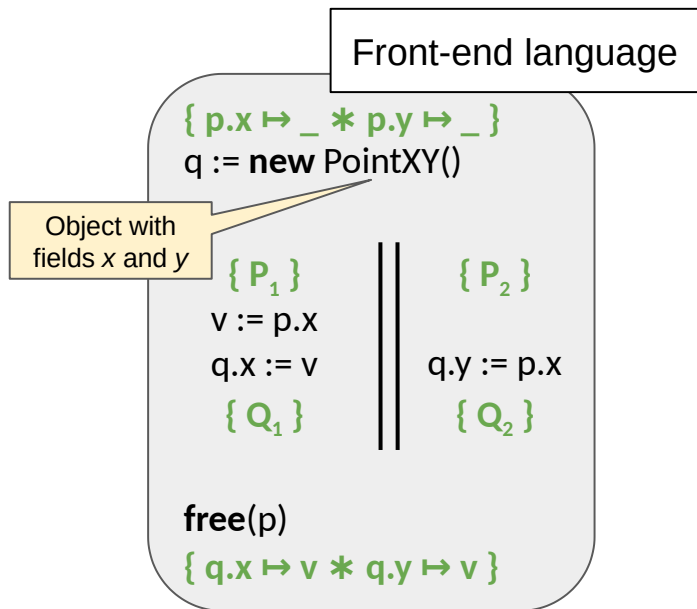


Example: Verifying a Parallel Composition (1/2)



$$P_1 \triangleq (q.x \mapsto _ * p.x \xrightarrow{1/2} _) \quad P_2 \triangleq (q.y \mapsto _ * p.x \xrightarrow{1/2} _)$$

Example: Verifying a Parallel Composition (1/2)

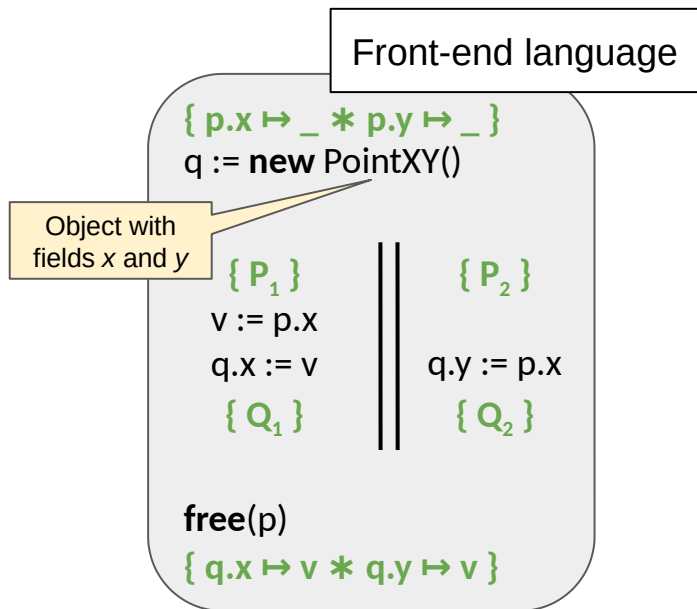


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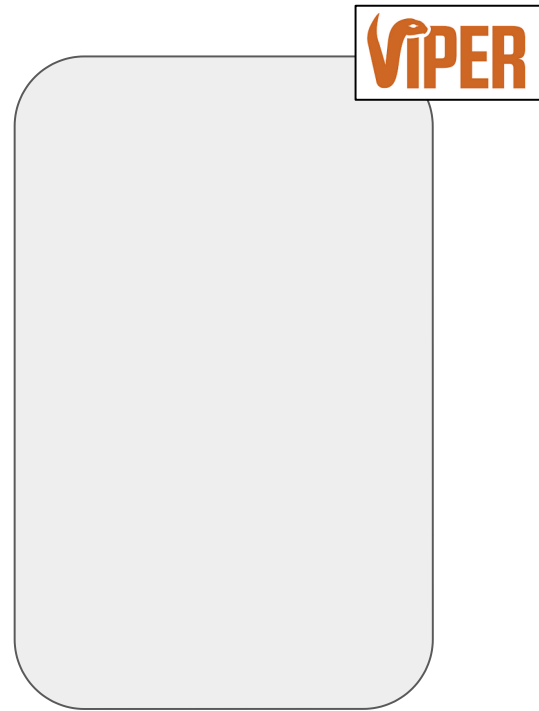
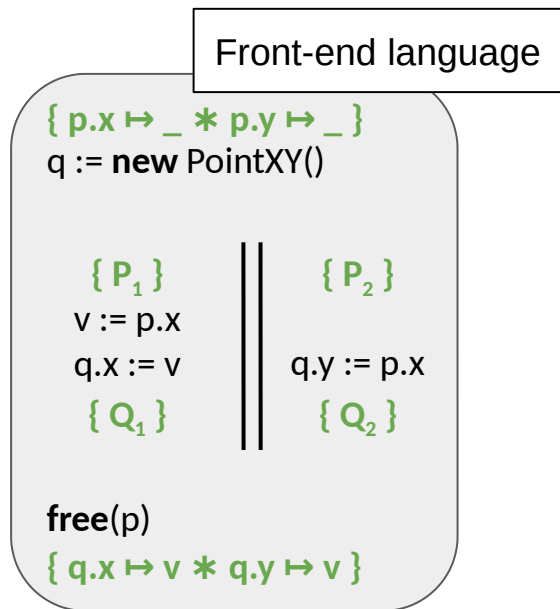
$$Q_1 \triangleq (q.x \mapsto v * p.x \xrightarrow{1/2} v)$$

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$$\begin{aligned}
 P_1 &\triangleq (q.x \mapsto _ * p.x \xrightarrow{1/2} _) & P_2 &\triangleq (q.y \mapsto _ * p.x \xrightarrow{1/2} _) \\
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Example: Verifying a Parallel Composition (1/2)

Front-end language

$\{ p.x \mapsto _ * p.y \mapsto _ \}$

$q := \text{new PointXY}()$

$\{ P_1 \}$

$v := p.x$

$q.x := v$

$\{ Q_1 \}$

$\{ P_2 \}$

$q.y := p.x$

$\{ Q_2 \}$

free(p)

$\{ q.x \mapsto v * q.y \mapsto v \}$

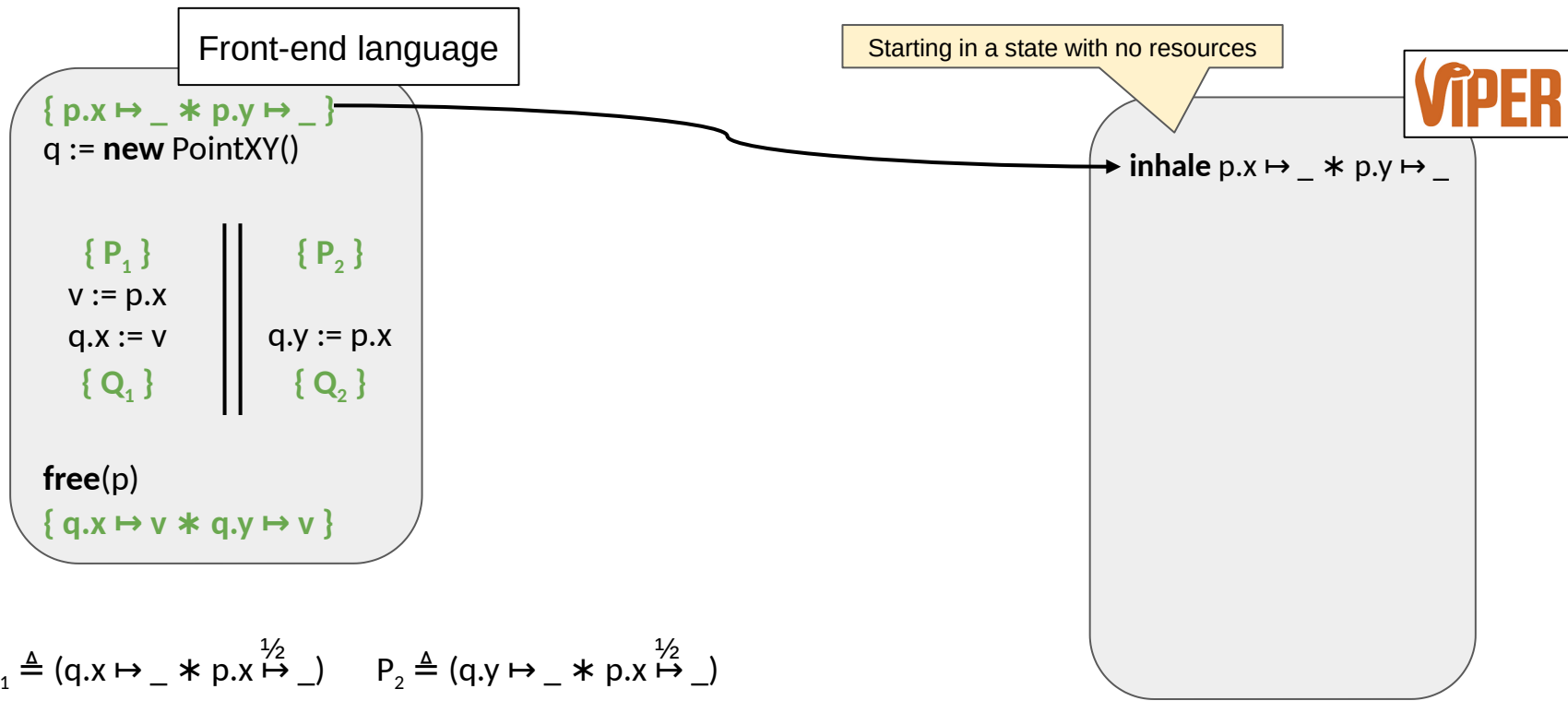
Starting in a state with no resources

VIPER

$$P_1 \triangleq (q.x \mapsto _ * p.x \stackrel{1/2}{\mapsto} _) \quad P_2 \triangleq (q.y \mapsto _ * p.x \stackrel{1/2}{\mapsto} _)$$

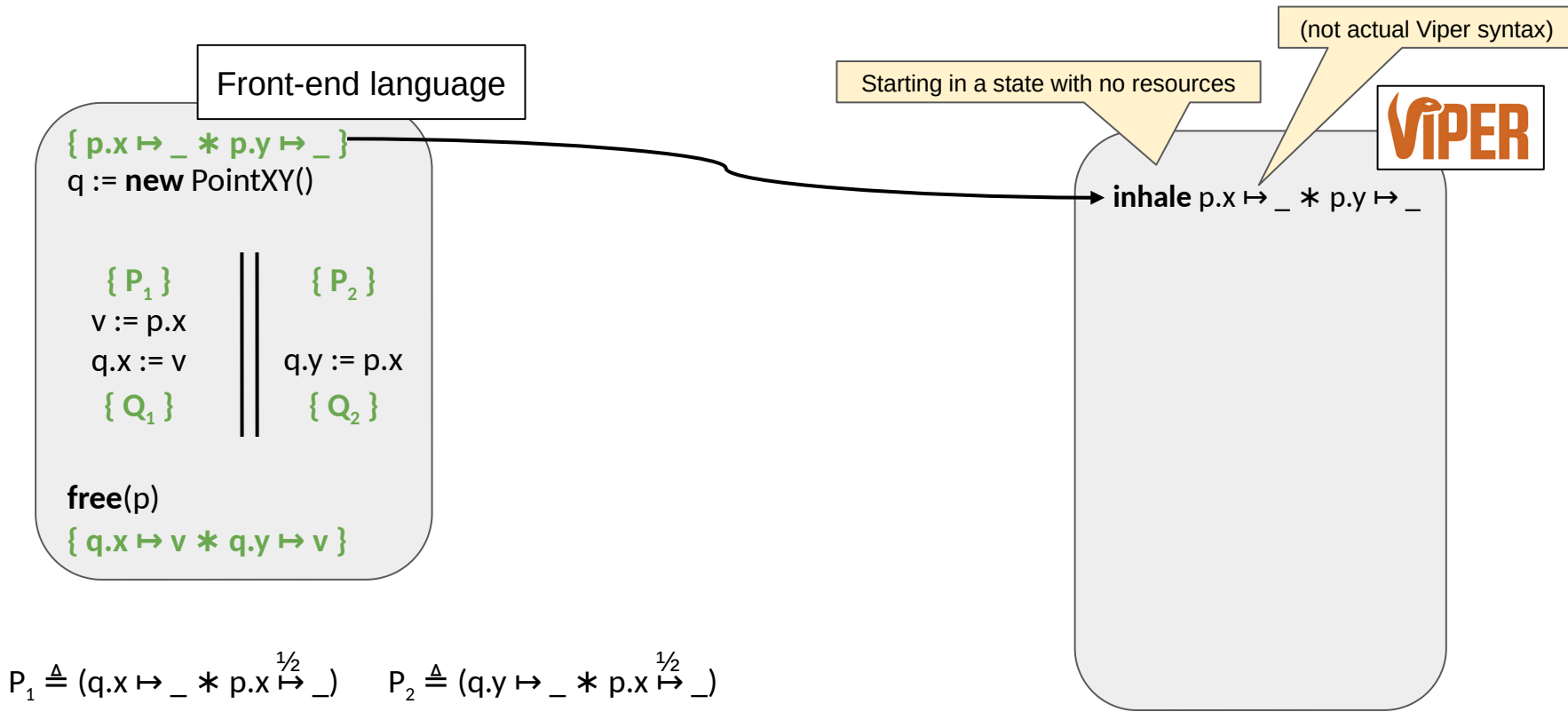
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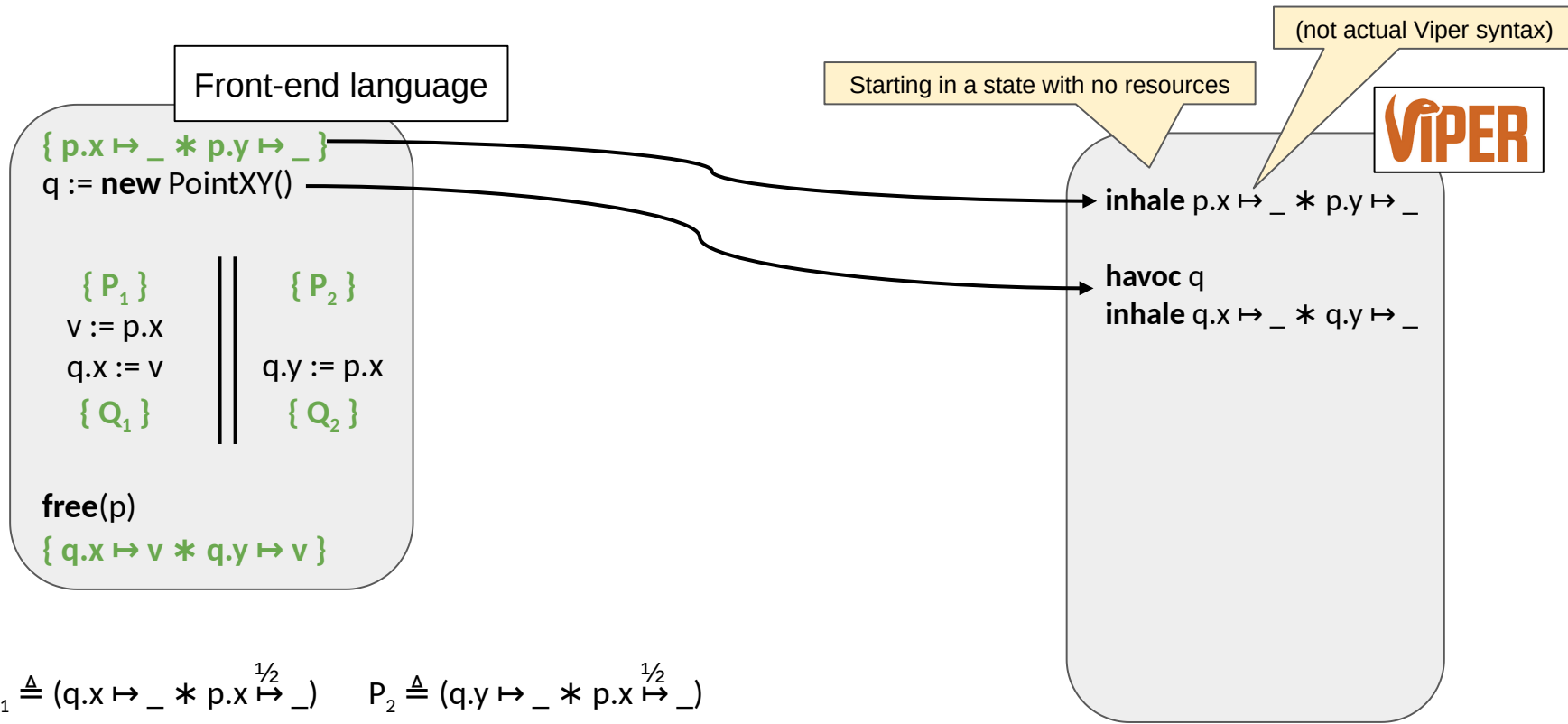
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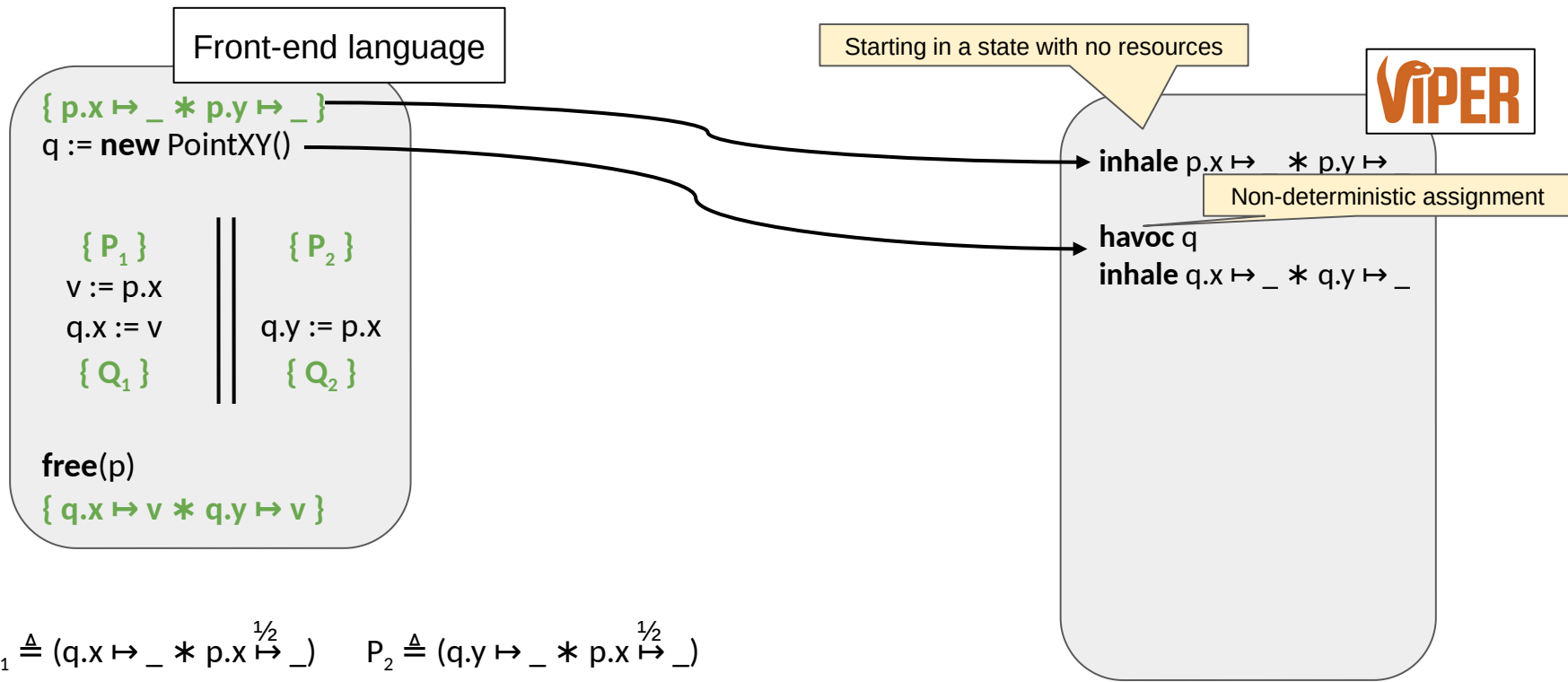
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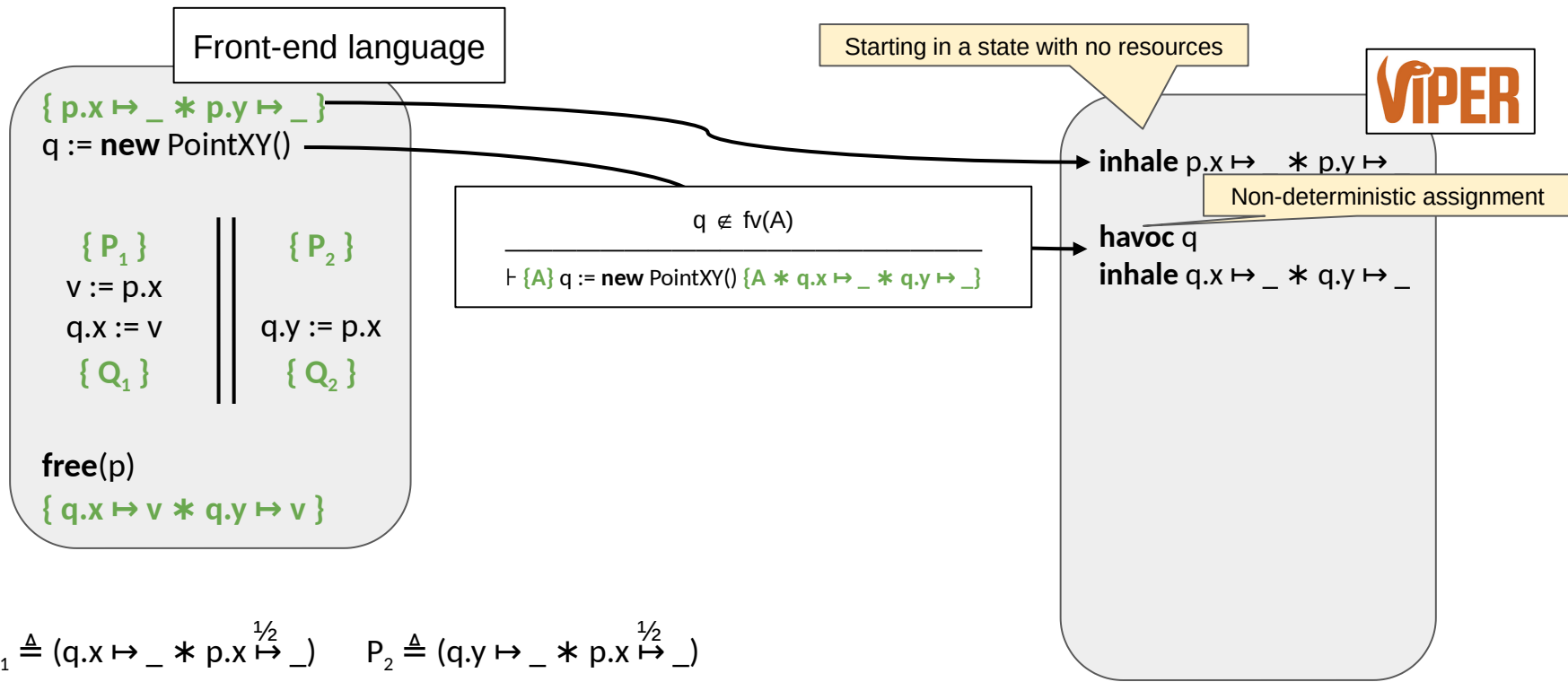
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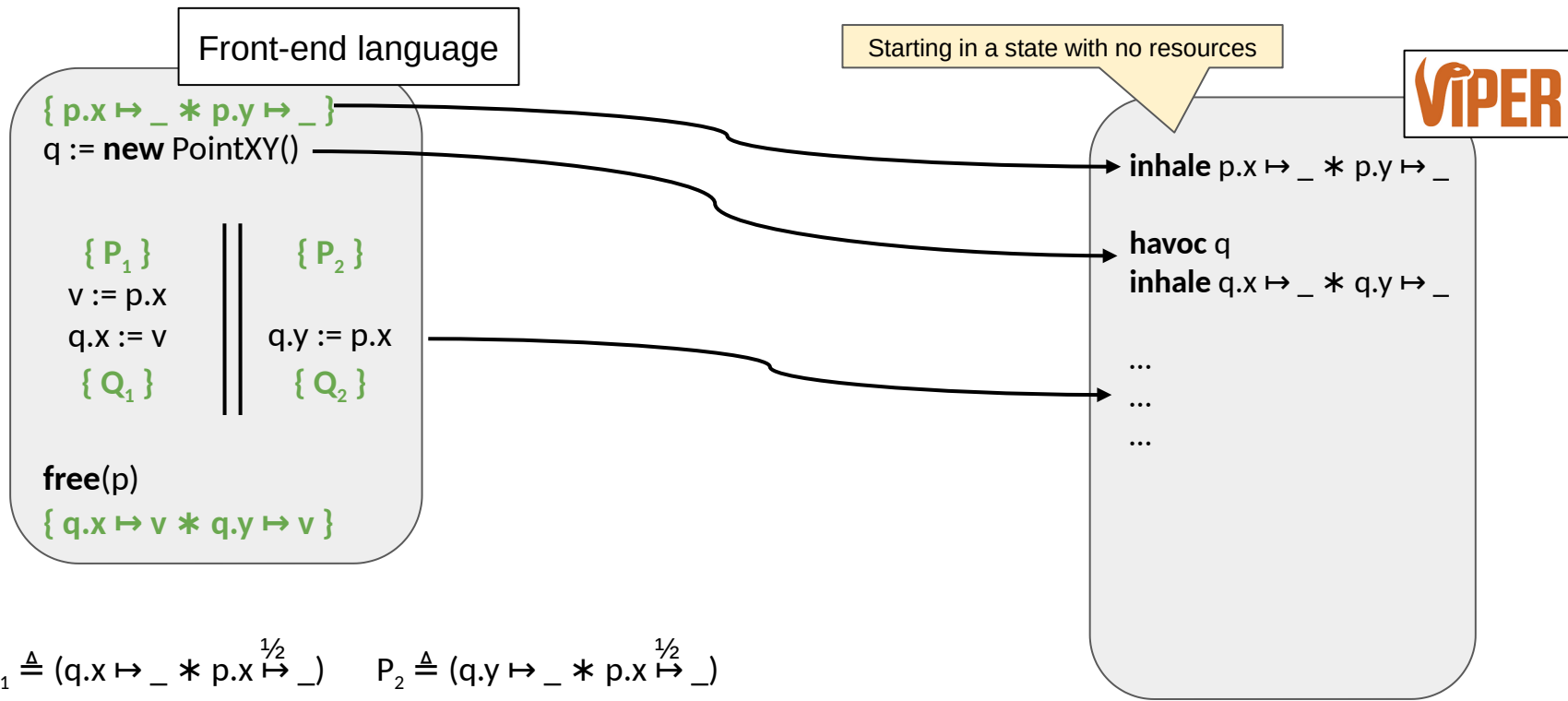
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 P_1 &\triangleq (q.x \mapsto _ * p.x \stackrel{1/2}{\mapsto} _) & P_2 &\triangleq (q.y \mapsto _ * p.x \stackrel{1/2}{\mapsto} _) \\
 Q_1 &\triangleq (q.x \mapsto v * p.x \stackrel{1/2}{\mapsto} v) & Q_2 &\triangleq (\exists k. q.y \mapsto k * p.x \stackrel{1/2}{\mapsto} k)
 \end{aligned}$$

Example: Verifying a Parallel Composition (1/2)



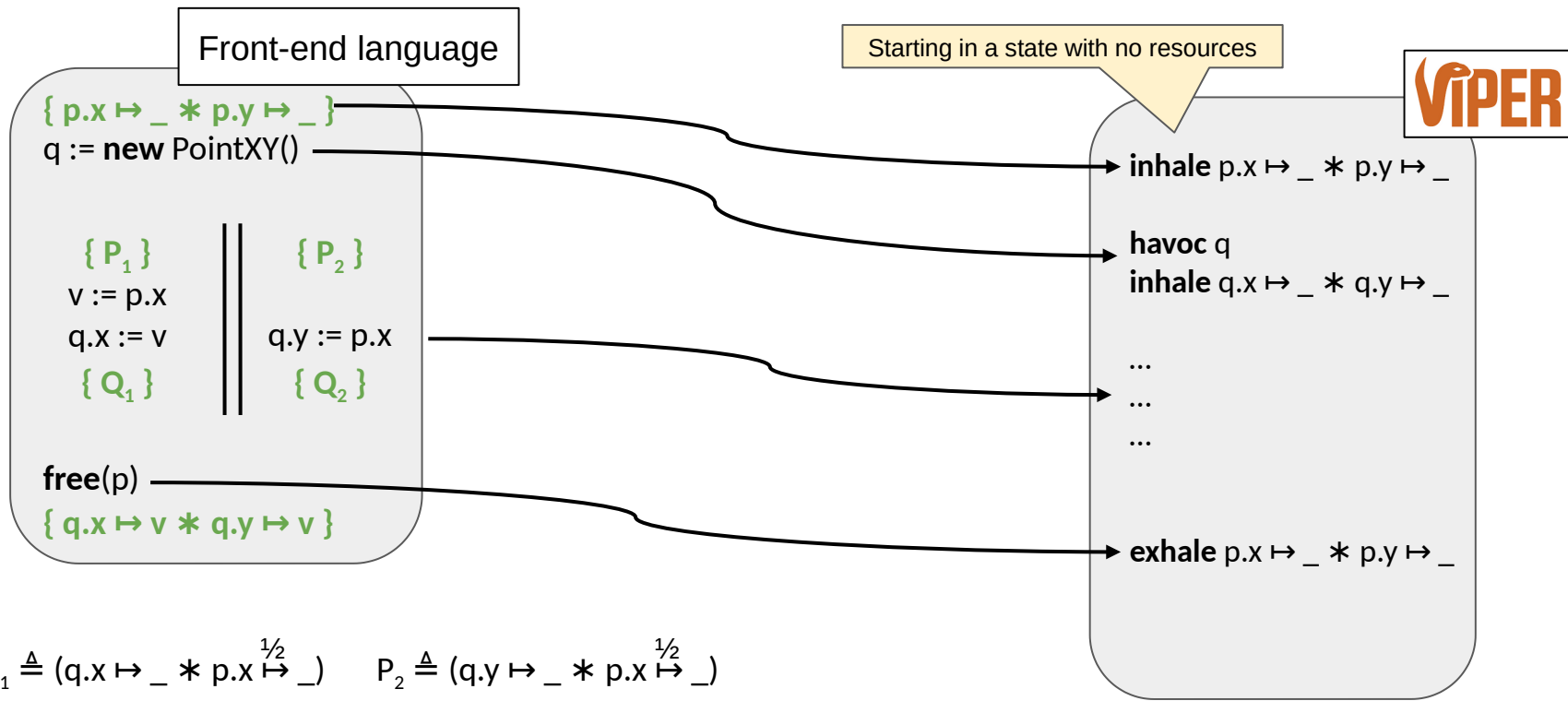
$$\begin{aligned}
 P_1 &\triangleq (q.x \mapsto _ * p.x \overset{1/2}{\mapsto} _) & P_2 &\triangleq (q.y \mapsto _ * p.x \overset{1/2}{\mapsto} _) \\
 Q_1 &\triangleq (q.x \mapsto v * p.x \overset{1/2}{\mapsto} v) & Q_2 &\triangleq (\exists k. q.y \mapsto k * p.x \overset{1/2}{\mapsto} k)
 \end{aligned}$$

Example: Verifying a Parallel Composition (1/2)



$$\begin{aligned}
 P_1 &\triangleq (q.x \mapsto _ * p.x \overset{1/2}{\mapsto} _) & P_2 &\triangleq (q.y \mapsto _ * p.x \overset{1/2}{\mapsto} _) \\
 Q_1 &\triangleq (q.x \mapsto v * p.x \overset{1/2}{\mapsto} v) & Q_2 &\triangleq (\exists k. q.y \mapsto k * p.x \overset{1/2}{\mapsto} k)
 \end{aligned}$$

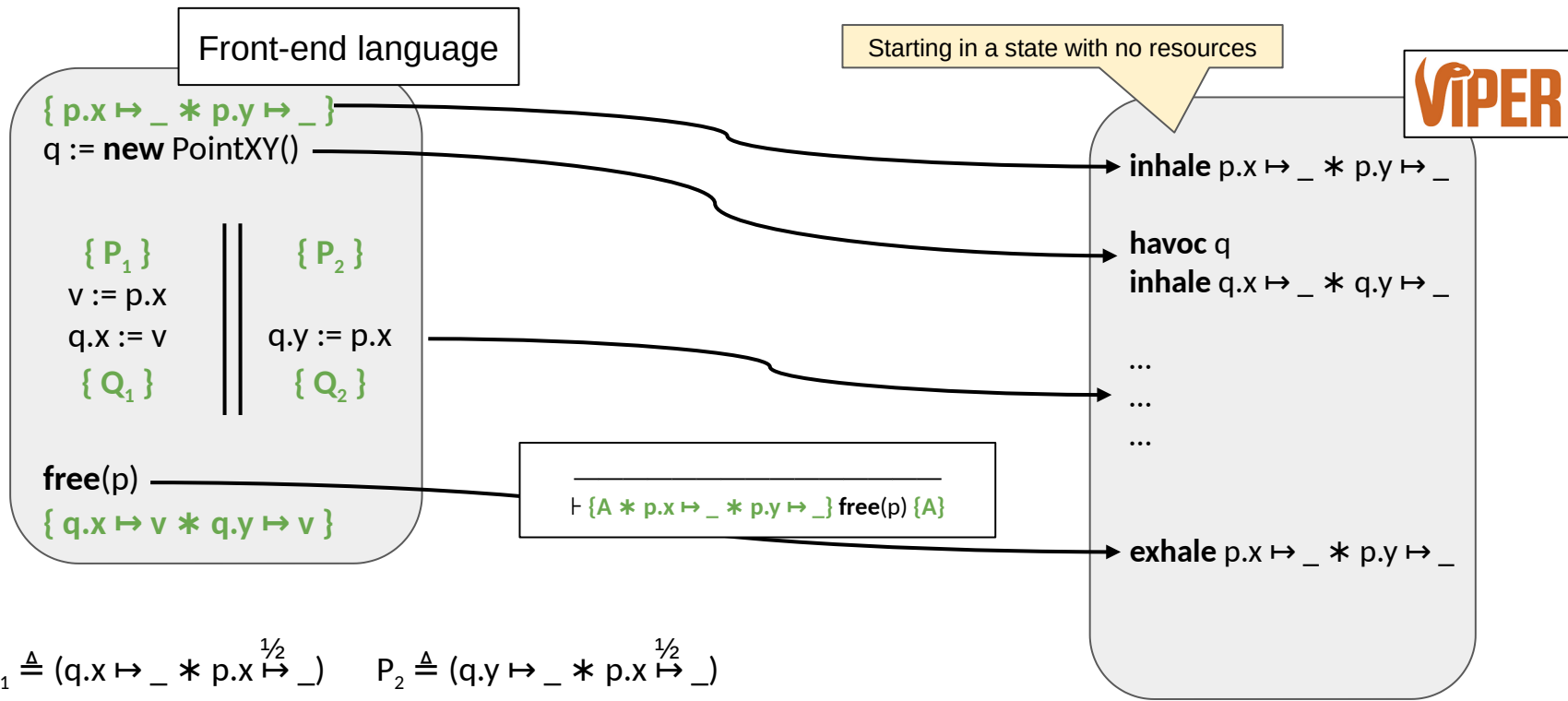
Example: Verifying a Parallel Composition (1/2)



$$P_1 \triangleq (q.x \mapsto _ * p.x \overset{1/2}{\mapsto} _) \quad P_2 \triangleq (q.y \mapsto _ * p.x \overset{1/2}{\mapsto} _)$$

$$Q_1 \triangleq (q.x \mapsto v * p.x \overset{1/2}{\mapsto} v) \quad Q_2 \triangleq (\exists k. q.y \mapsto k * p.x \overset{1/2}{\mapsto} k)$$

Example: Verifying a Parallel Composition (1/2)



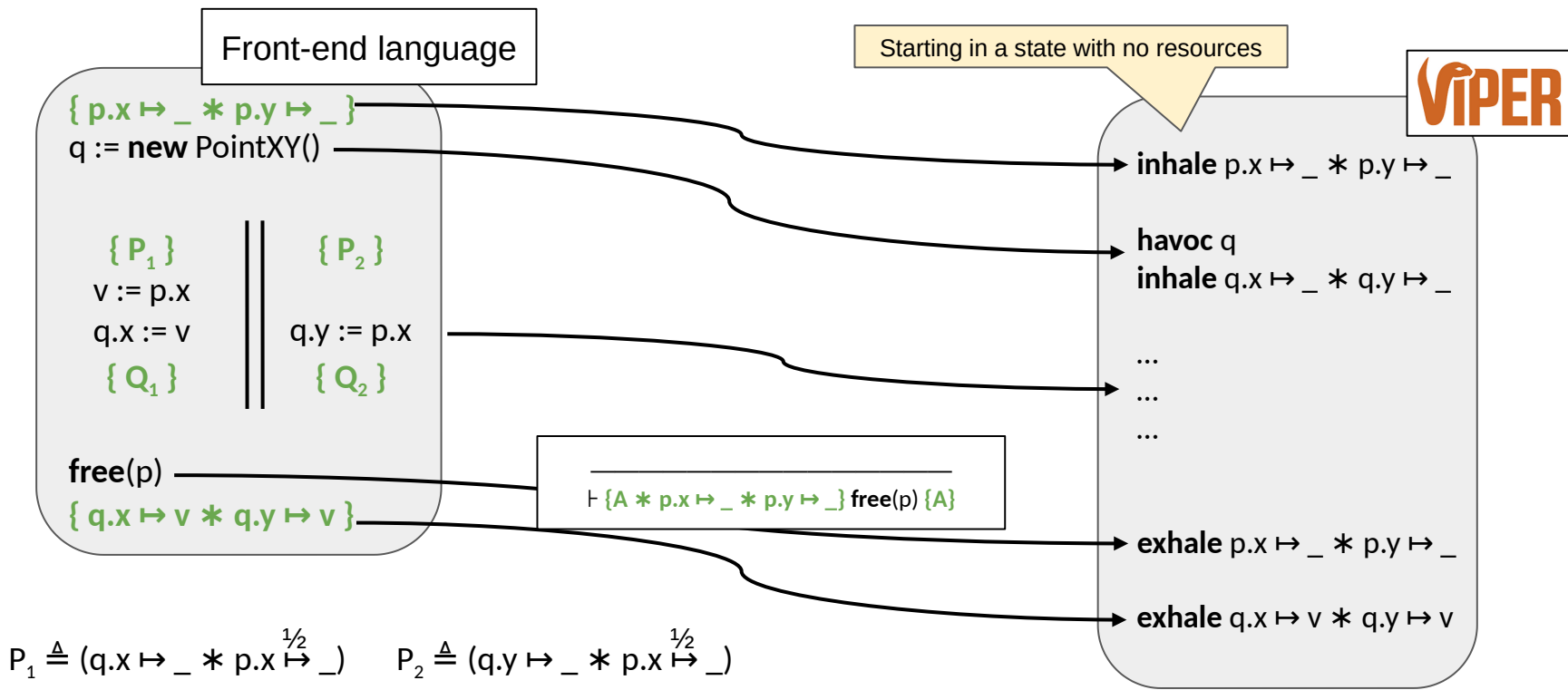
$$P_1 \triangleq (q.x \mapsto _ * p.x \overset{1/2}{\mapsto} _)$$

$$P_2 \triangleq (q.y \mapsto _ * p.x \overset{1/2}{\mapsto} _)$$

$$Q_1 \triangleq (q.x \mapsto v * p.x \overset{1/2}{\mapsto} v)$$

$$Q_2 \triangleq (\exists k. q.y \mapsto k * p.x \overset{1/2}{\mapsto} k)$$

Example: Verifying a Parallel Composition (1/2)



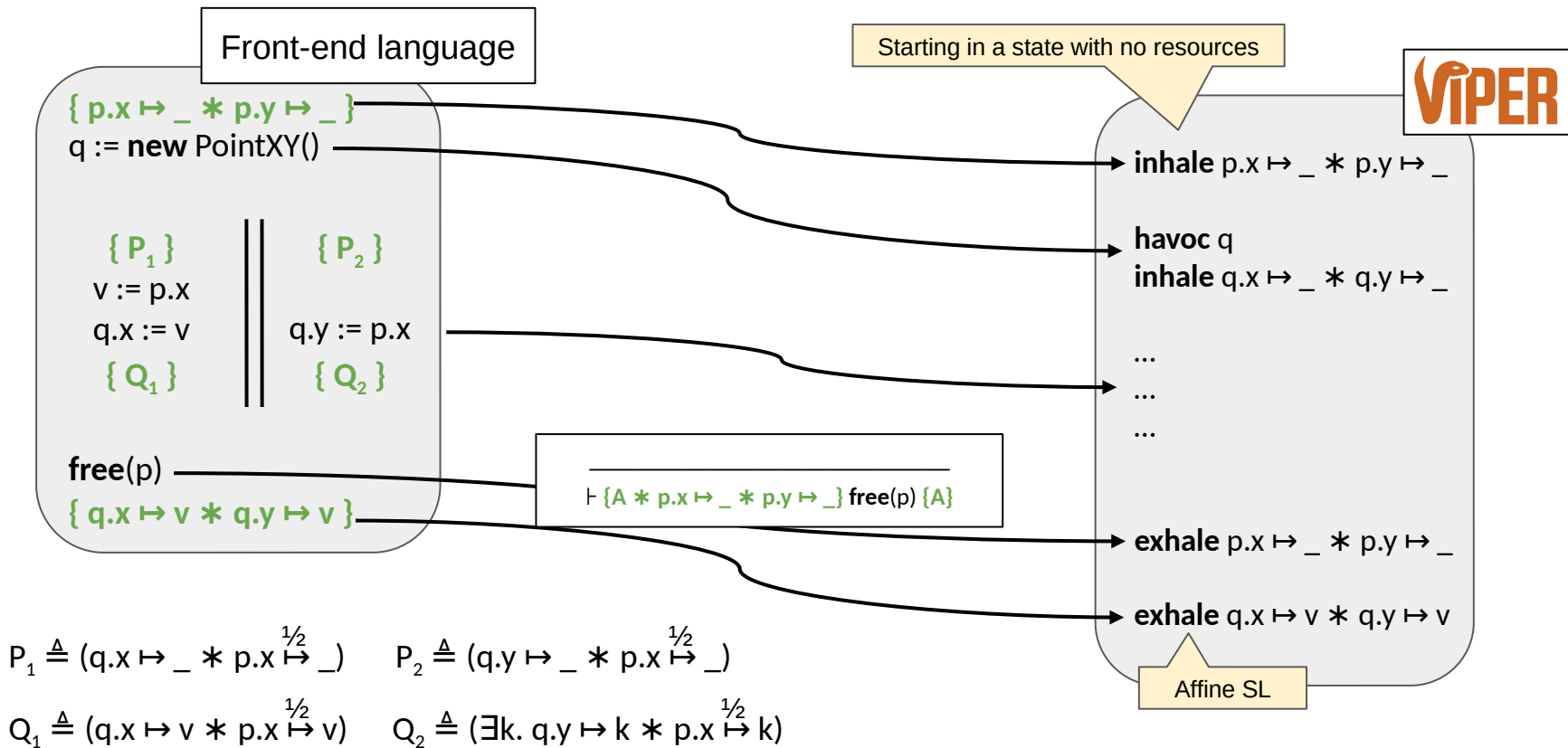
$$P_1 \triangleq (q.x \mapsto _ * p.x \overset{1/2}{\mapsto} _)$$

$$P_2 \triangleq (q.y \mapsto _ * p.x \overset{1/2}{\mapsto} _)$$

$$Q_1 \triangleq (q.x \mapsto v * p.x \overset{1/2}{\mapsto} v)$$

$$Q_2 \triangleq (\exists k. q.y \mapsto k * p.x \overset{1/2}{\mapsto} k)$$

Example: Verifying a Parallel Composition (1/2)



Example: Verifying a Parallel Composition (2/2)

Front-end language

$\{ p.x \mapsto _ * p.y \mapsto _ \}$

$q := \text{new PointXY}()$

$\{ P_1 \}$

$v := p.x$

$q.x := v$

$\{ Q_1 \}$

$\{ P_2 \}$

$q.y := p.x$

$\{ Q_2 \}$

$\text{free}(p)$

$\{ q.x \mapsto v * q.y \mapsto v \}$

VIPER

$\text{inhale } p.x \mapsto _ * p.y \mapsto _$

$\text{havoc } q$

$\text{inhale } q.x \mapsto _ * q.y \mapsto _$

...

...

...

$\text{exhale } p.x \mapsto _ * p.y \mapsto _$

$\text{exhale } q.x \mapsto v * q.y \mapsto v$

Example: Verifying a Parallel Composition (2/2)

Front-end language

```
{ p.x ↦ _ * p.y ↦ _ }  
q := new PointXY()
```

$\{P_1\}$

$v := p.x$

$q.x := v$

$\{Q_1\}$

$\{P_2\}$

$q.y := p.x$

$\{Q_2\}$

$\text{free}(p)$

```
{ q.x ↦ v * q.y ↦ v }
```

VIPER

```
inhale p.x ↦ _ * p.y ↦ _
```

```
havoc q
```

```
inhale q.x ↦ _ * q.y ↦ _
```

...

...

...

```
exhale p.x ↦ _ * p.y ↦ _
```

```
exhale q.x ↦ v * q.y ↦ v
```

Example: Verifying a Parallel Composition (2/2)

Front-end language

```
{ p.x ↦ _ * p.y ↦ _ }
q := new PointXY()
```

$\{P_1\}$

$v := p.x$

$q.x := v$

$\{Q_1\}$

$\{P_2\}$

$q.y := p.x$

$\{Q_2\}$

free(p)

```
{ q.x ↦ v * q.y ↦ v }
```

$\vdash \{P_1\} C_1 \{Q_1\} \quad \vdash \{P_2\} C_2 \{Q_2\}$

$fv(R) \cap wr(C_1) = \emptyset \quad \dots$

$\vdash \{P_1 * P_2 * R\} C_1 \parallel C_2 \{Q_1 * Q_2 * R\}$

VIPER

```
inhale p.x ↦ _ * p.y ↦ _
```

havoc q

```
inhale q.x ↦ _ * q.y ↦ _
```

...

...

...

```
exhale p.x ↦ _ * p.y ↦ _
```

```
exhale q.x ↦ v * q.y ↦ v
```

Example: Verifying a Parallel Composition (2/2)



Front-end language

```
{ p.x ↦ _ * p.y ↦ _ }
q := new PointXY()
```

$\{P_1\}$

$v := p.x$

$q.x := v$

$\{Q_1\}$

$\{P_2\}$

$q.y := p.x$

$\{Q_2\}$

$\text{free}(p)$

$\{ q.x \mapsto v * q.y \mapsto v \}$

$\vdash \{P_1\} C_1 \{Q_1\} \quad \vdash \{P_2\} C_2 \{Q_2\}$

$\text{fv}(R) \cap \text{wr}(C_1) = \emptyset \quad \dots$

$\vdash \{P_1 * P_2 * R\} C_1 \parallel C_2 \{Q_1 * Q_2 * R\}$

inhale P_1
 $v := p.x$
 $q.x := v$
exhale Q_1

inhale $p.x \mapsto _ * p.y \mapsto _$

havoc q

inhale $q.x \mapsto _ * q.y \mapsto _$

...

...

...

exhale $p.x \mapsto _ * p.y \mapsto _$

exhale $q.x \mapsto v * q.y \mapsto v$

Example: Verifying a Parallel Composition (2/2)



Front-end language

```

{ p.x ↦ _ * p.y ↦ _ }
q := new PointXY()

{ P1 }      ||      { P2 }
v := p.x    ||      q.y := p.x
q.x := v    ||      { Q2 }
{ Q1 }

free(p)

{ q.x ↦ v * q.y ↦ v }
    
```

$$\frac{\vdash \{P_1\} C_1 \{Q_1\} \quad \vdash \{P_2\} C_2 \{Q_2\} \quad \text{fv}(R) \cap \text{wr}(C_1) = \emptyset \quad \dots}{\vdash \{P_1 * P_2 * R\} C_1 || C_2 \{Q_1 * Q_2 * R\}}$$

inhale P_1
 $v := p.x$
 $q.x := v$
exhale Q_1

inhale P_2
 $q.y := p.x$
exhale Q_2

```

inhale p.x ↦ _ * p.y ↦ _

havoc q
inhale q.x ↦ _ * q.y ↦ _

...

exhale p.x ↦ _ * p.y ↦ _

exhale q.x ↦ v * q.y ↦ v
    
```

Example: Verifying a Parallel Composition (2/2)



Front-end language

```
{ p.x ↦ _ * p.y ↦ _ }
q := new PointXY()
```

$\{P_1\}$ $v := p.x$ $q.x := v$ $\{Q_1\}$		$\{P_2\}$ $q.y := p.x$ $\{Q_2\}$
--	--	--

free(p)

```
{ q.x ↦ v * q.y ↦ v }
```

$$\frac{\vdash \{P_1\} C_1 \{Q_1\} \quad \vdash \{P_2\} C_2 \{Q_2\} \quad \text{fv}(R) \cap \text{wr}(C_1) = \emptyset \quad \dots}{\vdash \{P_1 * P_2 * R\} C_1 || C_2 \{Q_1 * Q_2 * R\}}$$

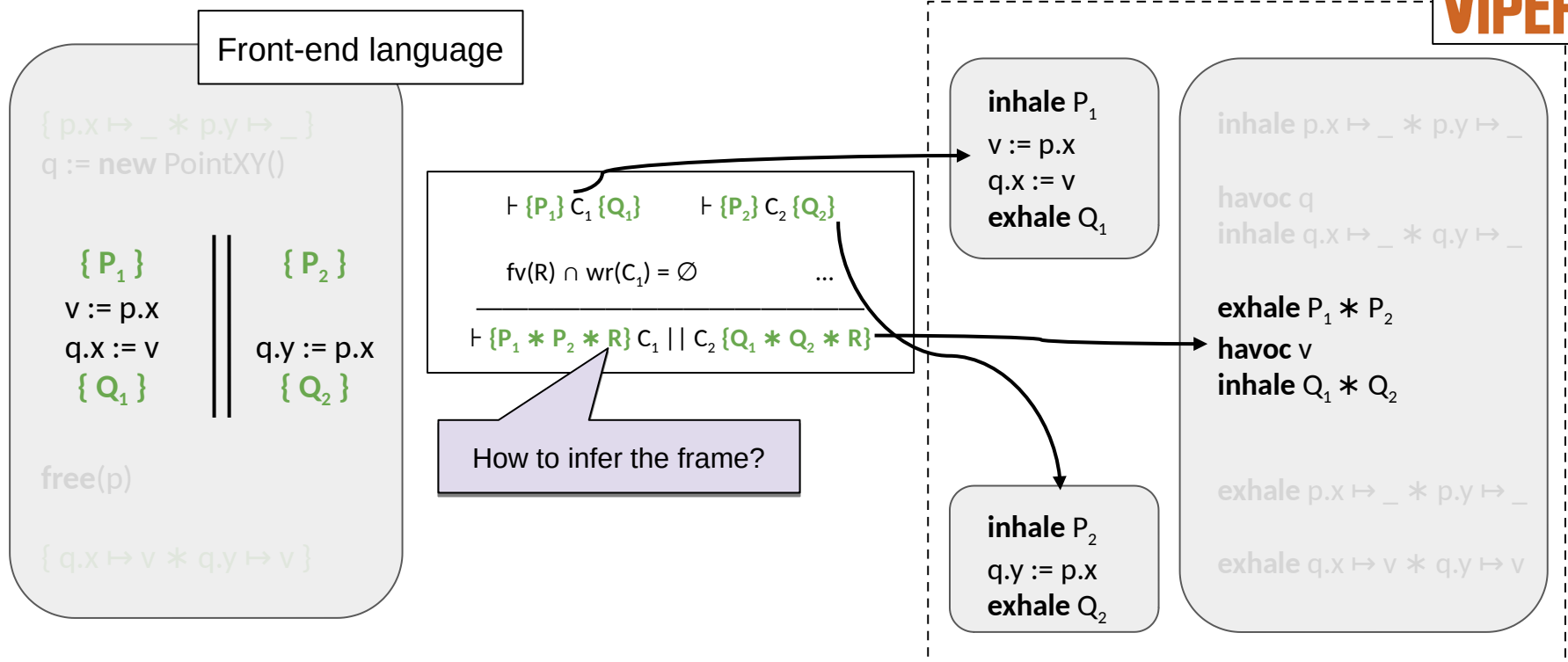
How to infer the frame?

inhale P_1
 $v := p.x$
 $q.x := v$
exhale Q_1

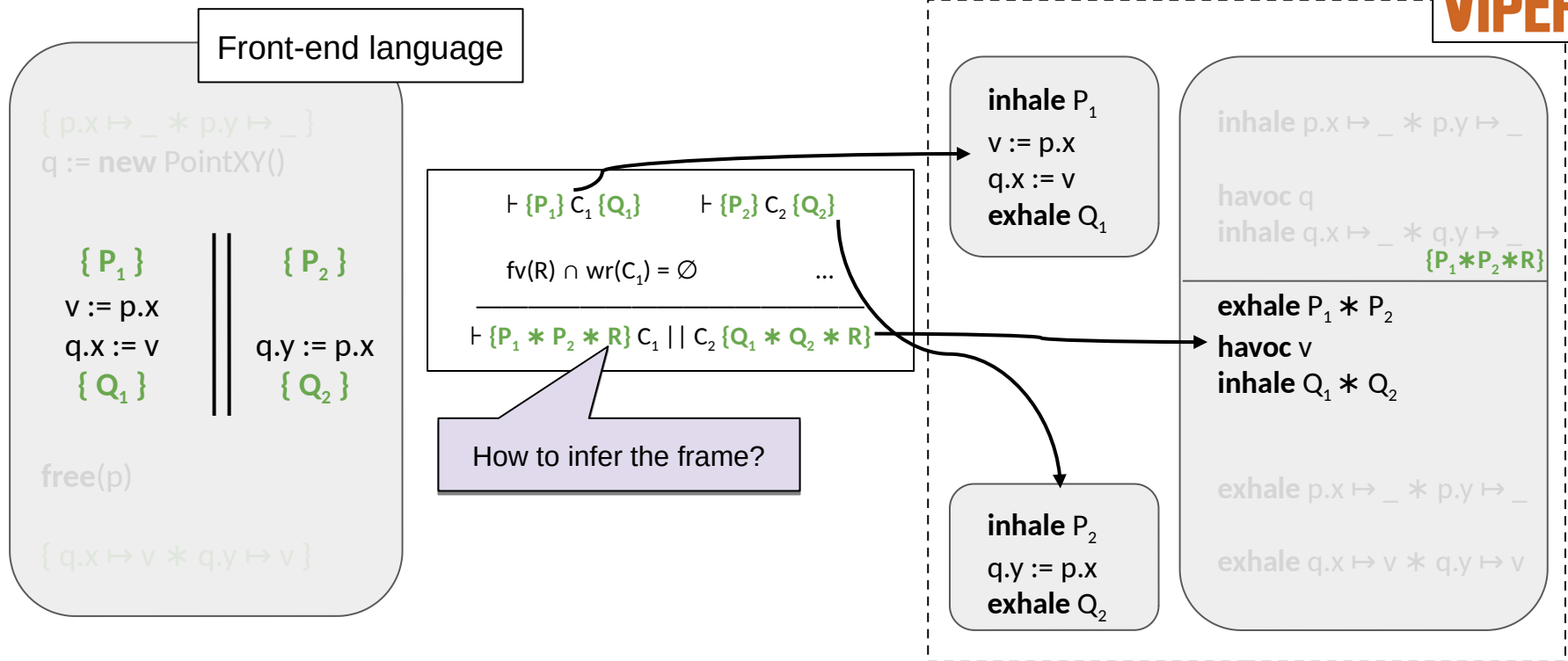
inhale P_2
 $q.y := p.x$
exhale Q_2

```
inhale p.x ↦ _ * p.y ↦ _
havoc q
inhale q.x ↦ _ * q.y ↦ _
...
...
...
exhale p.x ↦ _ * p.y ↦ _
exhale q.x ↦ v * q.y ↦ v
```

Example: Verifying a Parallel Composition (2/2)



Example: Verifying a Parallel Composition (2/2)



Example: Verifying a Parallel Composition (2/2)



Front-end language

```

{ p.x ↦ _ * p.y ↦ _ }
q := new PointXY()

{ P1 }      ||      { P2 }
v := p.x    ||      q.y := p.x
q.x := v    ||      { Q2 }

free(p)

{ q.x ↦ v * q.y ↦ v }
    
```

$$\begin{array}{c}
 \vdash \{P_1\} C_1 \{Q_1\} \quad \vdash \{P_2\} C_2 \{Q_2\} \\
 \text{fv}(R) \cap \text{wr}(C_1) = \emptyset \quad \dots \\
 \hline
 \vdash \{P_1 * P_2 * R\} C_1 || C_2 \{Q_1 * Q_2 * R\}
 \end{array}$$

How to infer the frame?

```

inhale P1
v := p.x
q.x := v
exhale Q1
    
```

```

inhale P2
q.y := p.x
exhale Q2
    
```

```

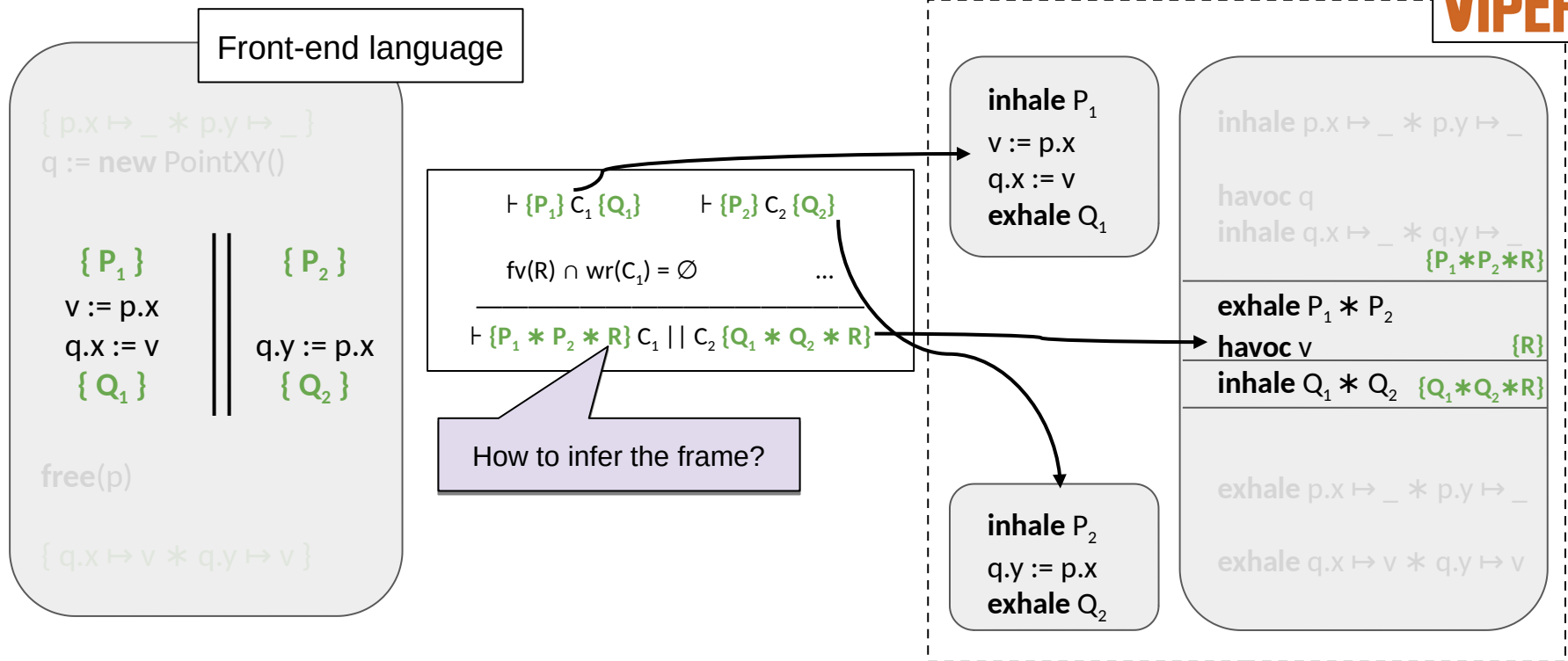
inhale p.x ↦ _ * p.y ↦ _

havoc q
inhale q.x ↦ _ * q.y ↦ _
{ P1 * P2 * R }

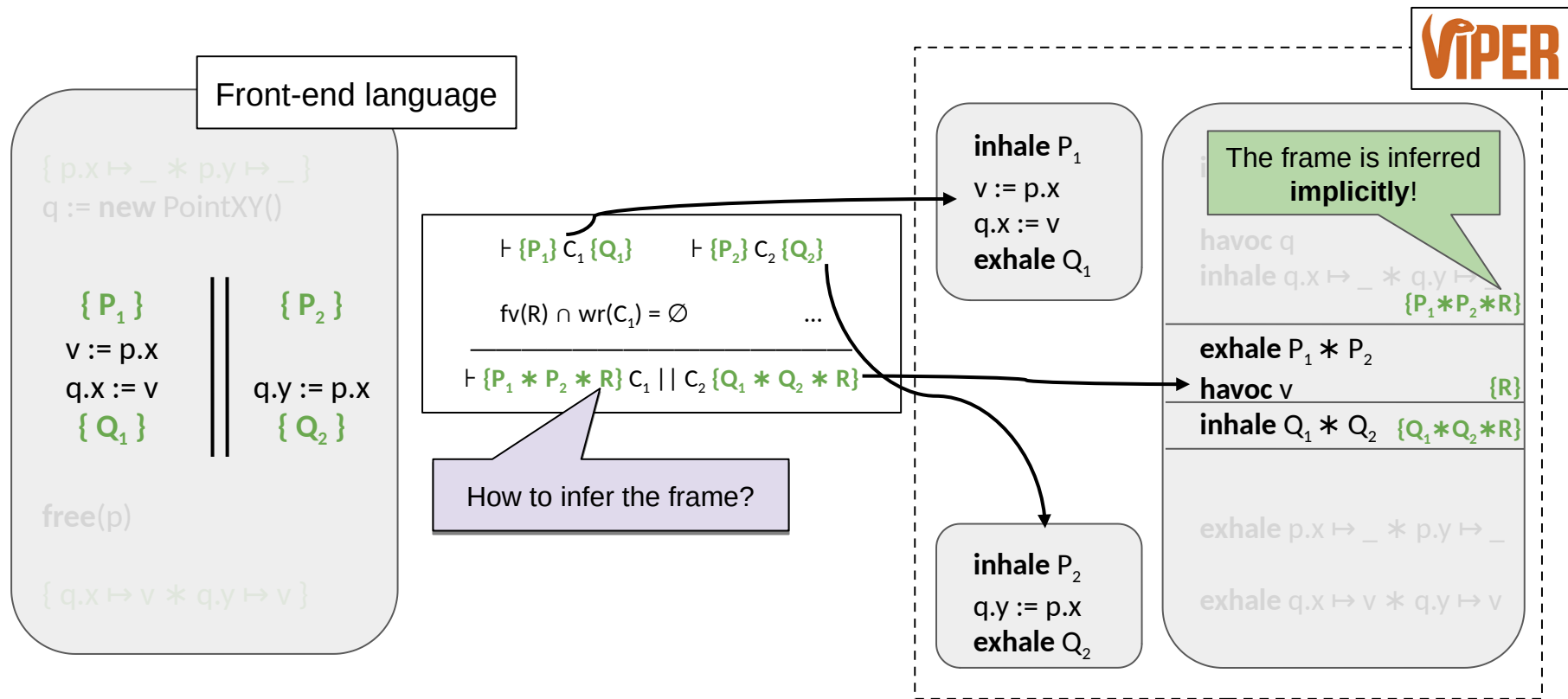
exhale P1 * P2
havoc v
inhale Q1 * Q2
{ R }

exhale p.x ↦ _ * p.y ↦ _
exhale q.x ↦ v * q.y ↦ v
    
```

Example: Verifying a Parallel Composition (2/2)



Example: Verifying a Parallel Composition (2/2)



Outline of the Talk

1. Overview of Viper
2. Inhale and Exhale: An Operational View of Separation Logic
- 3. Designed for Automation**
4. Toward a Foundational Viper

Automating Separation Logic: Challenges

Automating Separation Logic: Challenges

Challenge 1

Existentials

Automating Separation Logic: Challenges

Challenge 1

Existentials

Challenge 2

Recursive predicates

Automating Separation Logic: Challenges

Challenge 1

Existentials

Challenge 2

Recursive predicates

Challenge 3

Magic wands

Automating Separation Logic: Challenges

Challenge 1

Existentials

Challenge 2

Recursive predicates

Challenge 3

Magic wands

Which resources to remove
when exhaling $A \multimap B$?

Automating Separation Logic: Challenges

Challenge 1

Existentials

Challenge 2

Recursive predicates

Challenge 3

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Which resources to remove
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Challenge 4

Iterated separating conjunction

Automating Separation Logic: Challenges

Challenge 1

Existentials

Challenge 2

Recursive predicates

Challenge 3

Magic wands

Which resources to remove
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Challenge 4

Iterated separating conjunction

...

Automating Separation Logic: Challenges

Challenge 1

Existentials

Challenge 2

Recursive predicates

Challenge 3

Magic wands

Which resources to remove
when exhaling $A \multimap B$?

Challenge 4

Iterated separating conjunction

...

Challenge 1: Existentials

Challenge 1: Existentials

exhale $\exists v. (p.x \stackrel{1/2}{\mapsto} v * v > 0)$

Challenge 1: Existentials

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

Challenge 1: Existentials

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

Sequence of elements

Challenge 1: Existentials

Output parameters

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

Sequence of elements

Challenge 1: Existentials

Output parameters

exhale $\exists v. (p.x \mapsto v \text{ * } v > 0)$

exhale $\exists s. \text{list}(l, s) \text{ * } |s| > 0$

exhale $\exists p. p.x \mapsto _ \text{ * } p.y \mapsto _$

Challenge 1: Existentials

Output parameters

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Challenge 1: Existentials

Output parameters

exhale $\exists v. (p.x \mapsto v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

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exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

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exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Challenge 1: Existentials

- Avoid existentials in the SMT encoding

Output parameters

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Challenge 1: Existentials

- ☐ Avoid existentials in the SMT encoding
- ☐ Avoid backtracking

Output parameters

exhale $\exists v. (p.x \mapsto v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

Input parameters

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Challenge 1: Existentials

- ☐ Avoid existentials in the SMT encoding
- ☐ Avoid backtracking
- ☐ Predictable automation

Output parameters

exhale $\exists v. (p.x \mapsto v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

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exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Forbidden by Viper's syntax

Challenge 1: Existentials

- ☐ Avoid existentials in the SMT encoding
- ☐ Avoid backtracking
- ☐ Predictable automation

Output parameters

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Forbidden by Viper's syntax

Viper uses
implicit dynamic frames

Challenge 1: Existentials

- ☐ Avoid existentials in the SMT encoding
- ☐ Avoid backtracking
- ☐ Predictable automation

Output parameters

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

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exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

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Forbidden by Viper's syntax

Viper uses
implicit dynamic frames

$\approx$ SL with **heap-dependent**
expressions and functions

Challenge 1: Existentials

- Avoid existentials in the SMT encoding
- Avoid backtracking
- Predictable automation

Output parameters

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

is written as

exhale $\text{acc}(p.x, 1/2) * p.x > 0$

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

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Challenge 1: Existentials

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exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

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Avoids existential

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

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Challenge 1: Existentials

- Avoid existentials in the SMT encoding
- Avoid backtracking
- Predictable automation

Output parameters

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

is written as

exhale $\text{acc}(p.x, 1/2) * p.x > 0$

is written as

exhale $\text{list}(l) * \text{len}(l) > 0$

Avoids existential

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Forbidden by Viper's syntax

Viper uses
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$\approx$ SL with **heap-dependent**
expressions and functions

Challenge 1: Existentials

- Avoid existentials in the SMT encoding
- Avoid backtracking
- Predictable automation

Output parameters

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

is written as

exhale $\text{acc}(p.x, 1/2) * p.x > 0$

is written as

exhale $\text{list}(l) * \text{len}(l) > 0$

Avoids existential

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Forbidden by Viper's syntax

Heap-dependent function

Viper uses
implicit dynamic frames

$\approx$ SL with **heap-dependent**
expressions and functions

Challenge 1: Existentials

- Avoid existentials in the SMT encoding
- Avoid backtracking
- Predictable automation

Output parameters

exhale $\exists v. (p.x \mapsto v * v > 0)$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

is written as

exhale $\text{acc}(p.x, 1/2) * p.x > 0$

is written as

exhale $\text{list}(l) * \text{len}(l) > 0$

Avoids existential

Heap-dependent function

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Forbidden by Viper's syntax

Viper uses
implicit dynamic frames

$\approx$ SL with **heap-dependent**
expressions and functions

Allows writing code and specifications
in the same language

Challenge 1: Existentials

- Avoid existentials in the SMT encoding
- Avoid backtracking
- Predictable automation

Output parameters

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

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exhale $\text{acc}(p.x, 1/2) * p.x > 0$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

is written as

exhale $\text{list}(l) * \text{len}(l) > 0$

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Forbidden by Viper's syntax

Viper uses
implicit dynamic frames

$\approx$ SL with **heap-dependent**
expressions and functions

Allows writing code and specifications
in the same language

inhale $A * B$

exhale $A * B$

Challenge 1: Existentials

- Avoid existentials in the SMT encoding
- Avoid backtracking
- Predictable automation

Output parameters

exhale $\exists v. (p.x \mapsto^{\frac{1}{2}} v * v > 0)$

is written as

exhale $\text{acc}(p.x, 1/2) * p.x > 0$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

is written as

exhale $\text{list}(l) * \text{len}(l) > 0$

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Forbidden by Viper's syntax

Viper uses
implicit dynamic frames

$\approx$ SL with **heap-dependent**
expressions and functions

Allows writing code and specifications
in the same language

Implicit existential quantification

inhale $A * B$

exhale $A * B$

Challenge 1: Existentials

- Avoid existentials in the SMT encoding
- Avoid backtracking
- Predictable automation

Output parameters

exhale $\exists v. (p.x \mapsto v * v > 0)$

is written as

exhale $\text{acc}(p.x, 1/2) * p.x > 0$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

is written as

exhale $\text{list}(l) * \text{len}(l) > 0$

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Forbidden by Viper's syntax

Viper uses
implicit dynamic frames

$\approx$ SL with **heap-dependent**
expressions and functions

Allows writing code and specifications
in the same language

Implicit existential quantification

operationally equivalent to

inhale $A * B$
exhale $A * B$

inhale A ; **inhale** B

Challenge 1: Existentials

- ☐ Avoid existentials in the SMT encoding
- ☐ Avoid backtracking
- ☐ Predictable automation

Output parameters

exhale $\exists v. (p.x \mapsto v * v > 0)$

is written as

exhale $\text{acc}(p.x, 1/2) * p.x > 0$

exhale $\exists s. \text{list}(l, s) * |s| > 0$

is written as

exhale $\text{list}(l) * \text{len}(l) > 0$

Input parameters

exhale $\exists p. p.x \mapsto _ * p.y \mapsto _$

exhale $\exists l. \text{list}(l, s) * l \neq \text{null}$

Forbidden by Viper's syntax

Viper uses
implicit dynamic frames

$\approx$ SL with **heap-dependent**
expressions and functions

Allows writing code and specifications
in the same language

Implicit existential quantification

inhale $A * B$
exhale $A * B$

operationally equivalent to

Analogous for **exhale**

inhale A ; **inhale** B

Viper's Expression and Assertion Language

Viper's Expression and Assertion Language

$e ::= e.x \mid f(e_1, \dots, e_n) \mid \mathbf{old}[l](e) \mid e_1 + e_2 \mid e_1 / e_2 \mid n \mid v \mid b ? e_1 : e_2 \mid \dots$

Viper's Expression and Assertion Language

Field access

$e ::= e.x \mid f(e_1, \dots, e_n) \mid \mathbf{old}[l](e) \mid e_1 + e_2 \mid e_1 / e_2 \mid n \mid v \mid b ? e_1 : e_2 \mid \dots$

Viper's Expression and Assertion Language

Field access

Heap-dependent
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Viper's Expression and Assertion Language

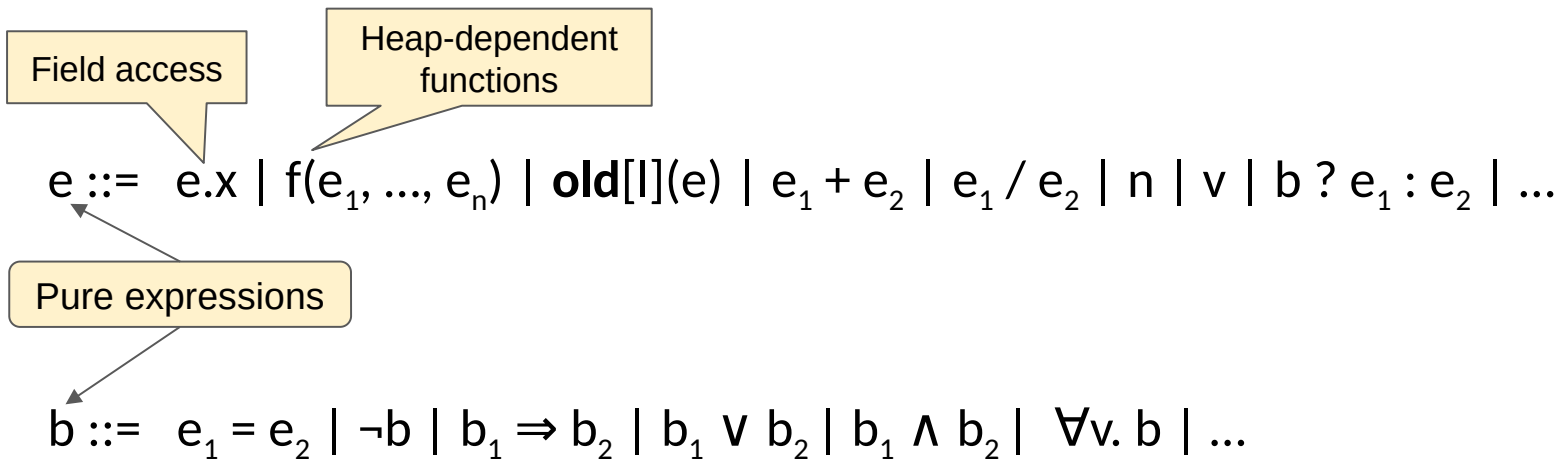
Field access

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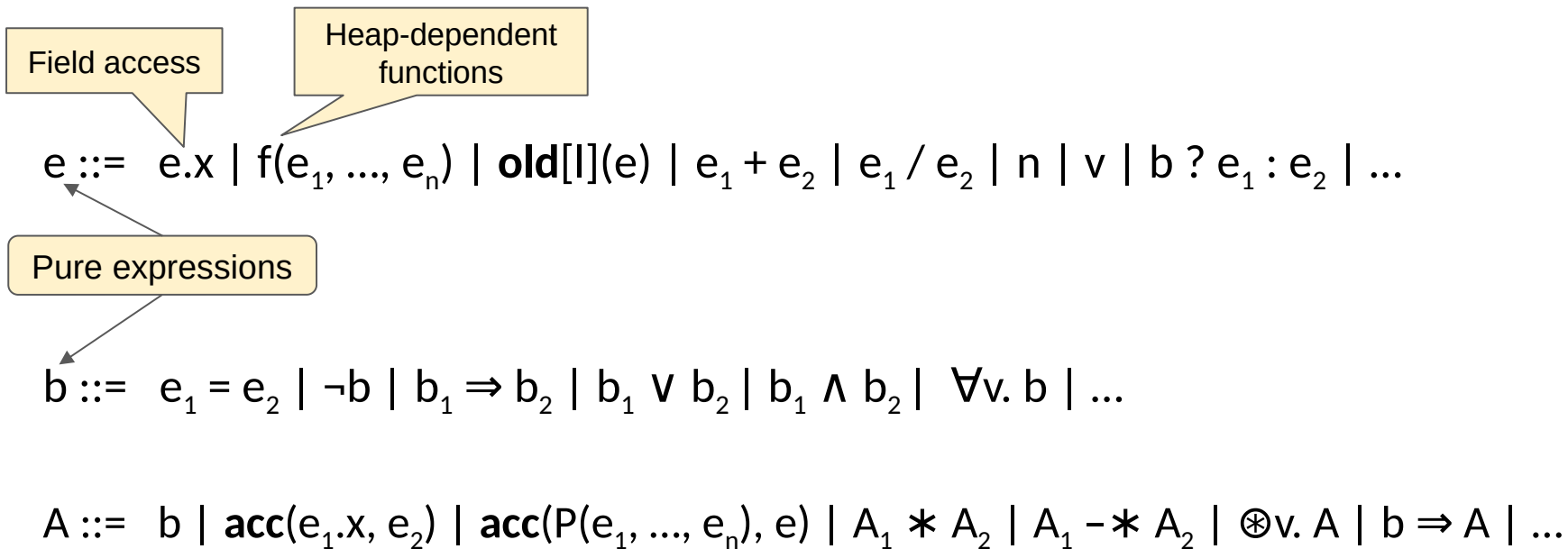
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$b ::= e_1 = e_2 \mid \neg b \mid b_1 \Rightarrow b_2 \mid b_1 \vee b_2 \mid b_1 \wedge b_2 \mid \forall v. b \mid \dots$

Viper's Expression and Assertion Language



Viper's Expression and Assertion Language



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Pure expressions

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Fractional permissions
for heap locations

Viper's Expression and Assertion Language

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Fractional permissions
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Inductive predicates
with fractional permissions

Viper's Expression and Assertion Language

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Fractional permissions
for heap locations

Inductive predicates
with fractional permissions

Iterated separating conjunction

Viper's Expression and Assertion Language

Design choice

- No impure existential
- No impure disjunction
- No impure implication
- No impure negation
- No impure logical conjunction

Field access

Heap-dependent
functions

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Fractional permissions
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Fractional permissions
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Inductive predicates
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Iterated separating conjunction

Challenge 2: Inductive Predicates

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$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

Challenge 2: Inductive Predicates

Input parameters only

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

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1. Existence of a (least) fixed-point?

Challenge 2: Inductive Predicates

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2. How to automate **inhale** list(l) and **exhale** list(l)?
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4. How to know when to **unfold** the definition?

Challenge 2: Inductive Predicates

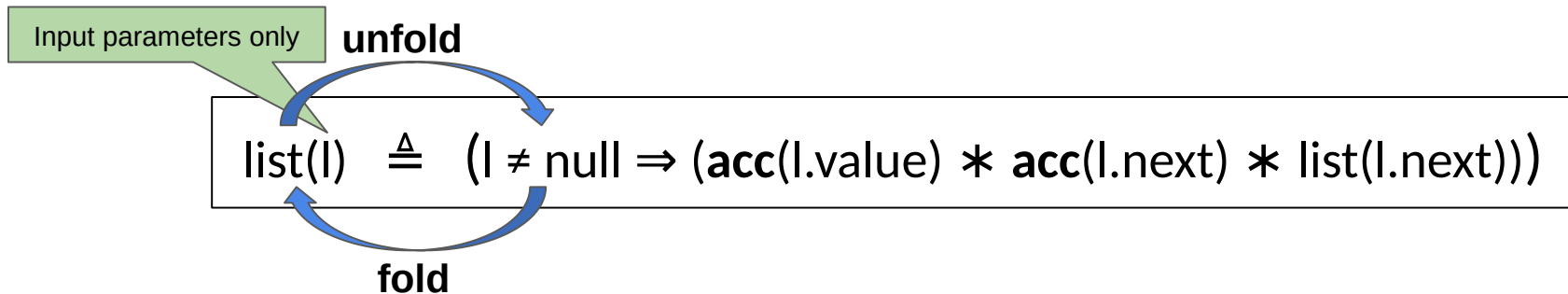
Input parameters only

unfold


$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

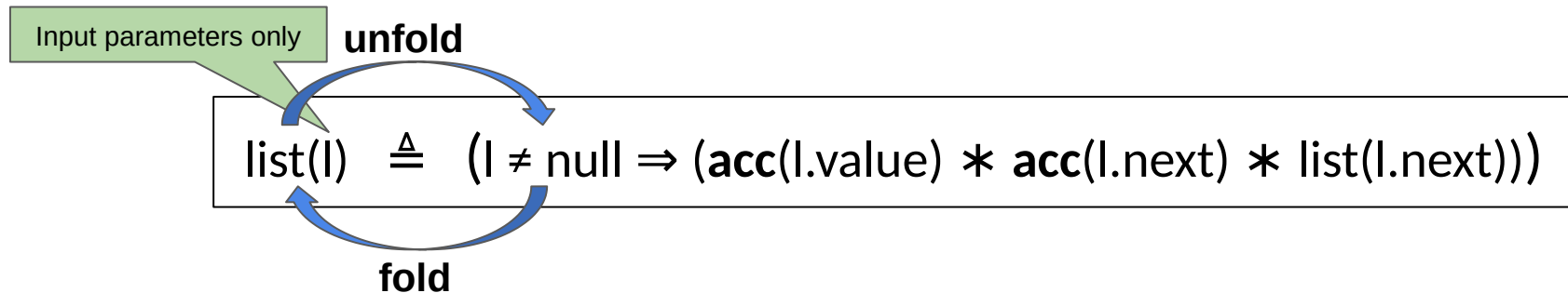
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Challenge 2: Inductive Predicates



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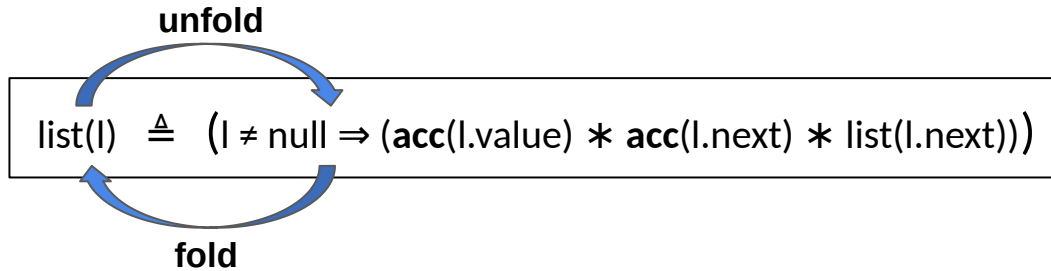
Challenge 2: Inductive Predicates



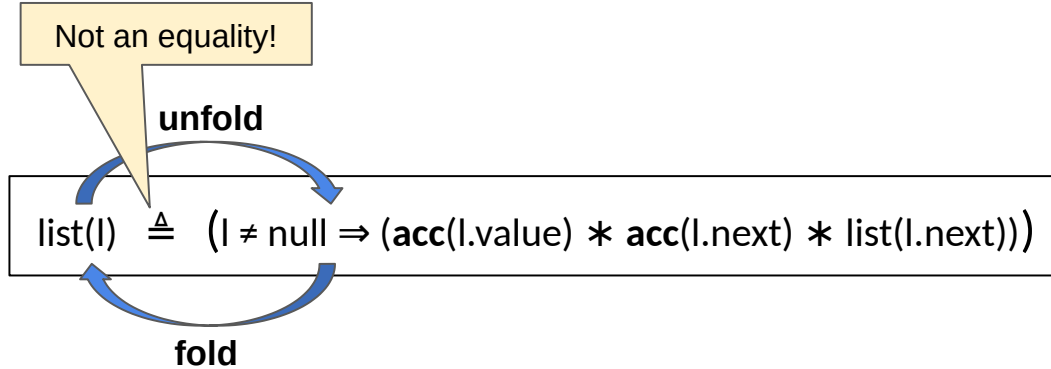
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Viper's approach: Treat predicates **isorecursively**

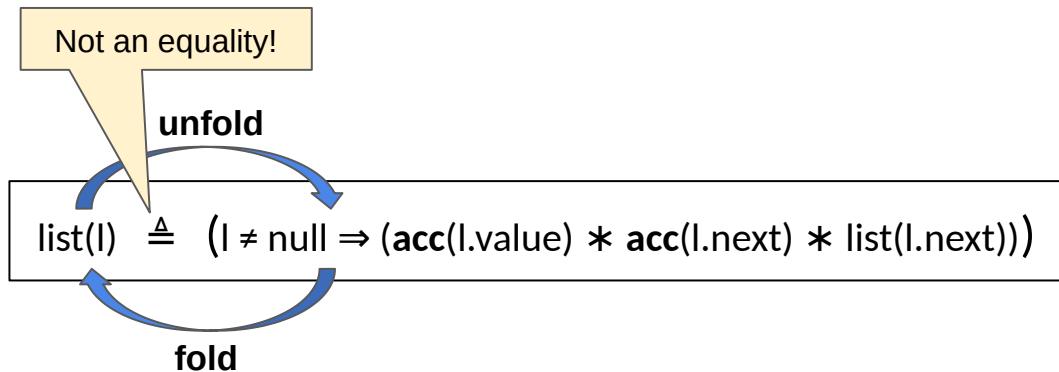
Isorecursive Predicates



Isorecursive Predicates

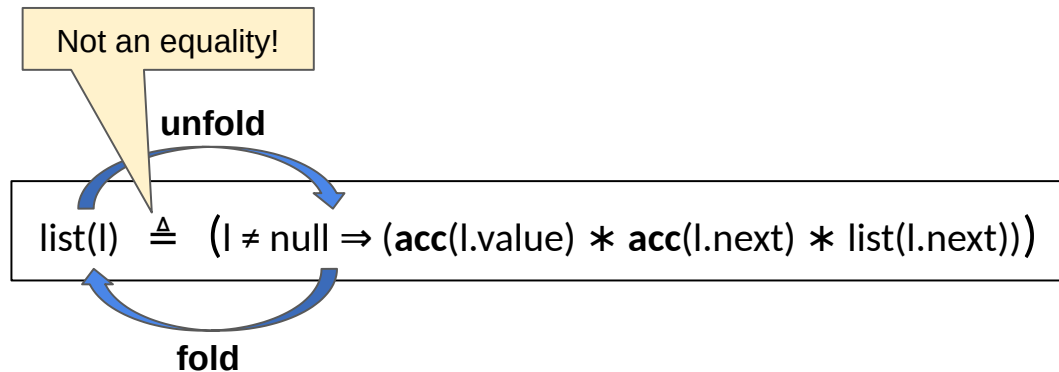


Isorecursive Predicates



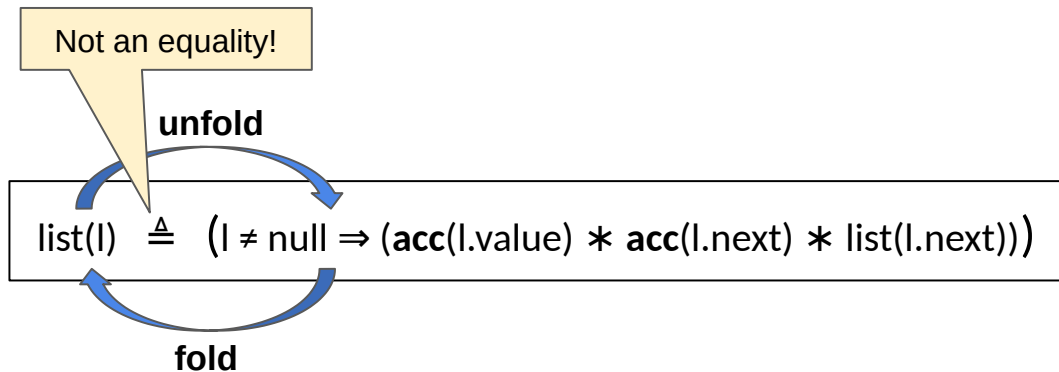
(simplified) Viper's state model: $(\text{Loc} \rightarrow (0, 1] \times \text{Val})$

Isorecursive Predicates



(simplified) Viper's state model: $(\text{Loc} \rightarrow (0, 1] \times \text{Val}) \times (\text{PredLoc} \rightarrow [0, +\infty))$

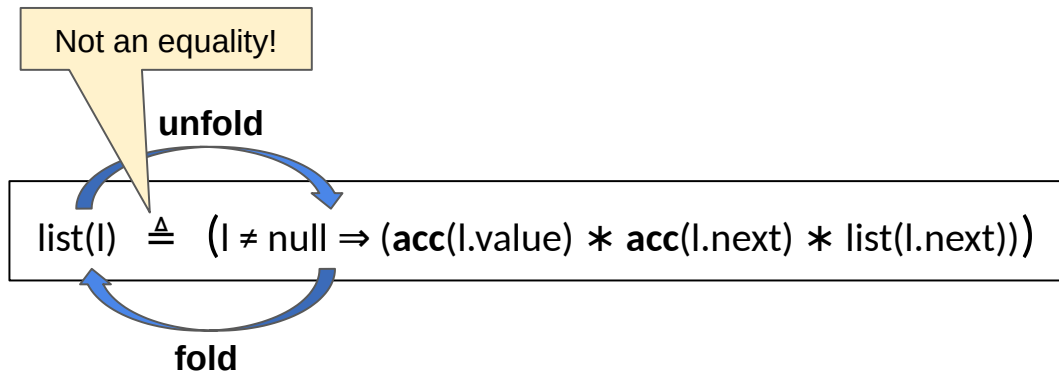
Isorecursive Predicates



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Predicate mask

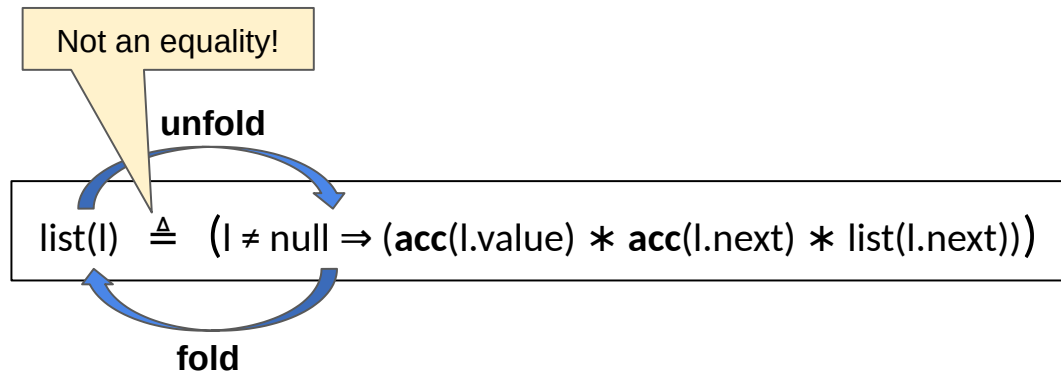
Isorecursive Predicates



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Predicate mask

Isorecursive Predicates



Acts on the predicate mask

VIPER

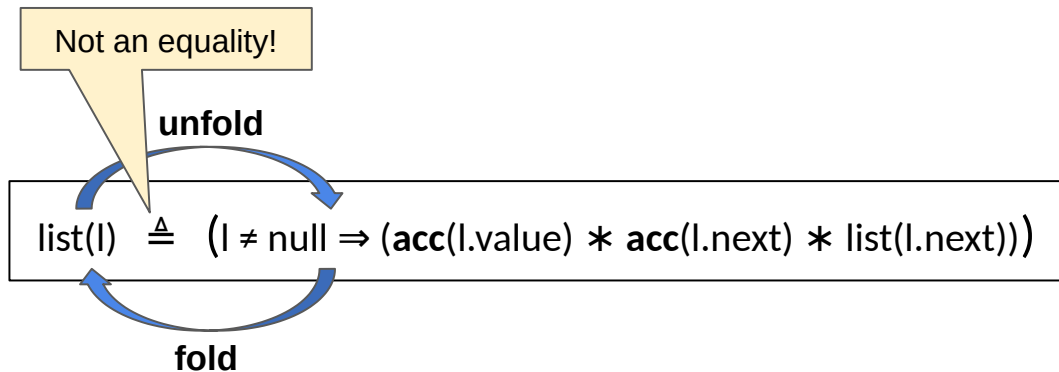
inhale list(l)

exhale list(l)

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Predicate mask

Isorecursive Predicates



Acts on the predicate mask



```
inhale list(l)
if (l != null) {

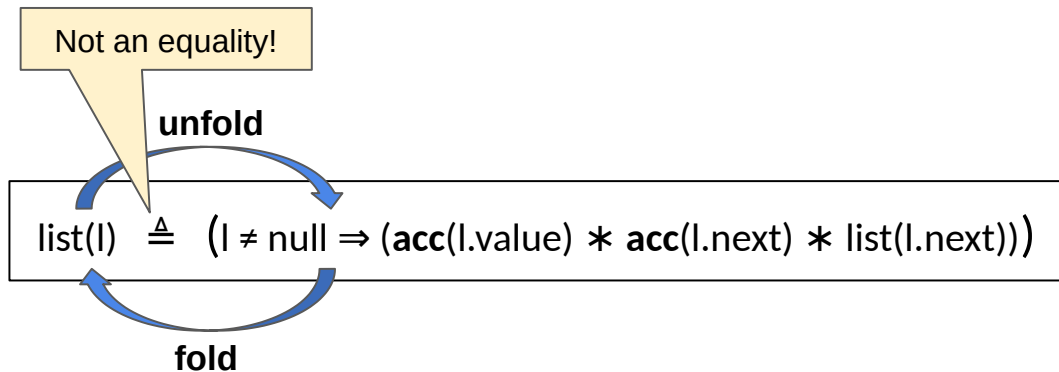
    l.value := l.value + 1

}
exhale list(l)
```

(simplified) Viper's state model: $(\text{Loc} \rightarrow (0, 1] \times \text{Val}) \times (\text{PredLoc} \rightarrow [0, +\infty))$

Predicate mask

Isorecursive Predicates



Acts on the predicate mask

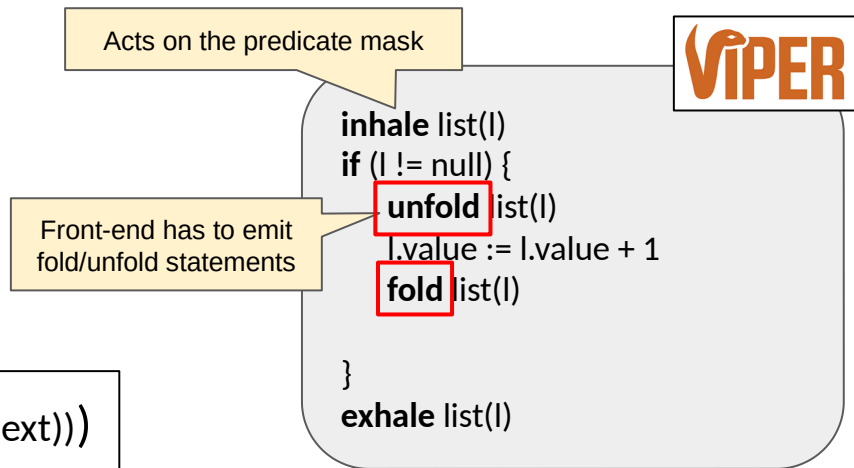
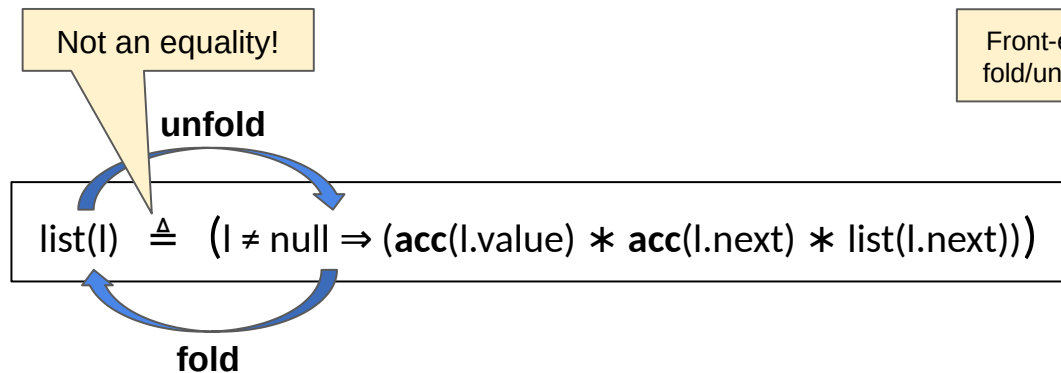
VIPER

```
inhale list(l)
if (l != null) {
  unfold list(l)
  l.value := l.value + 1
  fold list(l)
}
exhale list(l)
```

(simplified) Viper's state model: $(\text{Loc} \rightarrow (0, 1] \times \text{Val}) \times (\text{PredLoc} \rightarrow [0, +\infty))$

Predicate mask

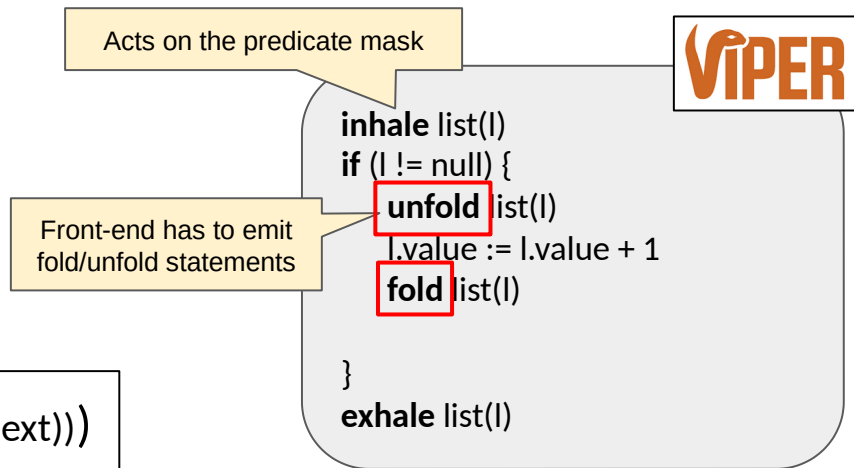
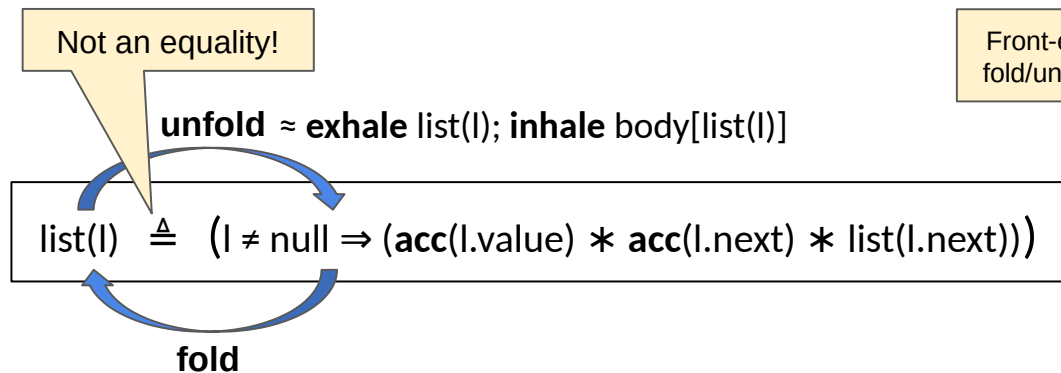
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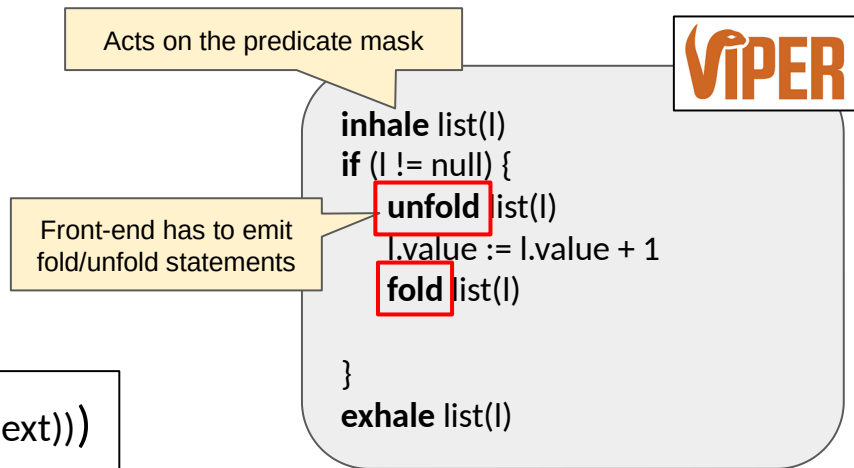
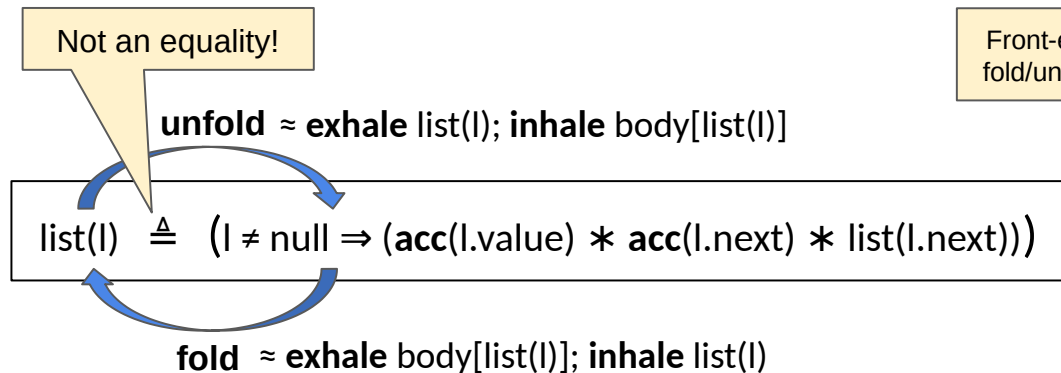
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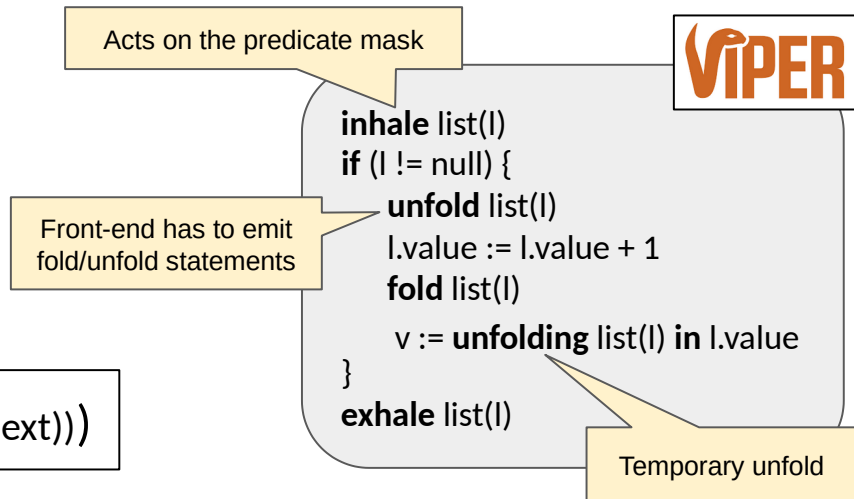
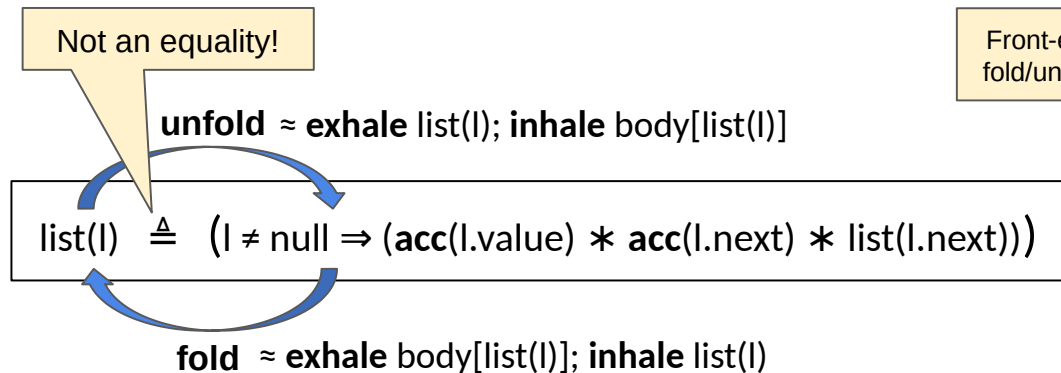
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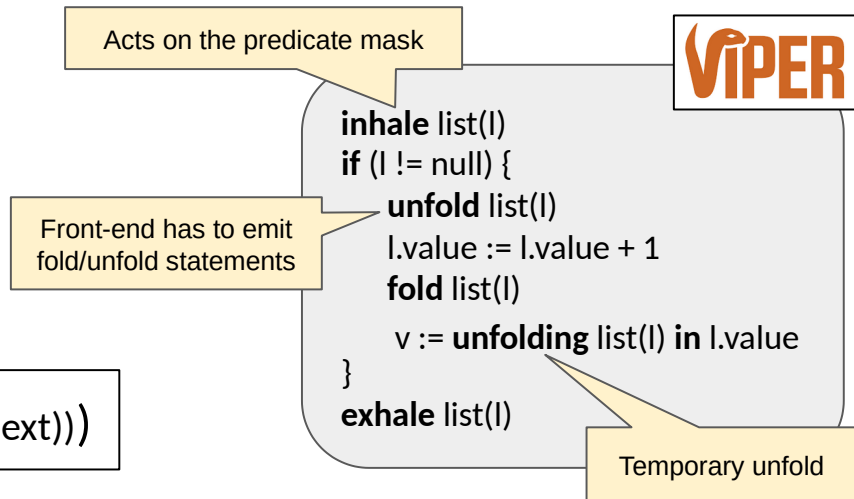
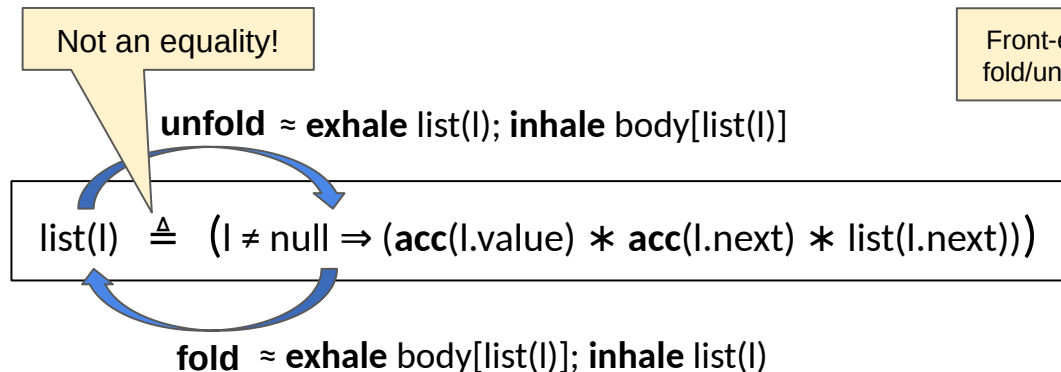
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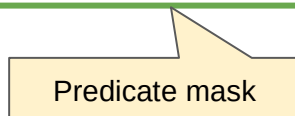
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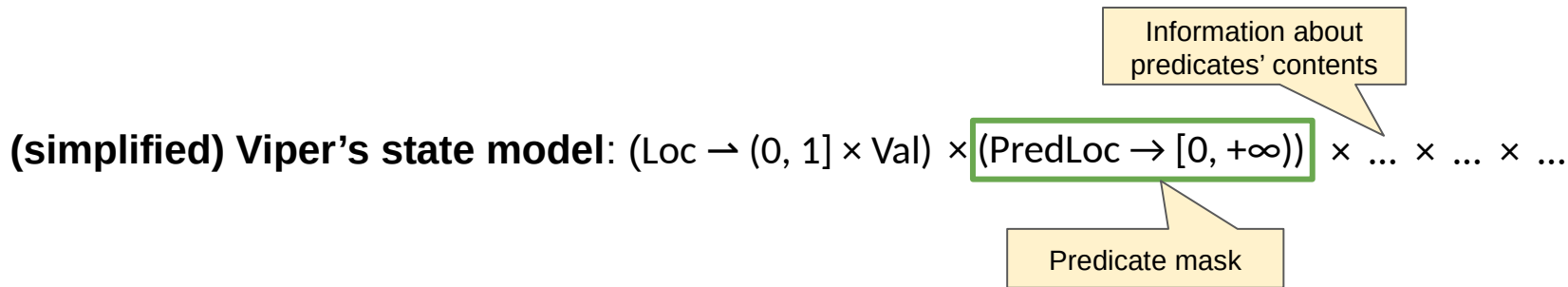
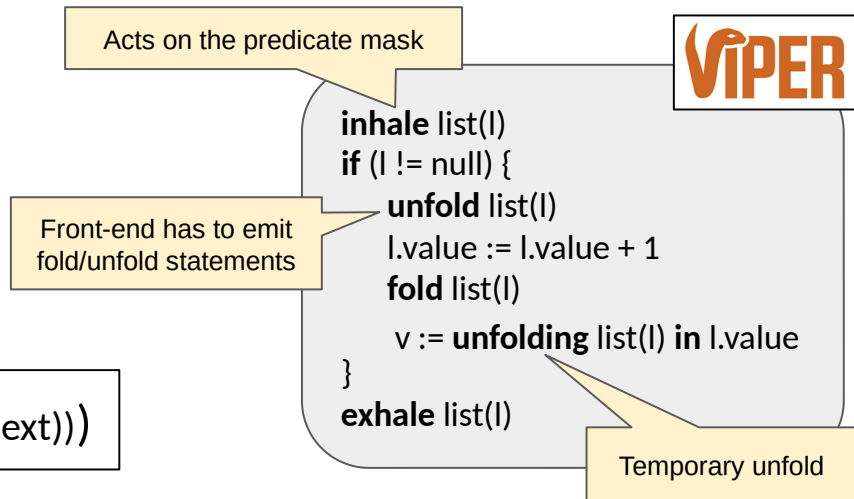
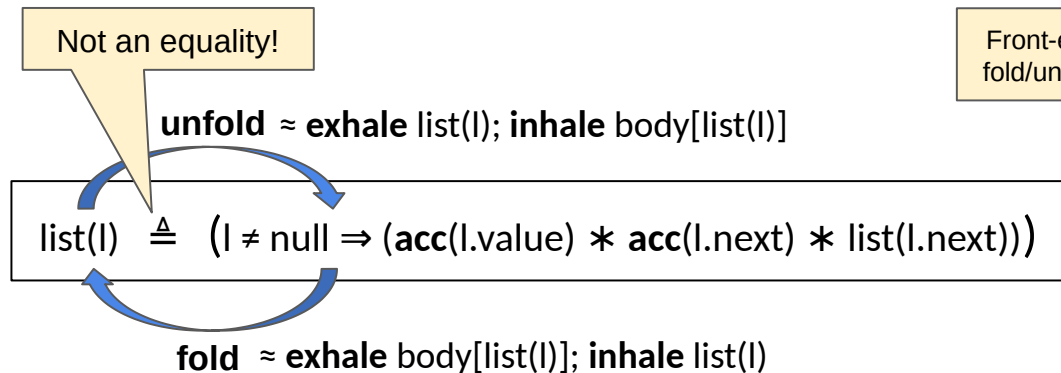
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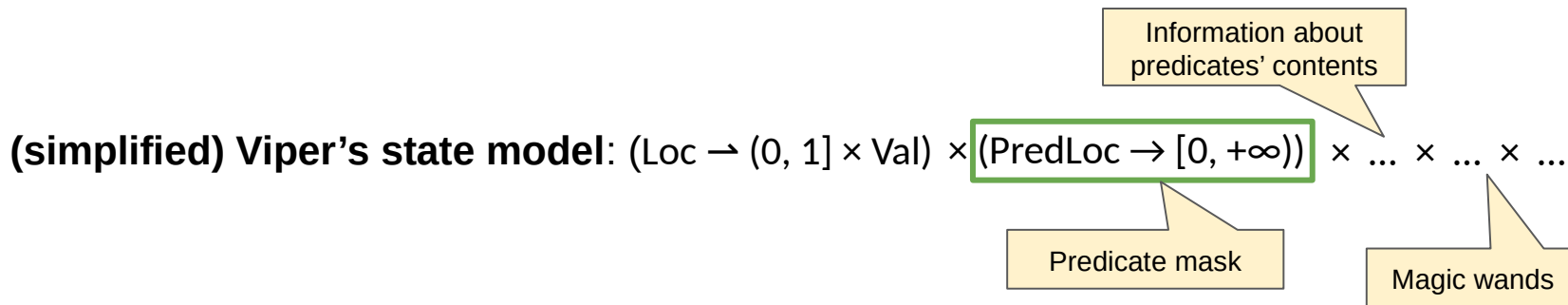
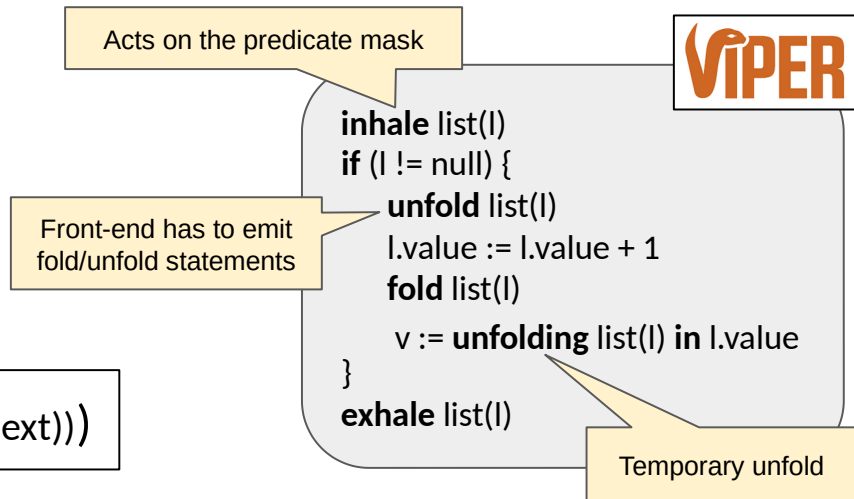
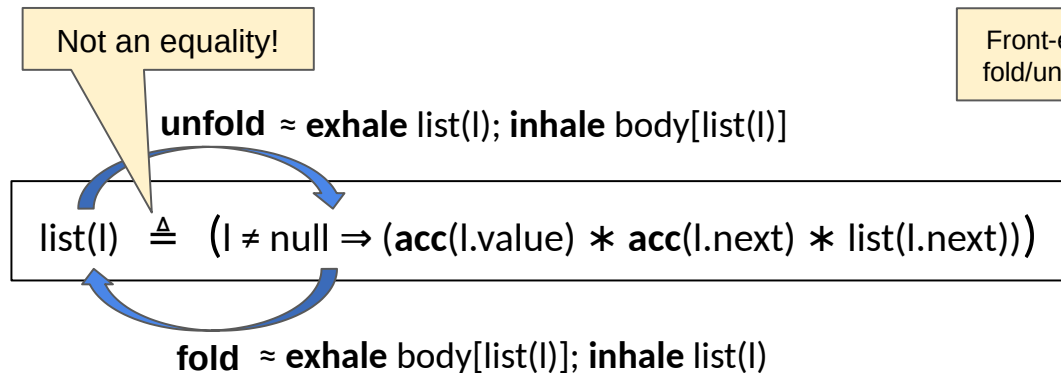
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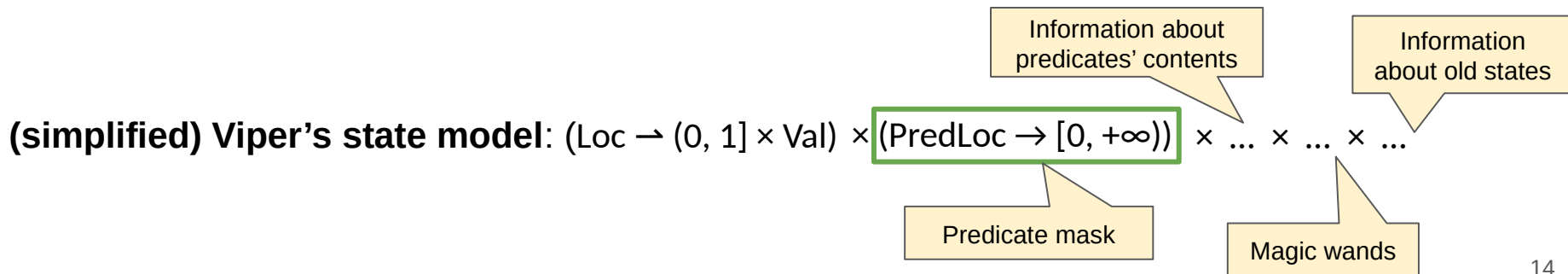
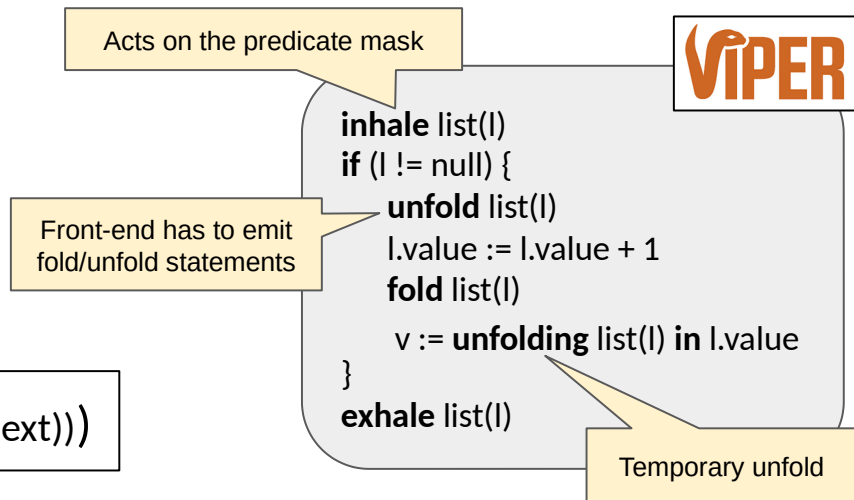
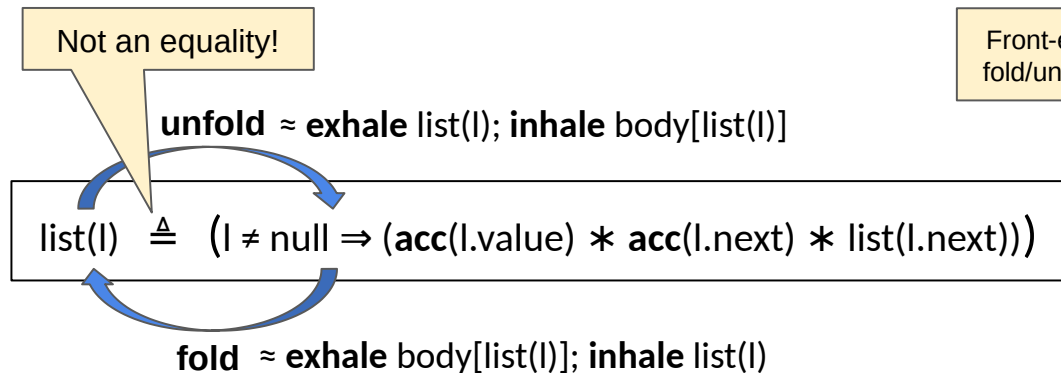
Isorecursive Predicates



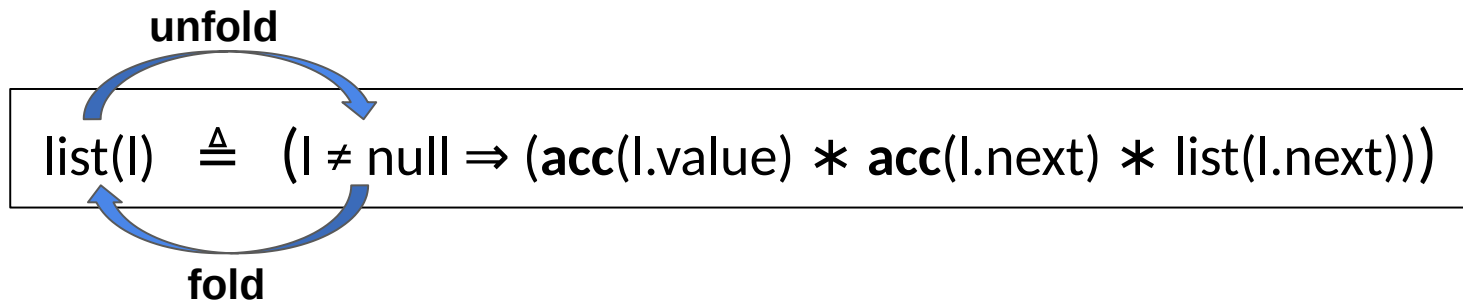
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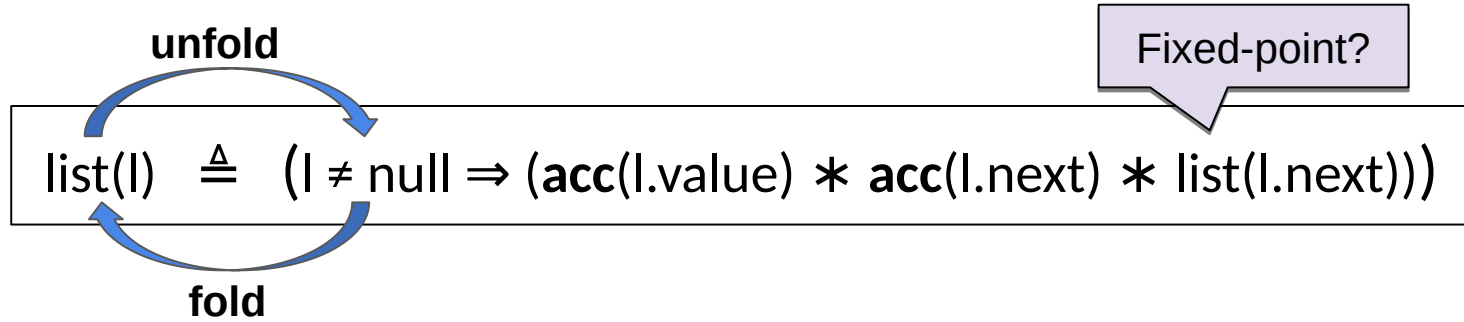
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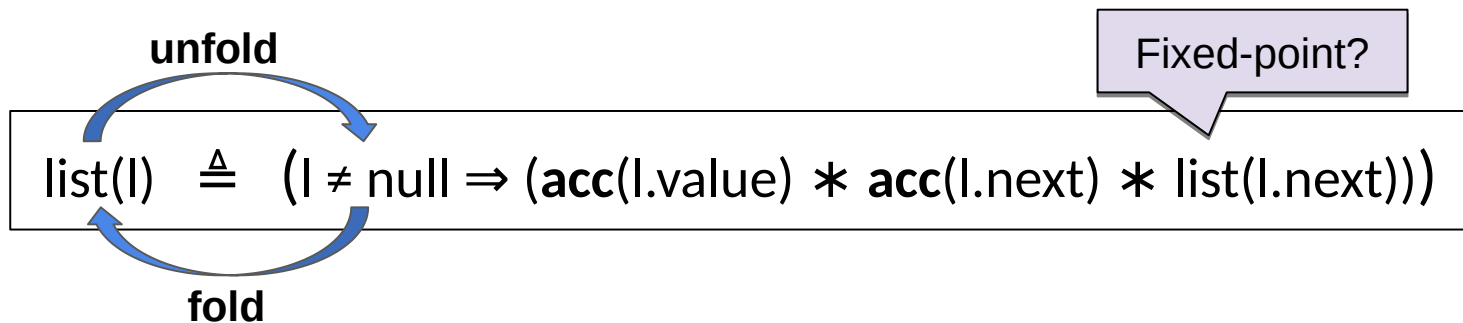
Existence of a Fixed-Point



Existence of a Fixed-Point

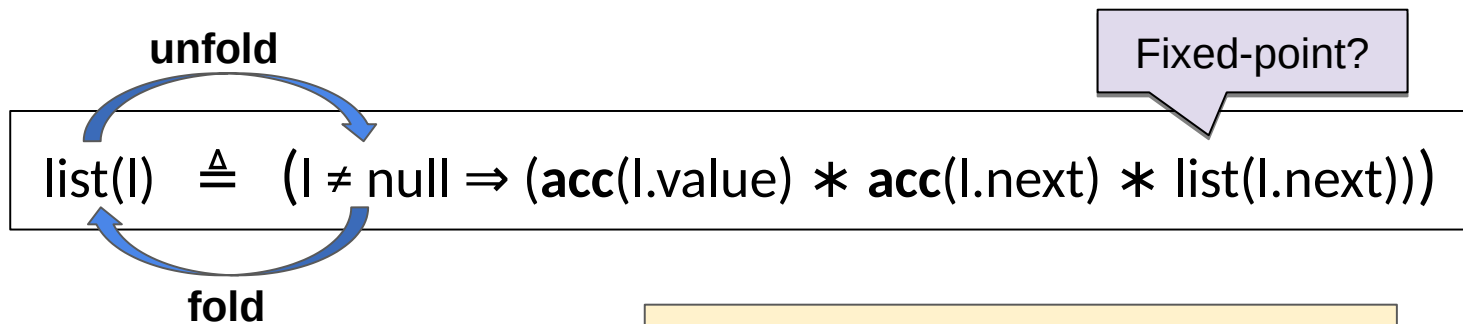


Existence of a Fixed-Point



$A ::= b \mid \text{acc}(e_1.x, e_2) \mid \text{acc}(P(e_1, \dots, e_n), e) \mid A_1 * A_2 \mid A_1 -* A_2 \mid \otimes v. A \mid b \Rightarrow A \mid \dots$

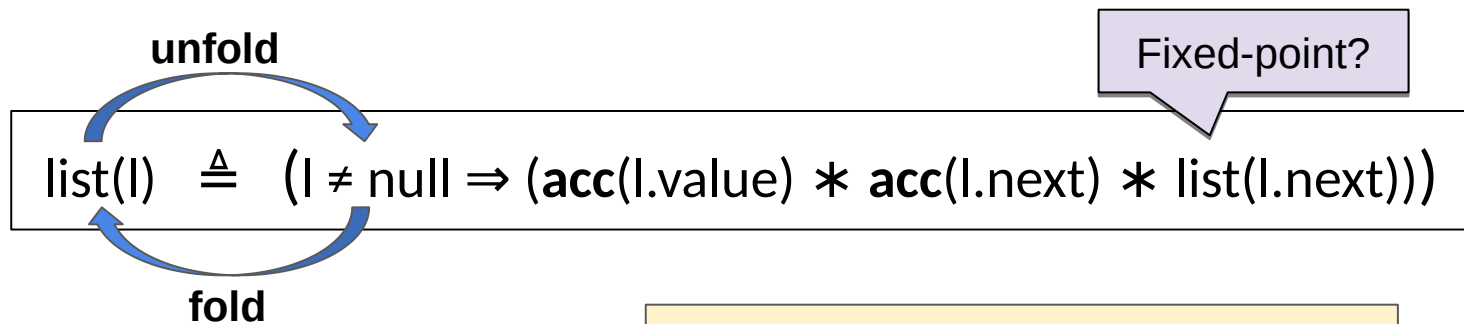
Existence of a Fixed-Point



Magic wands are not allowed in recursive definitions

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Existence of a Fixed-Point

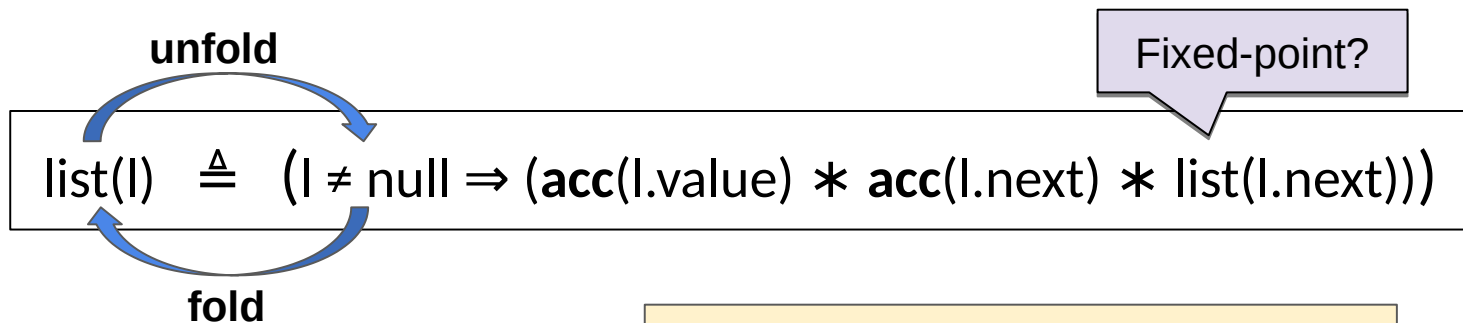


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Scott-continuity

Existence of a Fixed-Point



Fixed-point?

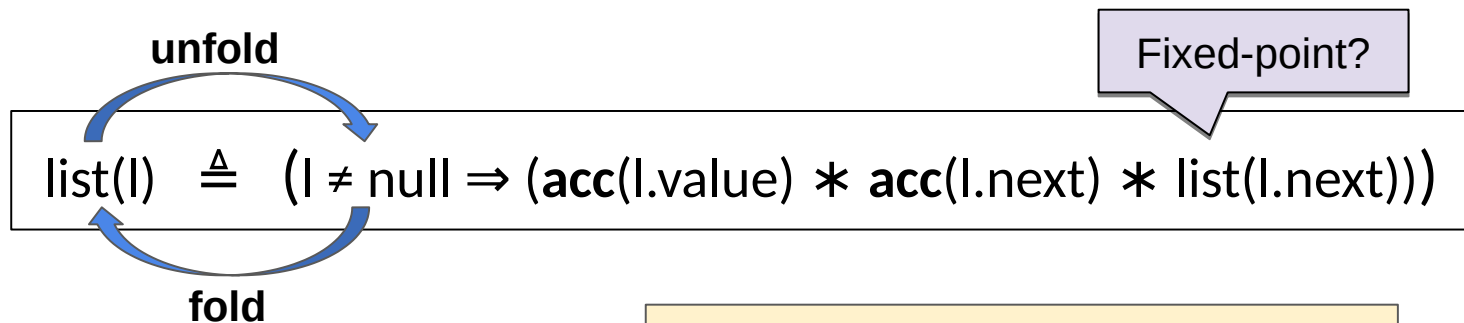
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Scott-continuity

Existence of a least fixed point

Existence of a Fixed-Point



Magic wands are not allowed in recursive definitions

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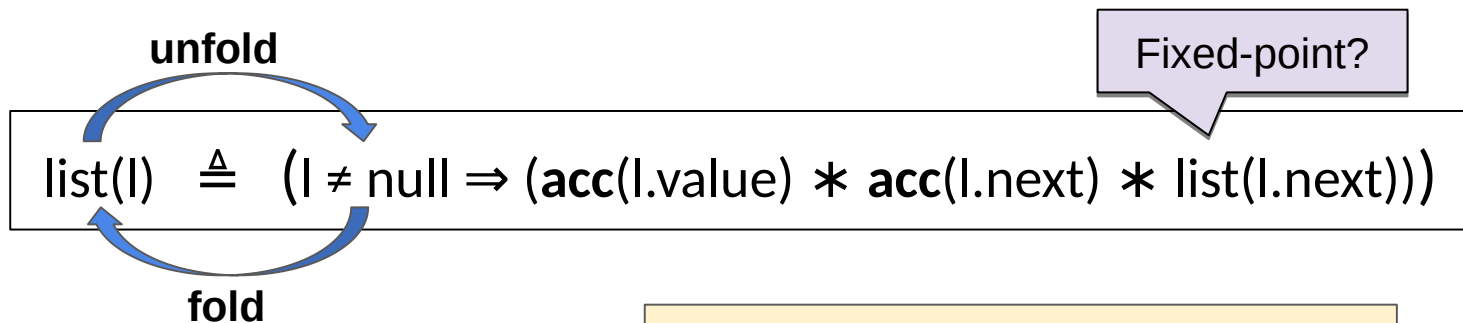
Scott-continuity

Existence of a least fixed point

Kleene's theorem

Any given predicate instance has a **finite** number of predicate instances folded within it

Existence of a Fixed-Point



Fixed-point?

Magic wands are not allowed in recursive definitions

$A ::= b \mid \text{acc}(e_1.x, e_2) \mid \text{acc}(P(e_1, \dots, e_n), e) \mid A_1 * A_2 \mid A_1 - * A_2 \mid \otimes v. A \mid b \Rightarrow A \mid \dots$

Scott-continuity

Kleene's theorem

Existence of a least fixed point

Can be used as a termination measure
(e.g., for heap-dependent functions)

Any given predicate instance has a **finite** number of predicate instances folded within it

Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

```
function len(l): Int  
  requires list(l)
```

```
{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }
```



Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

function `len(l): Int`

requires `list(l)`

`{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }`

VIPER

Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

function `len(l): Int`

requires `list(l)`

ensures `result >= 0`

`{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }`



Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

function `len(l): Int`

requires `list(l)`

ensures `result >= 0`

`{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }`

Automatically proven
by induction

VIPER

Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

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function `len(l): Int`

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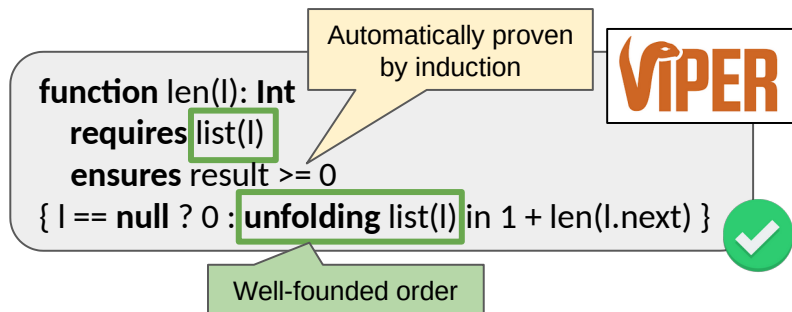
`{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }`

Automatically proven
by induction

VIPER

Well-founded order

Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$


Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

function `len(l): Int`

requires `list(l)`

ensures `result >= 0`

`{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }`

Automatically proven
by induction

VIPER

Well-founded order



function `sum(l): Int`

requires `list(l)`

`{ l == null ? 0 : unfolding list(l) in l.value + sum(l.next) }`

VIPER



Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

function `len(l): Int`

requires `list(l)`

ensures `result >= 0`

`{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }`

Automatically proven
by induction

VIPER

Well-founded order



How deep should the
definition be unfolded?

function `sum(l): Int`

requires `list(l)`

`{ l == null ? 0 : unfolding list(l) in l.value + sum(l.next) }`

VIPER



Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

function `len(l): Int`

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ensures `result >= 0`

`{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }`

Automatically proven
by induction

VIPER



Well-founded order

How deep should the
definition be unfolded?

function `sum(l): Int`

requires `list(l)`

`{ l == null ? 0 : unfolding list(l) in l.value + sum(l.next) }`

VIPER



method `main(l: Ref)`

requires `list(l) * len(l) >= 2`

ensures `list(l) * sum(l) == old(sum(l)) + 5`

`{`

`l.next.value := l.next.value + 5`

`}`

VIPER

Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

function len(l): Int

requires list(l)

ensures result >= 0

{ l == null ? 0 : **unfolding** list(l) in 1 + len(l.next) }

Automatically proven
by induction

VIPER



Well-founded order

How deep should the
definition be unfolded?

function sum(l): Int

requires list(l)

{ l == null ? 0 : **unfolding** list(l) in l.value + sum(l.next) }

VIPER



method main(l: Ref)

requires list(l) * len(l) >= 2

ensures list(l) * sum(l) == old(sum(l)) + 5

{

unfold list(l)

unfold list(l.next)

l.next.value := l.next.value + 5

fold list(l.next)

fold list(l)

}

VIPER

Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

function `len(l): Int`

requires `list(l)`

ensures `result >= 0`

`{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }`

Automatically proven
by induction

VIPER



Well-founded order

method `main(l: Ref)`

requires `list(l) * len(l) >= 2`

ensures `list(l) * sum(l) == old(sum(l)) + 5`

`{`

unfold `list(l)`

unfold `list(l.next)`

`l.next.value := l.next.value + 5`

fold `list(l.next)`

fold `list(l)`

`}`

VIPER

function `sum(l): Int`

requires `list(l)`

`{ l == null ? 0 : unfolding list(l) in l.value + sum(l.next) }`

How deep should the
definition be unfolded?

VIPER



`sum(l) = l.value + sum(l.next)`

Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

function `len(l): Int`

requires `list(l)`

ensures `result >= 0`

`{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }`

Automatically proven
by induction

VIPER



Well-founded order

How deep should the
definition be unfolded?

function `sum(l): Int`

requires `list(l)`

`{ l == null ? 0 : unfolding list(l) in l.value + sum(l.next) }`

VIPER



method `main(l: Ref)`

requires `list(l) * len(l) >= 2`

ensures `list(l) * sum(l) == old(sum(l)) + 5`

`{`

unfold `list(l)`

unfold `list(l.next)`

`l.next.value := l.next.value + 5`

fold `list(l.next)`

fold `list(l)`

`}`

VIPER

`sum(l) = l.value + sum(l.next)`

`sum(l) = l.value + l.next.value + sum(l.next.next)`

Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

function `len(l): Int`

requires `list(l)`

ensures `result >= 0`

`{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }`

Automatically proven
by induction

VIPER



Well-founded order

How deep should the
definition be unfolded?

function `sum(l): Int`

requires `list(l)`

`{ l == null ? 0 : unfolding list(l) in l.value + sum(l.next) }`

VIPER



method `main(l: Ref)`

requires `list(l) * len(l) >= 2`

ensures `list(l) * sum(l) == old(sum(l)) + 5`

`{`

unfold `list(l)`

unfold `list(l.next)`

`l.next.value := l.next.value + 5`

fold `list(l.next)`

fold `list(l)`

`}`

VIPER

`sum(l) = l.value + sum(l.next)`

`sum(l) = l.value + l.next.value + sum(l.next.next)`

Output parameter of
`list(l.next.next)`

Heap-Dependent Functions

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

function `len(l): Int`

requires `list(l)`

ensures `result >= 0`

`{ l == null ? 0 : unfolding list(l) in 1 + len(l.next) }`

Automatically proven
by induction

VIPER



Well-founded order

method `main(l: Ref)`

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ensures `list(l) * sum(l) == old(sum(l)) + 5`

`{`

unfold `list(l)`

unfold `list(l.next)`

`l.next.value := l.next.value + 5`

fold `list(l.next)`

fold `list(l)`

`}`

VIPER



How deep should the
definition be unfolded?

function `sum(l): Int`

requires `list(l)`

`{ l == null ? 0 : unfolding list(l) in l.value + sum(l.next) }`

VIPER



`sum(l) = l.value + sum(l.next)`

`sum(l) = l.value + l.next.value + sum(l.next.next)`

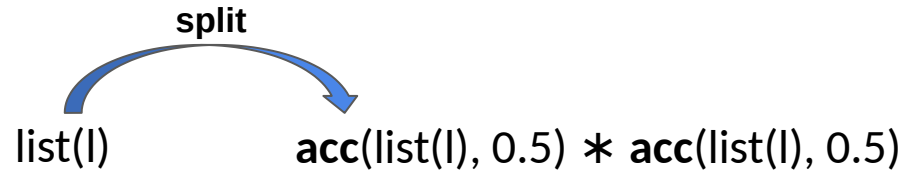
Output parameter of
`list(l.next.next)`

Fractional (Recursive) Predicates

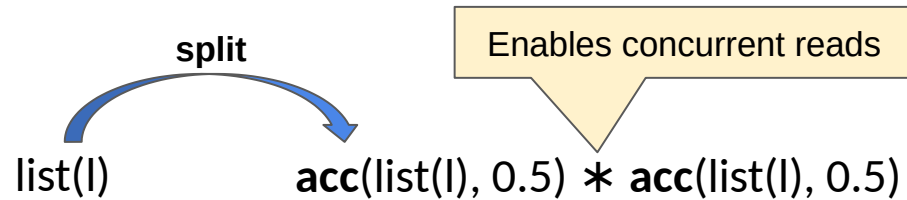
Fractional (Recursive) Predicates

list(l)

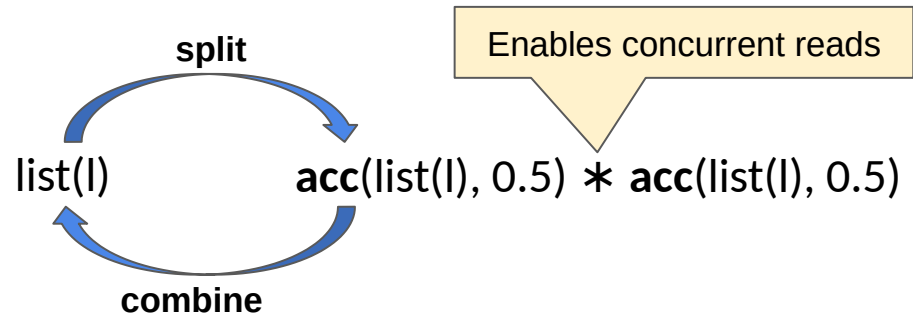
Fractional (Recursive) Predicates



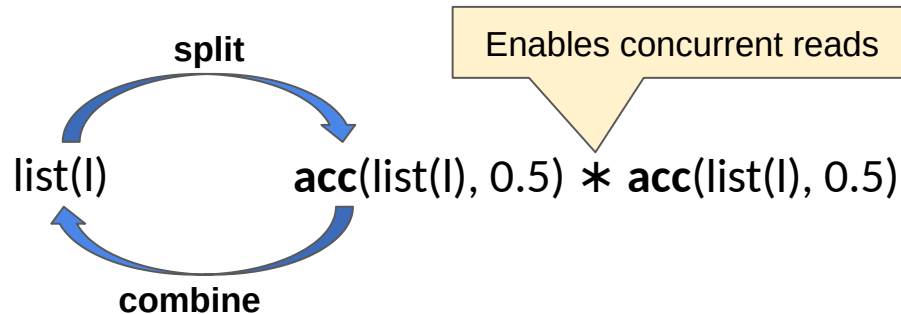
Fractional (Recursive) Predicates



Fractional (Recursive) Predicates



Fractional (Recursive) Predicates



inhale `list(l)`

...

exhale `acc(list(l), 0.5)`

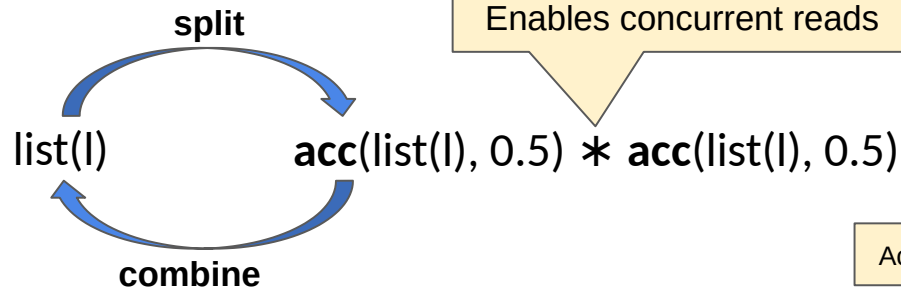
...

inhale `acc(list(l), 0.5)`

...

exhale `list(l)`

Fractional (Recursive) Predicates



Acts on the predicate mask

inhale list(l)

...

exhale acc(list(l), 0.5)

...

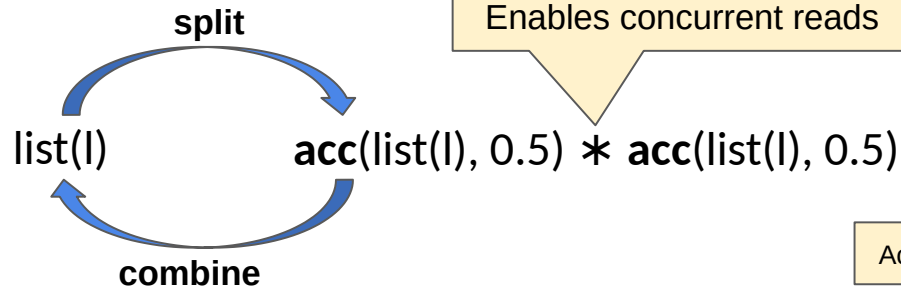
inhale acc(list(l), 0.5)

...

exhale list(l)

VIPER

Fractional (Recursive) Predicates



$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$

Acts on the predicate mask

inhale `list(l)`

...

exhale `acc(list(l), 0.5)`

...

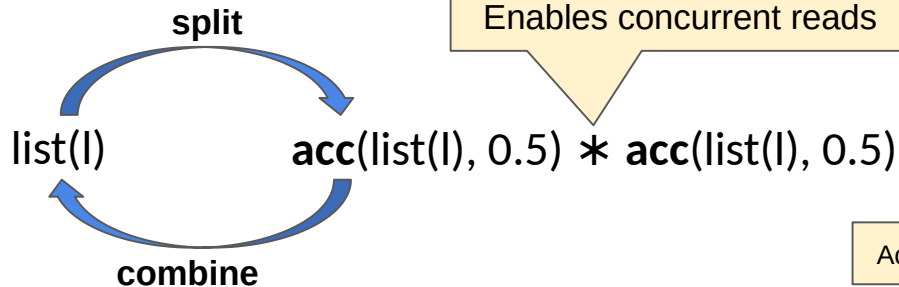
inhale `acc(list(l), 0.5)`

...

exhale `list(l)`

VIPER

Fractional (Recursive) Predicates



Acts on the predicate mask

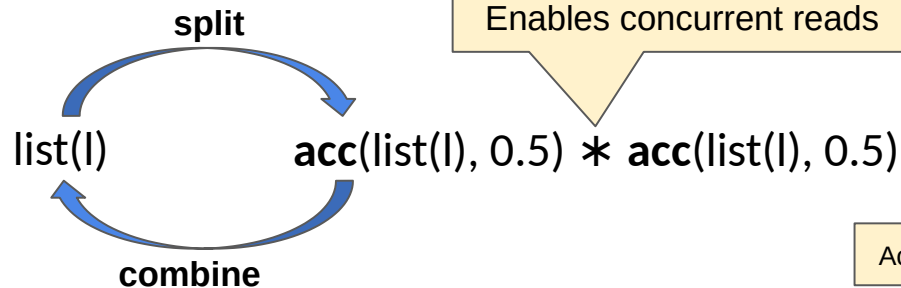
```
inhale list(l)
...
exhale acc(list(l), 0.5)
...
inhale acc(list(l), 0.5)
...
exhale list(l)
```

$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$

↓ automatically derived (syntactically)

$\text{acc}(\text{list}(l), \boxed{0.5}) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}, 0.5) * \text{acc}(l.\text{next}, 0.5) * \text{acc}(\text{list}(l.\text{next}, 0.5))))$

Fractional (Recursive) Predicates



Enables concurrent reads

Acts on the predicate mask

inhale list(l)

...

exhale acc(list(l), 0.5)

...

inhale acc(list(l), 0.5)

...

exhale list(l)

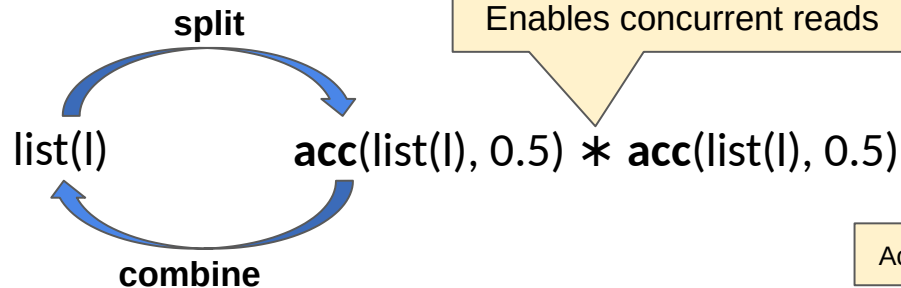
$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$



automatically derived (syntactically)

$\text{acc}(\text{list}(l), 0.5) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}, 0.5) * \text{acc}(l.\text{next}, 0.5) * \text{acc}(\text{list}(l.\text{next}), 0.5)))$

Fractional (Recursive) Predicates



inhale list(l)
...
exhale acc(list(l), 0.5)
...
inhale acc(list(l), 0.5)
...
exhale list(l)

Acts on the predicate mask

$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$

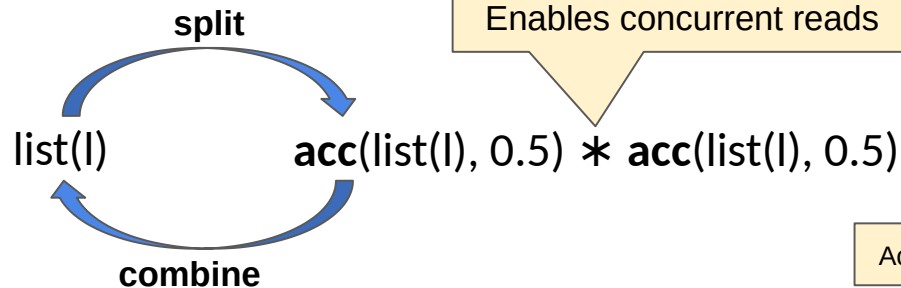
automatically derived (syntactically)

unfold

$\text{acc}(\text{list}(l), 0.5) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}, 0.5) * \text{acc}(l.\text{next}, 0.5) * \text{acc}(\text{list}(l.\text{next}), 0.5)))$

fold

Fractional (Recursive) Predicates



inhale list(l)
...
exhale acc(list(l), 0.5)
...
inhale acc(list(l), 0.5)
...
exhale list(l)

Acts on the predicate mask

$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$

automatically derived (syntactically)

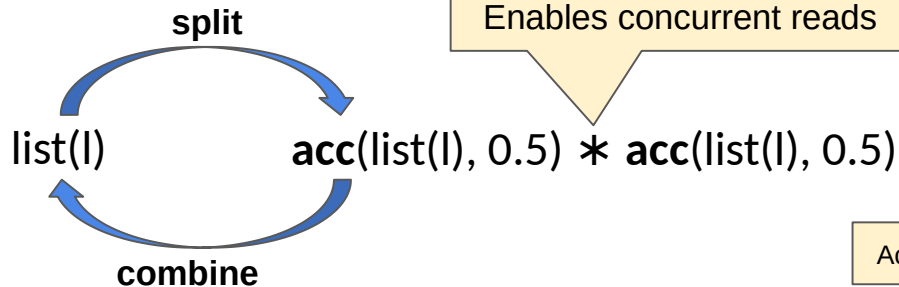
unfold

$\text{acc}(\text{list}(l), 0.5) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}, 0.5) * \text{acc}(l.\text{next}, 0.5) * \text{acc}(\text{list}(l.\text{next}), 0.5)))$

fold

Sound for Viper (recursive) predicate definitions!

Fractional (Recursive) Predicates



Enables concurrent reads

Acts on the predicate mask

```

inhale list(l)
...
exhale acc(list(l), 0.5)
...
inhale acc(list(l), 0.5)
...
exhale list(l)
    
```

$$\text{list}(l) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}) * \text{acc}(l.\text{next}) * \text{list}(l.\text{next})))$$

automatically derived (syntactically)

unfold

fold

$$\text{acc}(\text{list}(l), 0.5) \triangleq (l \neq \text{null} \Rightarrow (\text{acc}(l.\text{value}, 0.5) * \text{acc}(l.\text{next}, 0.5) * \text{acc}(\text{list}(l.\text{next}), 0.5)))$$

Sound for Viper (recursive) predicate definitions!

Theoretical foundations in our OOPSLA'22 paper
"Fractional Resources in Unbounded Separation Logic"

Outline of the Talk

1. Overview of Viper
2. Inhale and Exhale: An Operational View of Separation Logic
3. Designed for Automation
- 4. Toward a Foundational Viper**

Toward a Foundational Viper

Toward a Foundational Viper

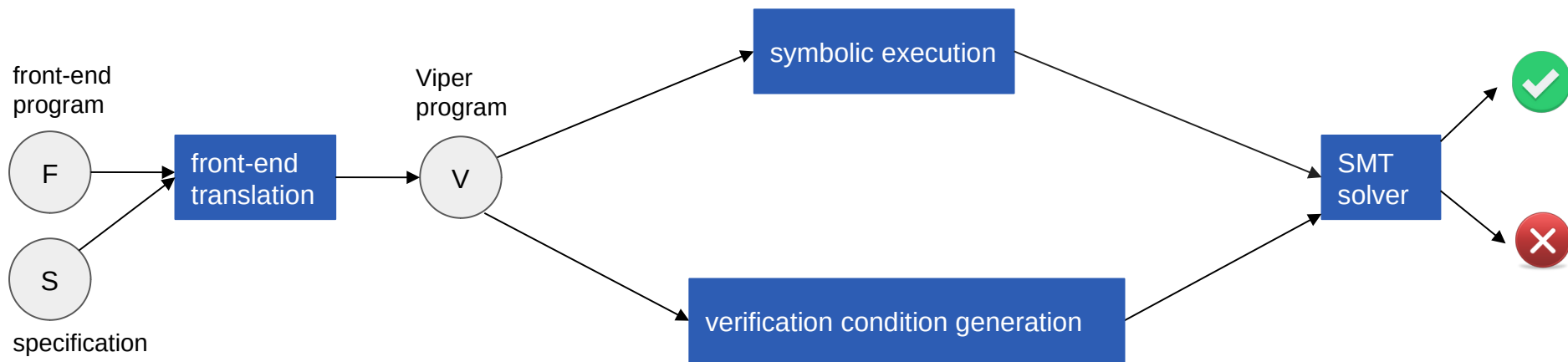
Iris from the ground up: A modular foundation for higher-order concurrent separation logic
Ralf Jung, Robert Krebbers, Jacques-Henri Jourdan, Aleš Bizjak, Lars Birkedal, Derek Dreyer

Toward a Foundational Viper

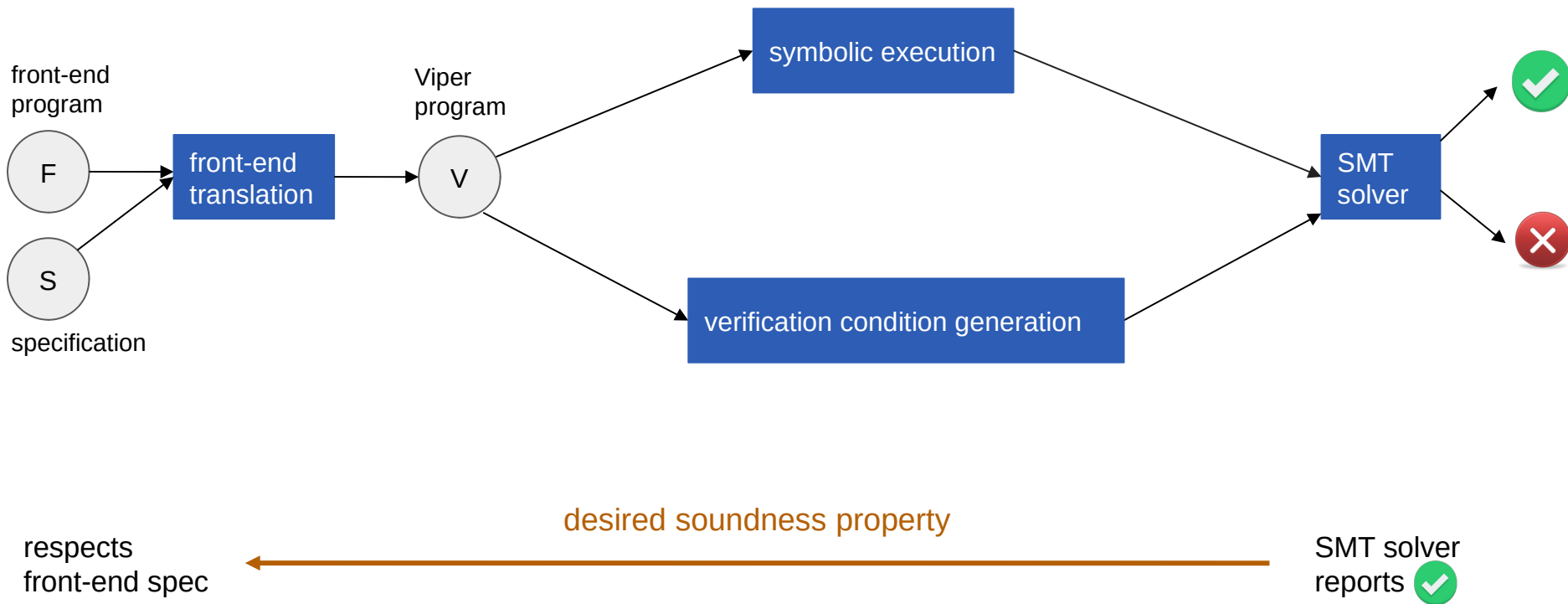
“This [foundational approach] is in contrast to tools like [...] **Viper**, which have much larger trusted computing bases because they assume the soundness of non-trivial extensions of Hoare logic and do not produce independently checkable proof terms.”

Iris from the ground up: A modular foundation for higher-order concurrent separation logic
Ralf Jung, Robert Krebbers, Jacques-Henri Jourdan, Aleš Bizjak, Lars Birkedal, Derek Dreyer

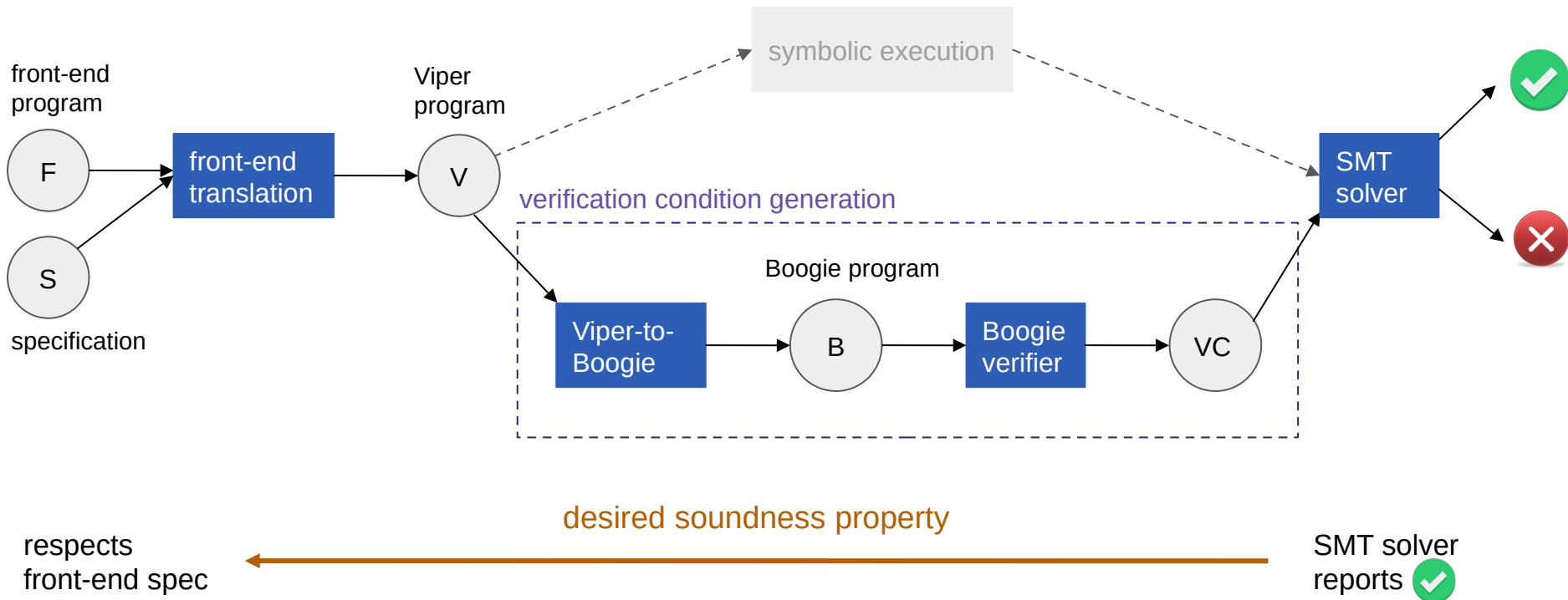
Soundness



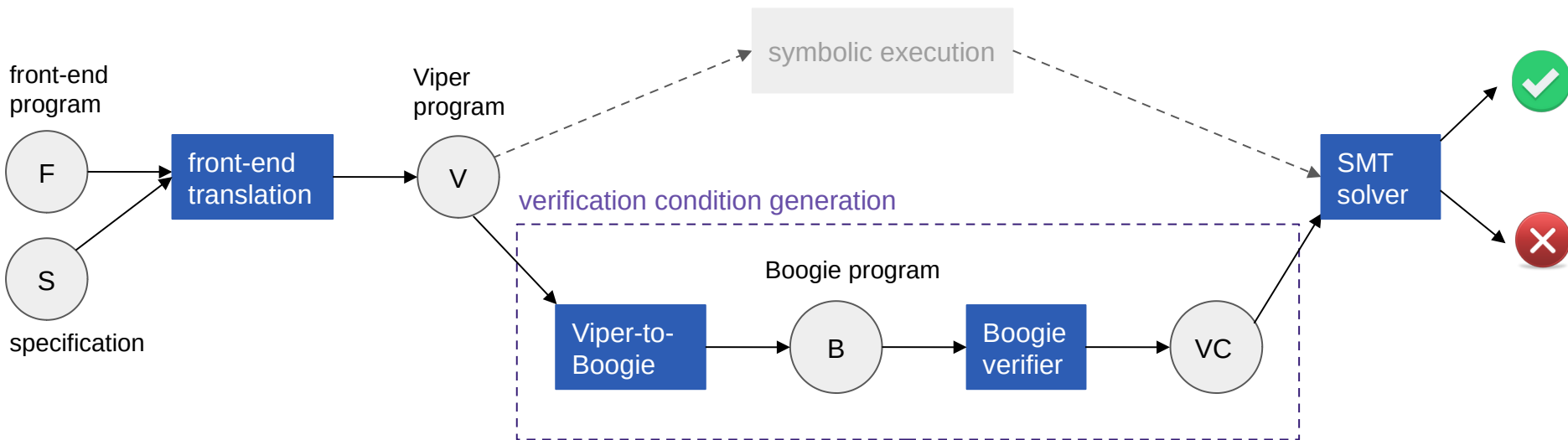
Soundness



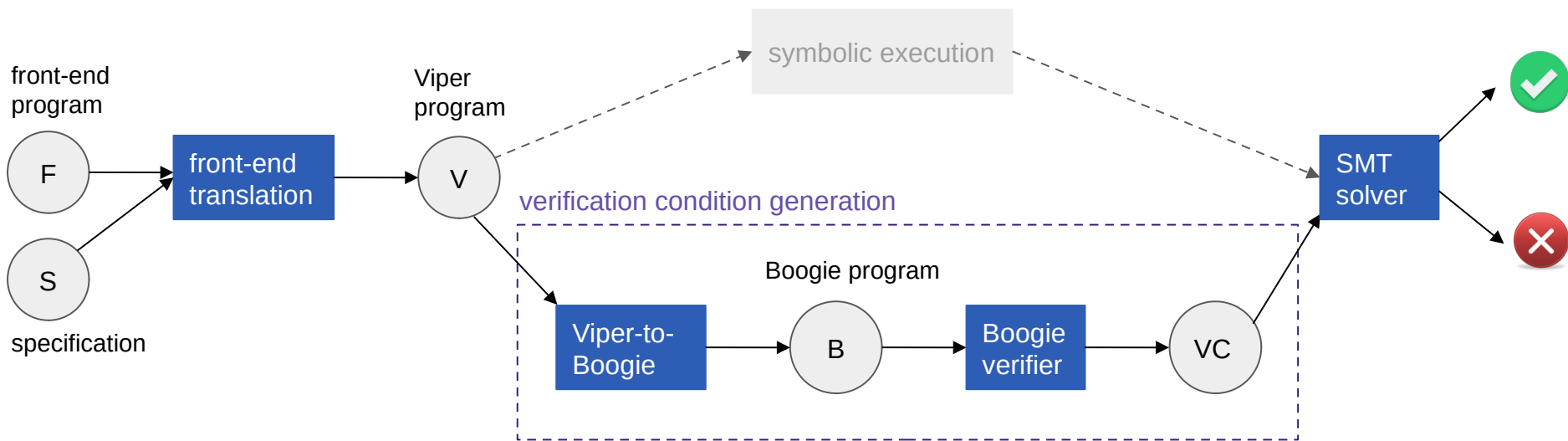
Soundness



Soundness: Proof Strategy

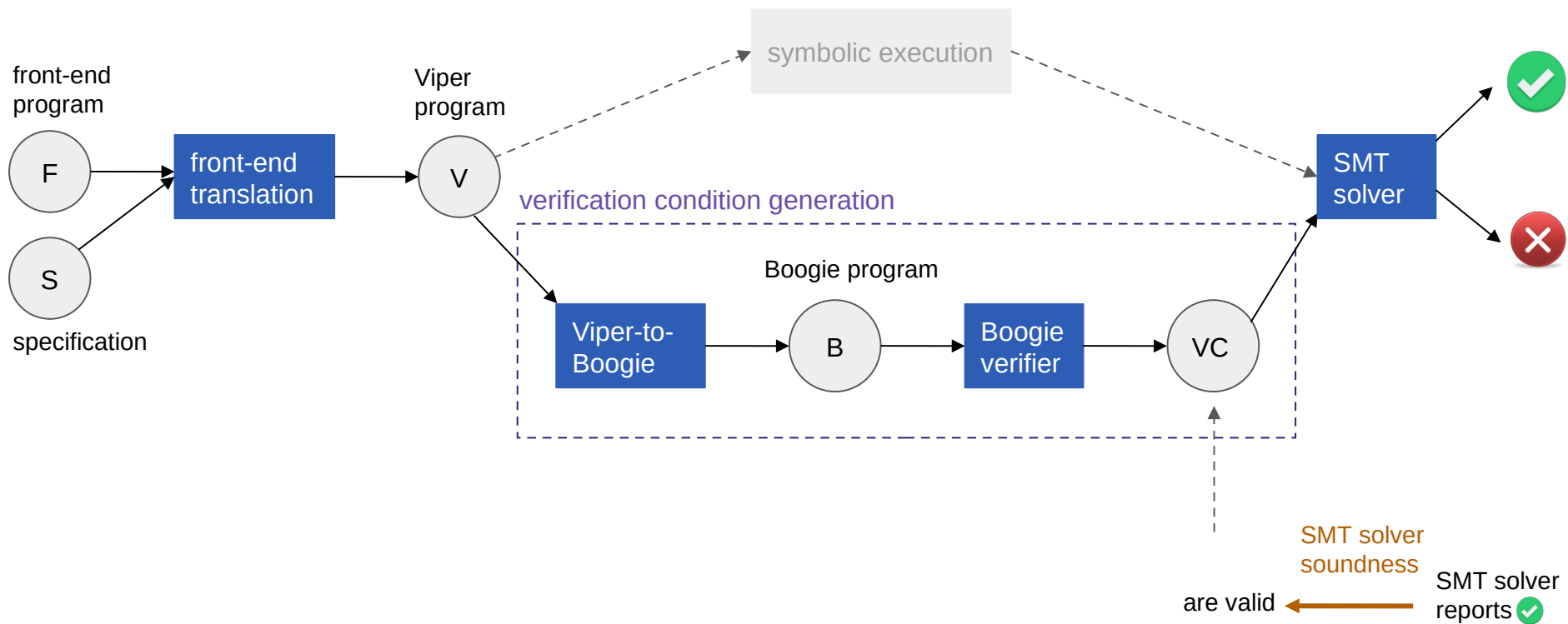


Soundness: Proof Strategy

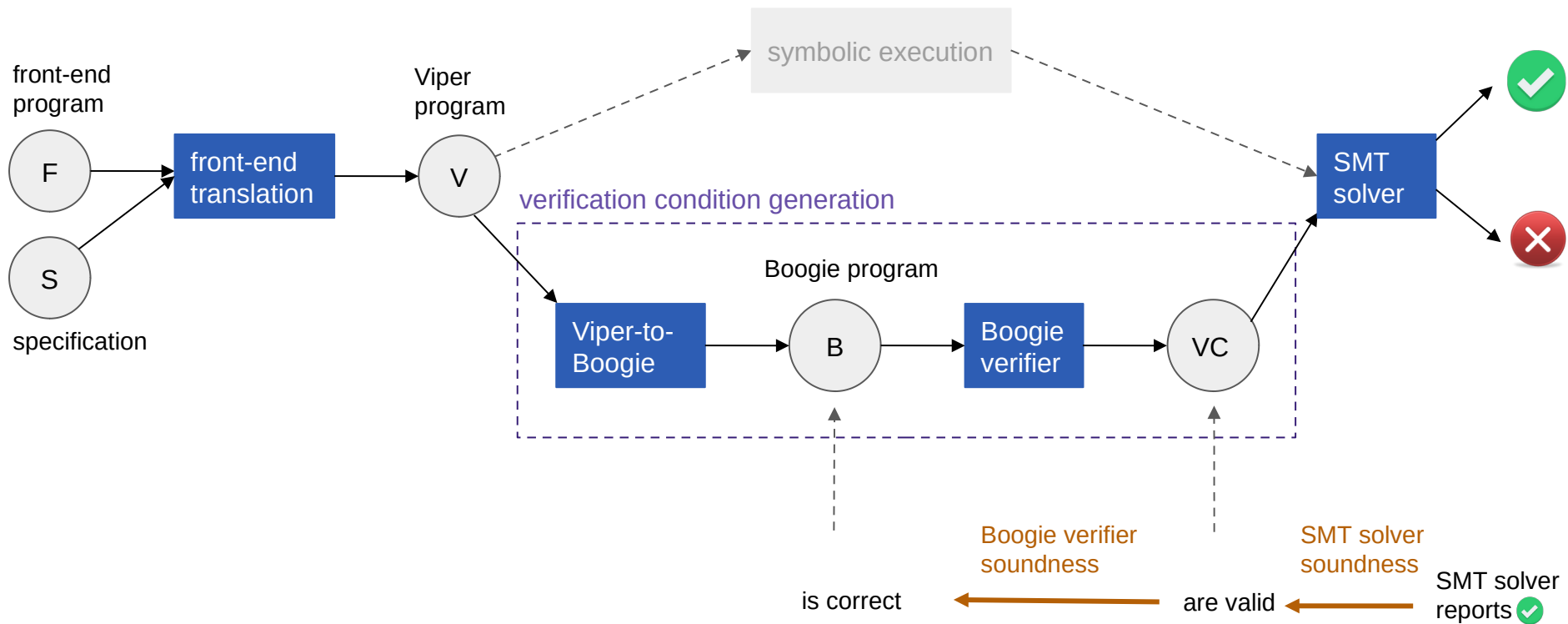


SMT solver reports ✓

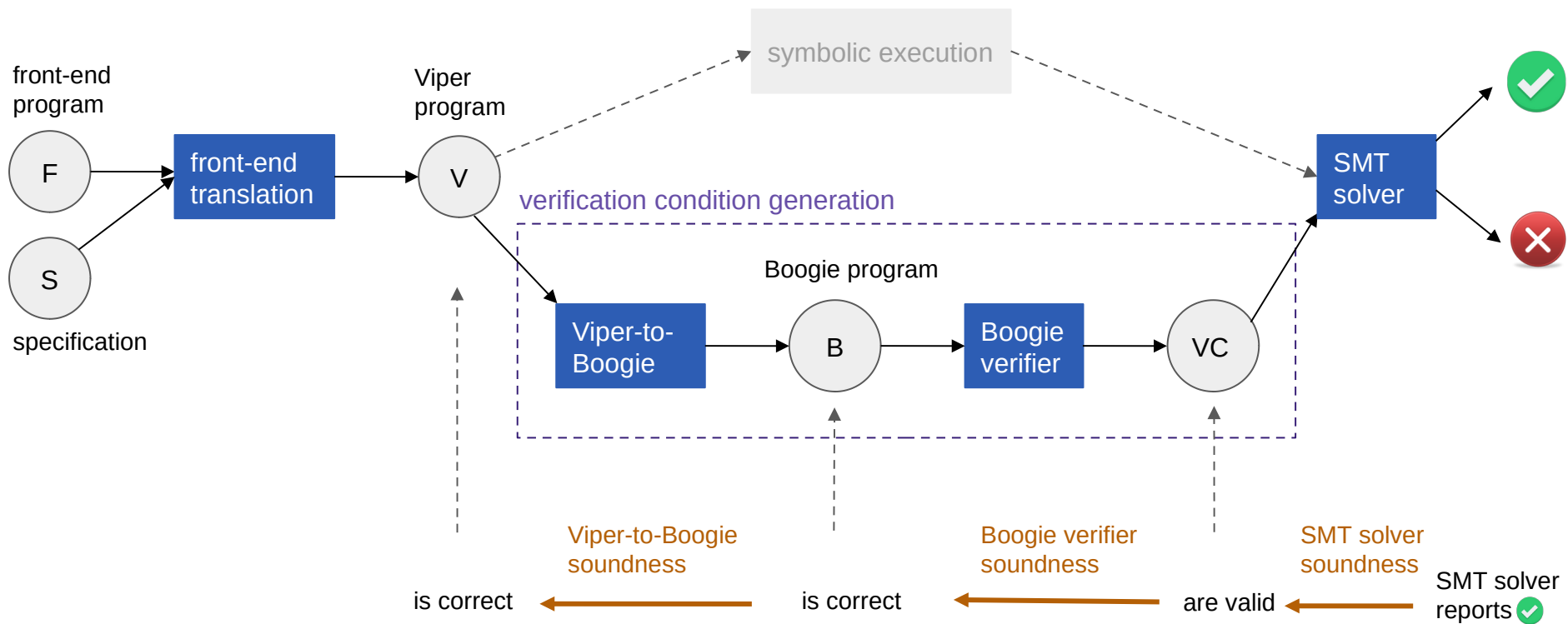
Soundness: Proof Strategy



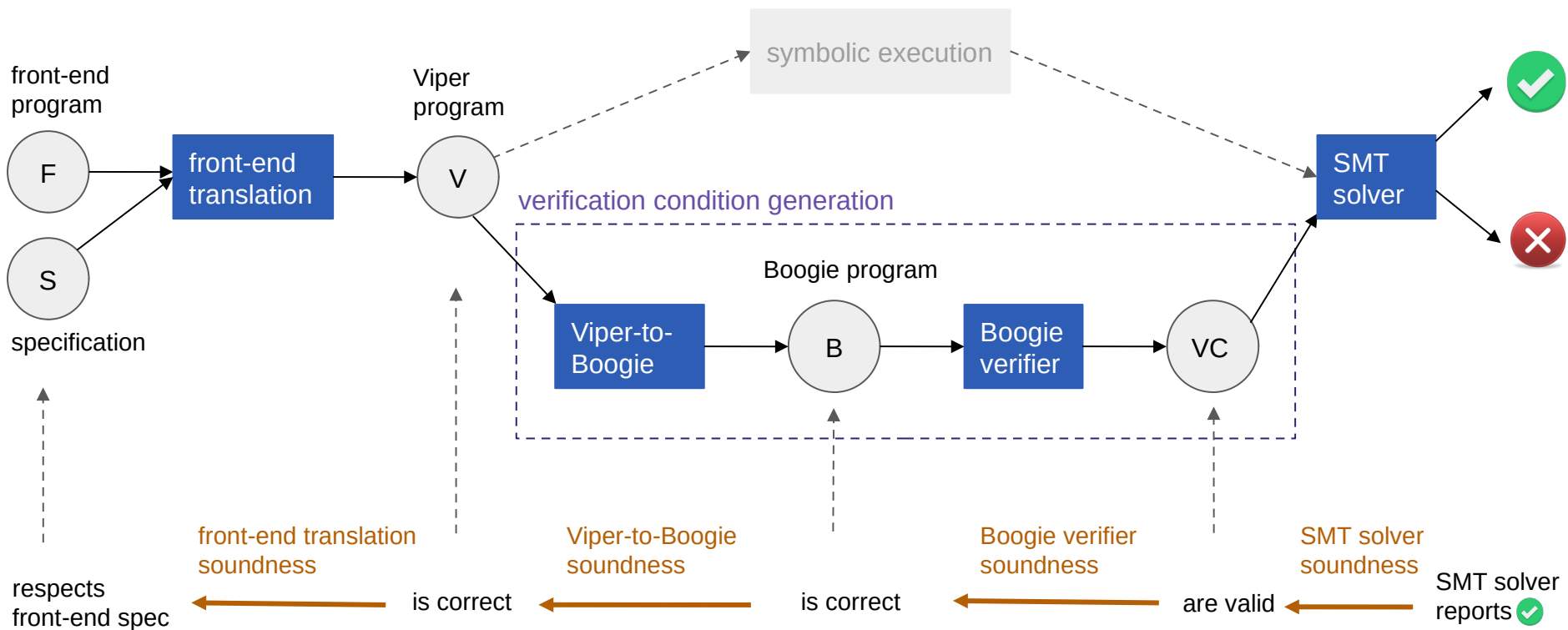
Soundness: Proof Strategy



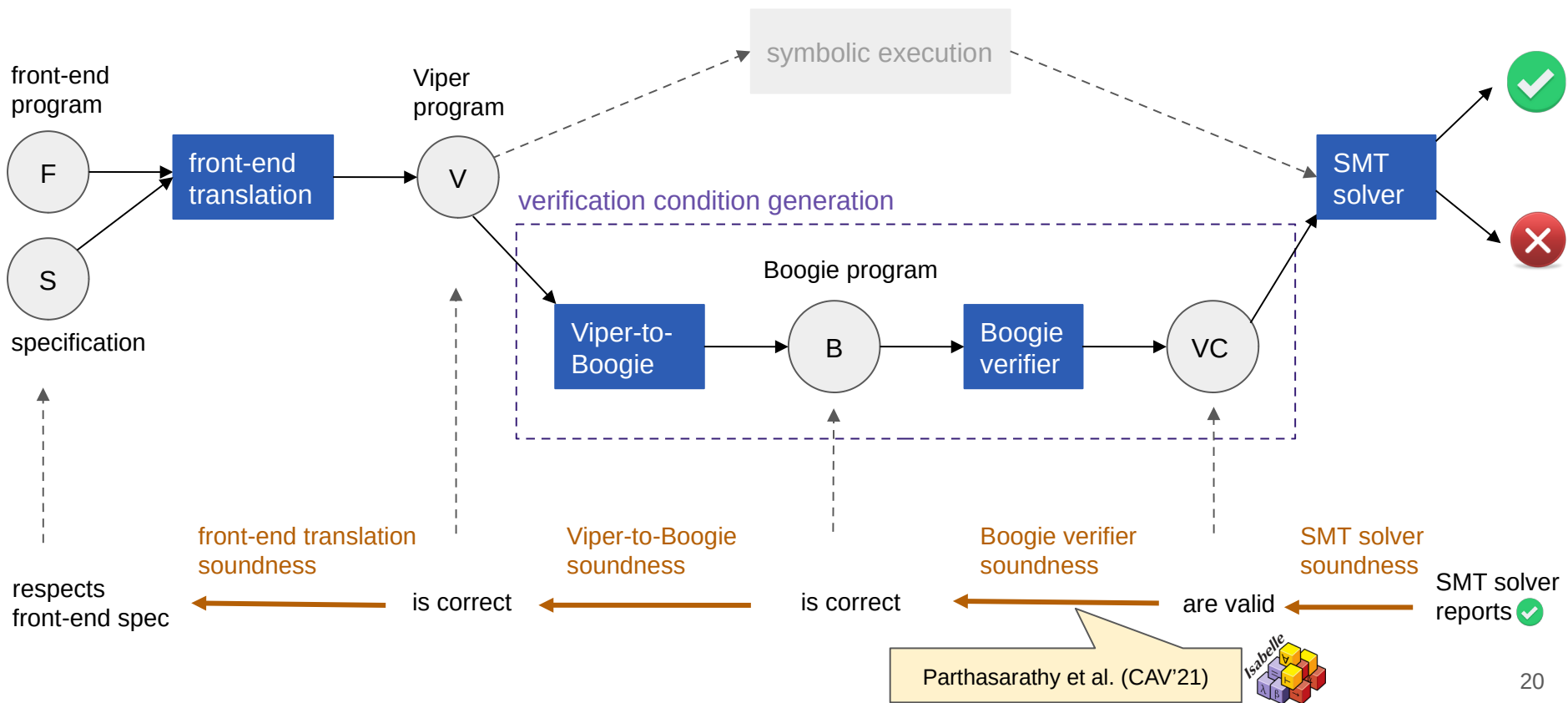
Soundness: Proof Strategy



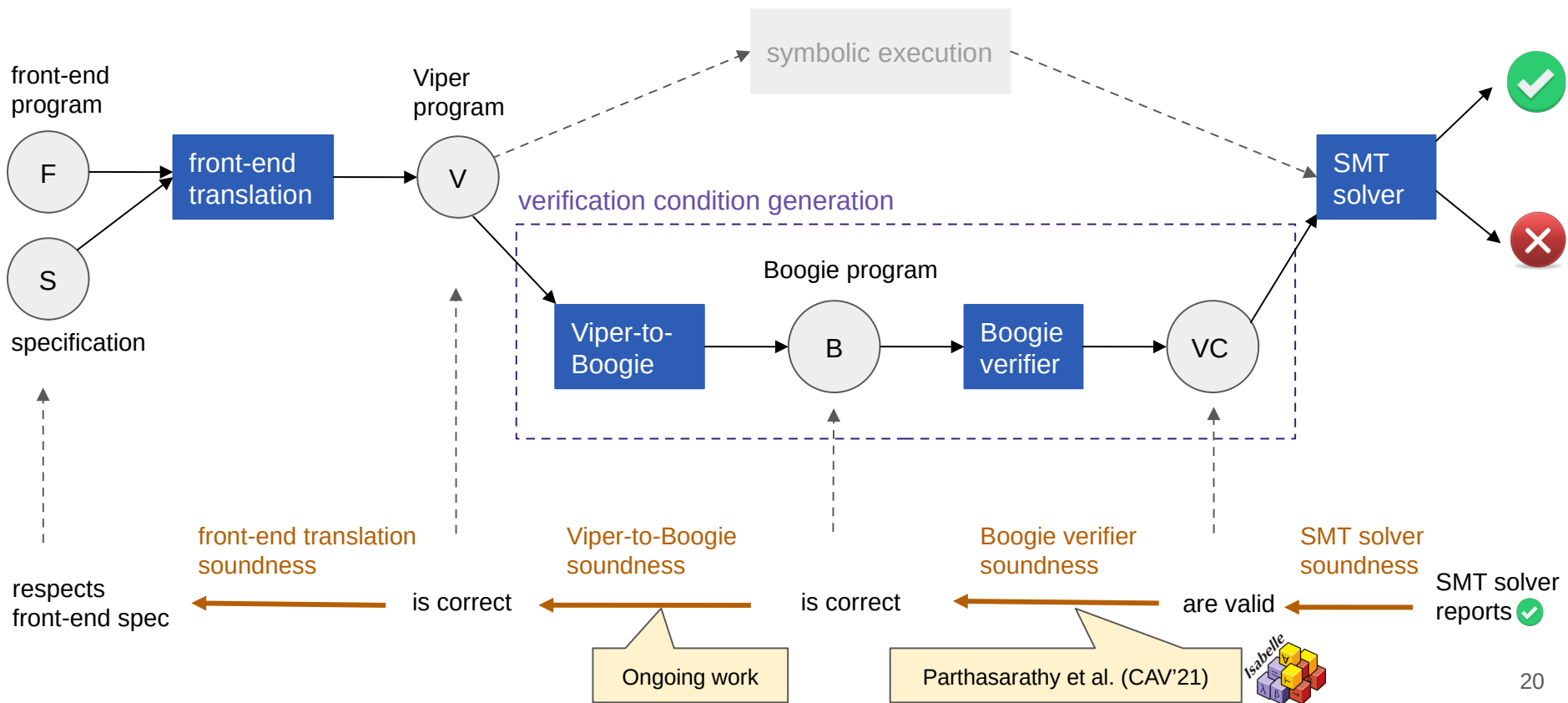
Soundness: Proof Strategy



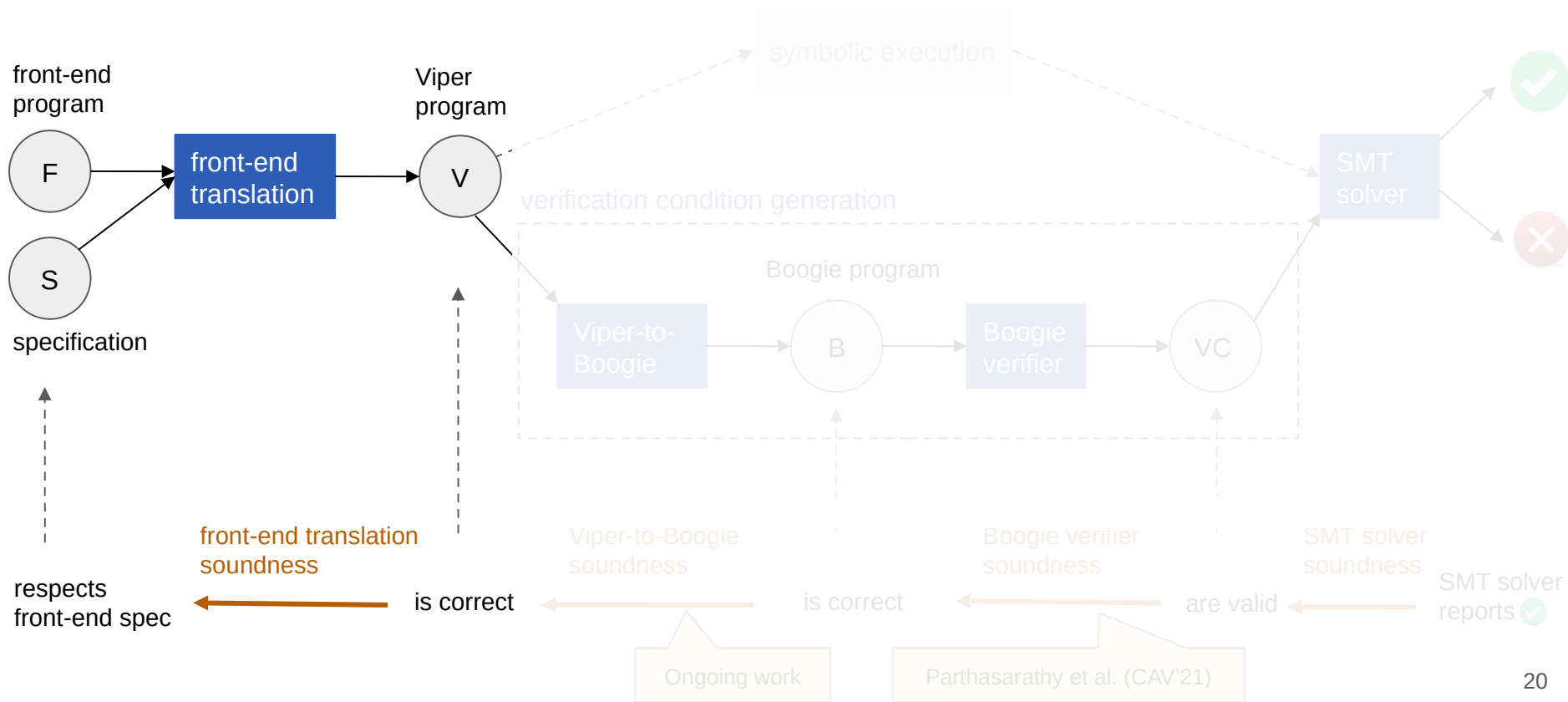
Soundness: Proof Strategy



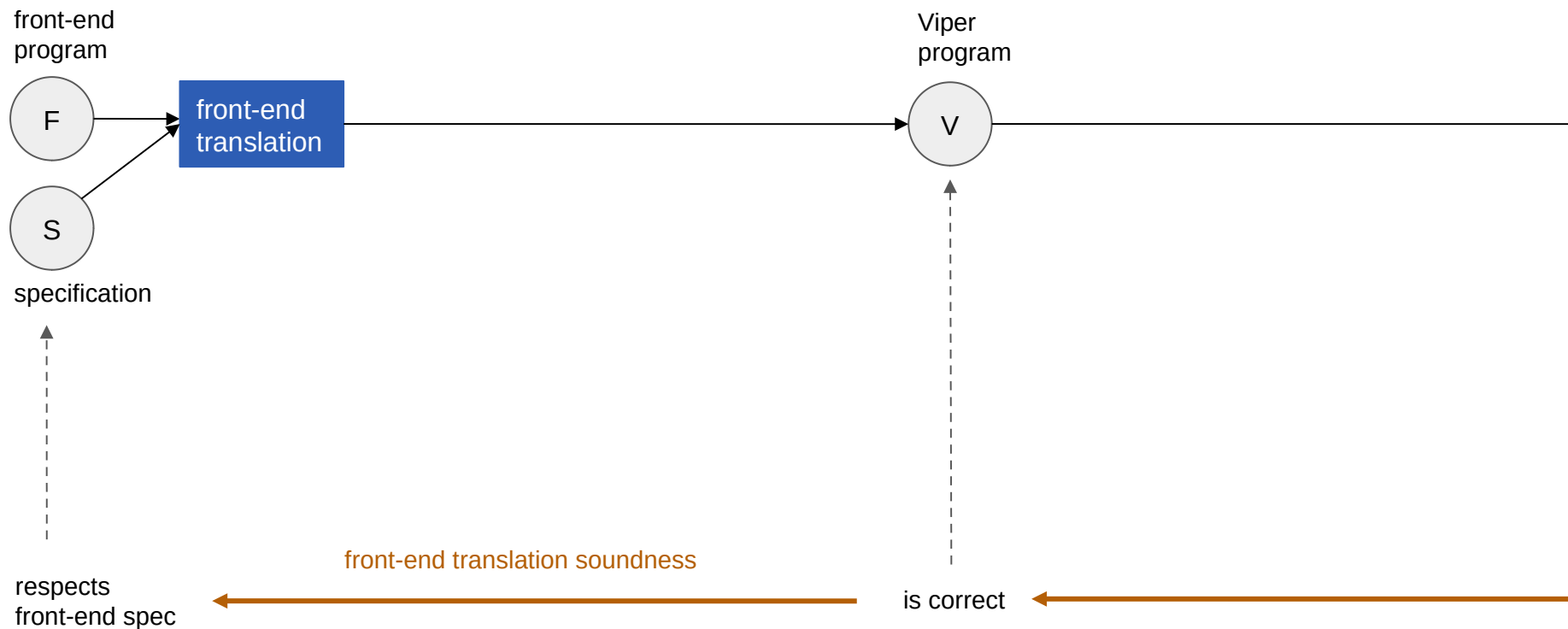
Soundness: Proof Strategy



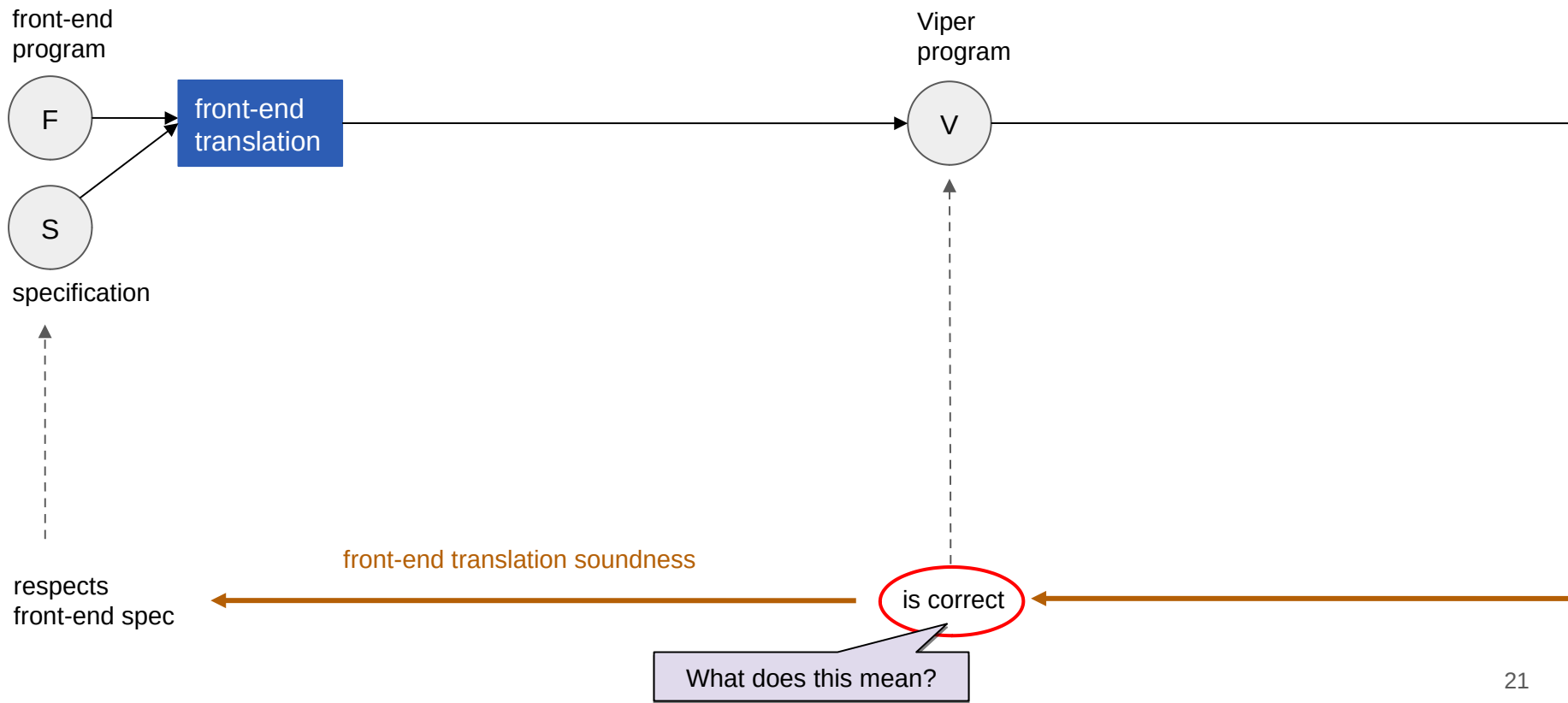
Soundness: Proof Strategy



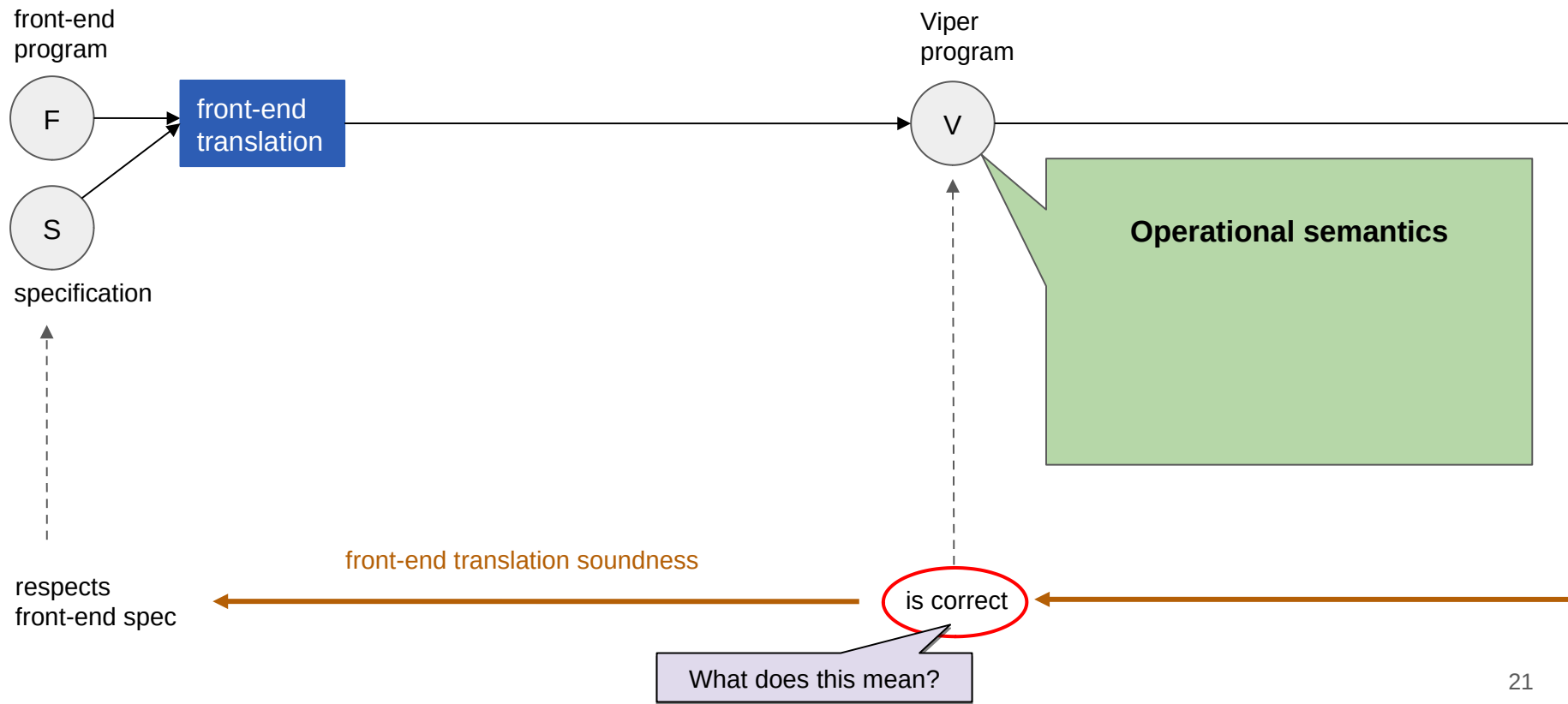
Operational Semantics and Adequacy Theorem



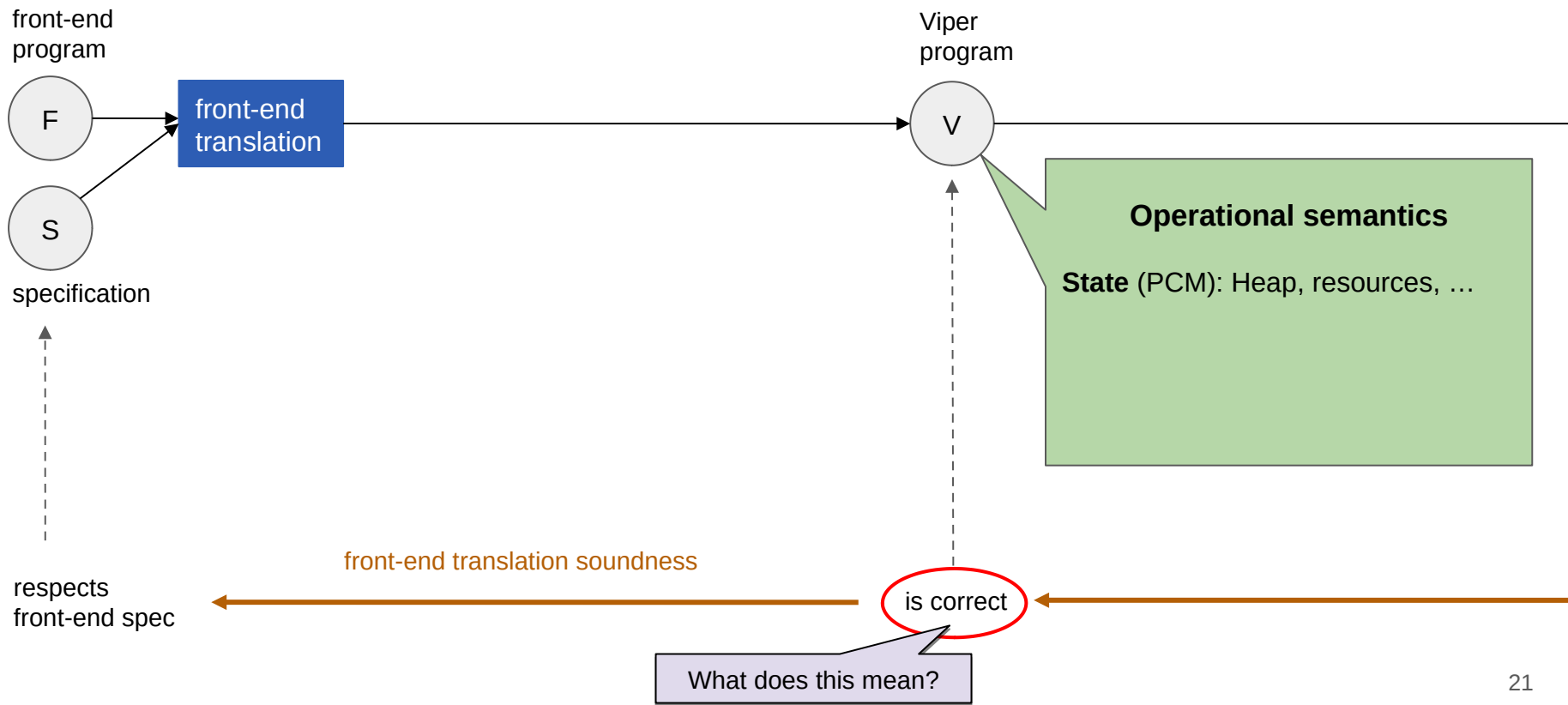
Operational Semantics and Adequacy Theorem



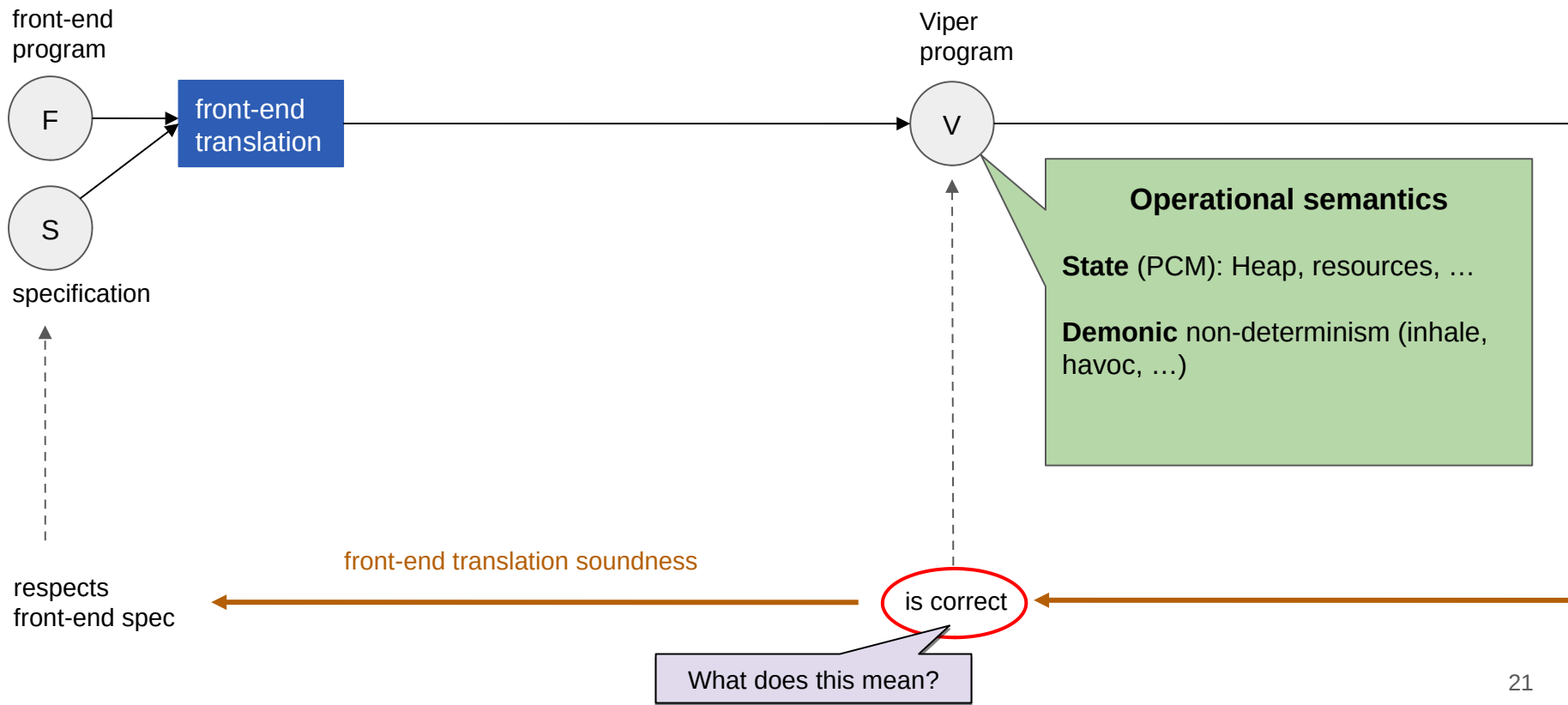
Operational Semantics and Adequacy Theorem



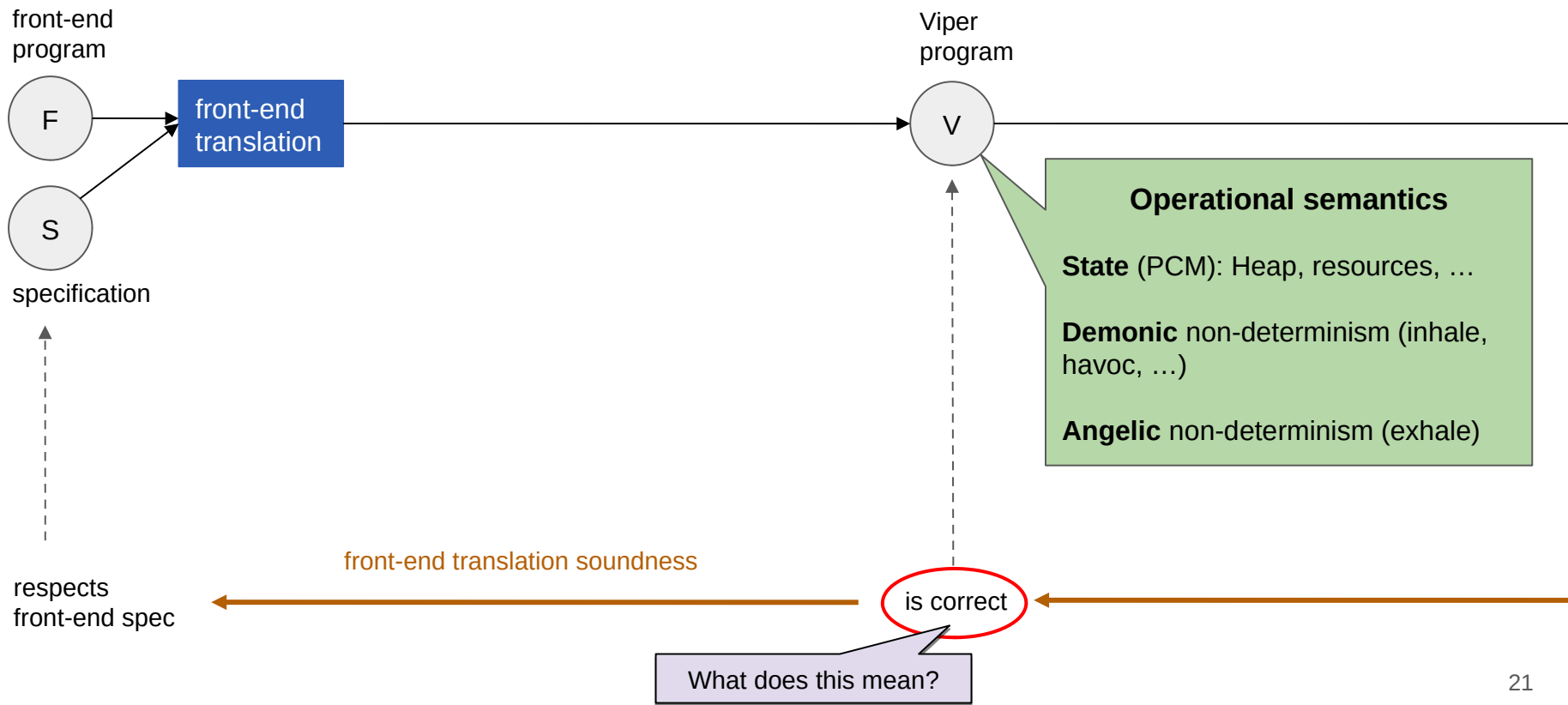
Operational Semantics and Adequacy Theorem



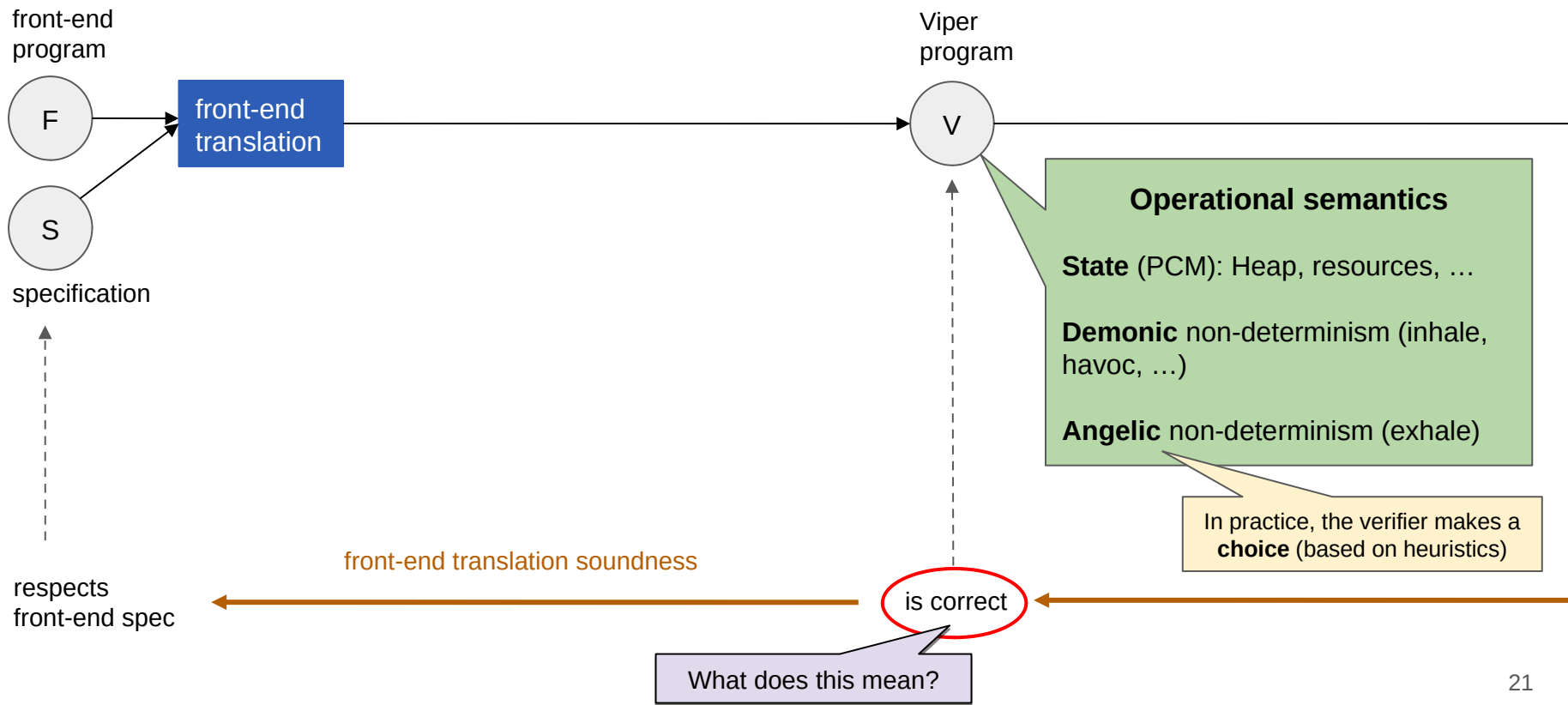
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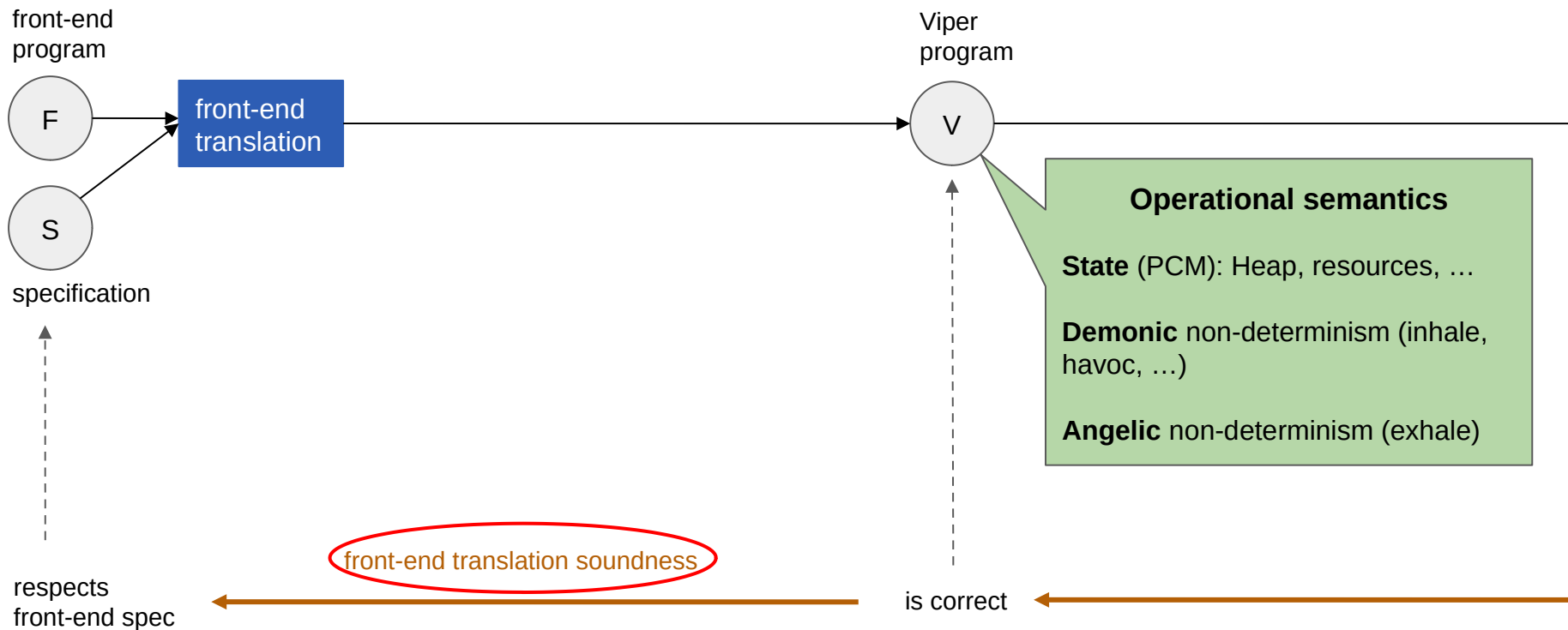
Operational Semantics and Adequacy Theorem



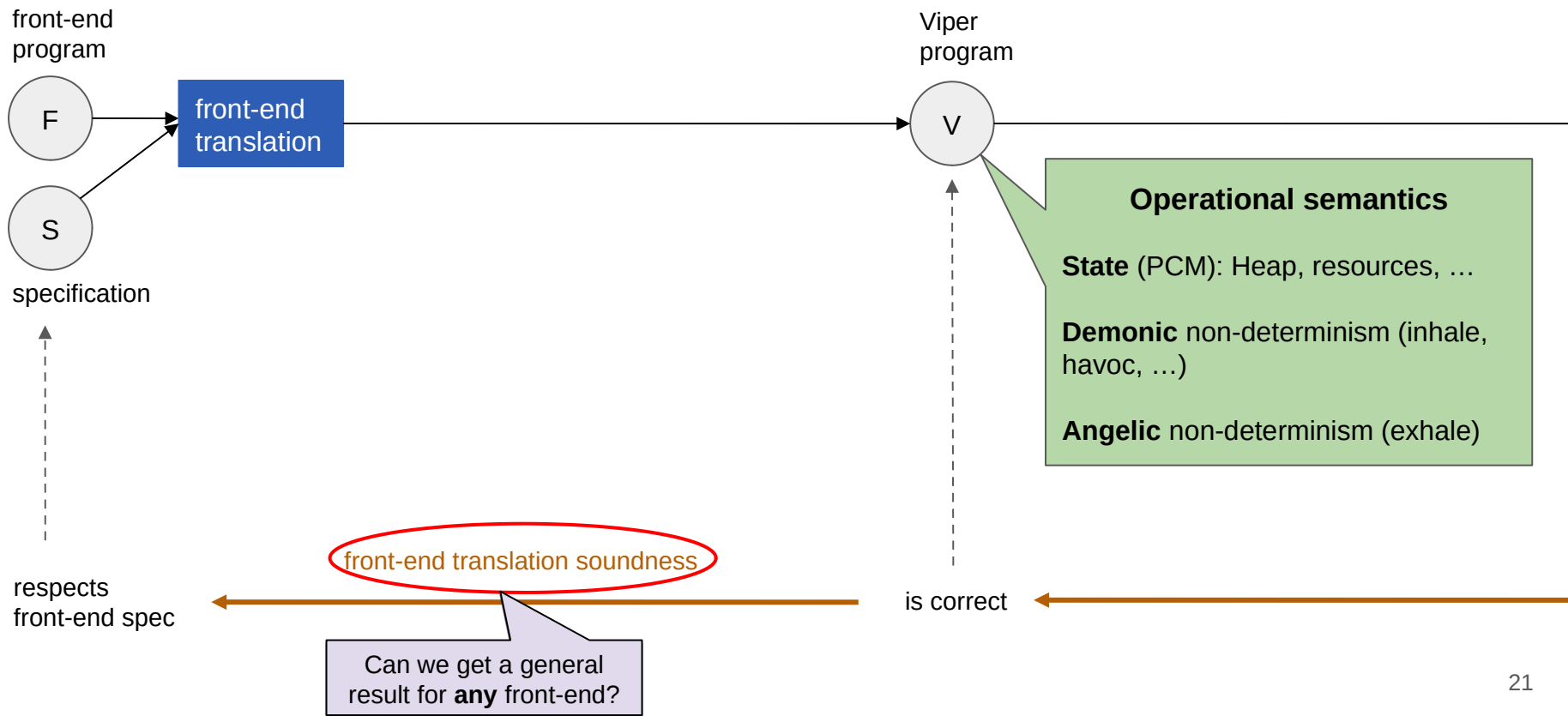
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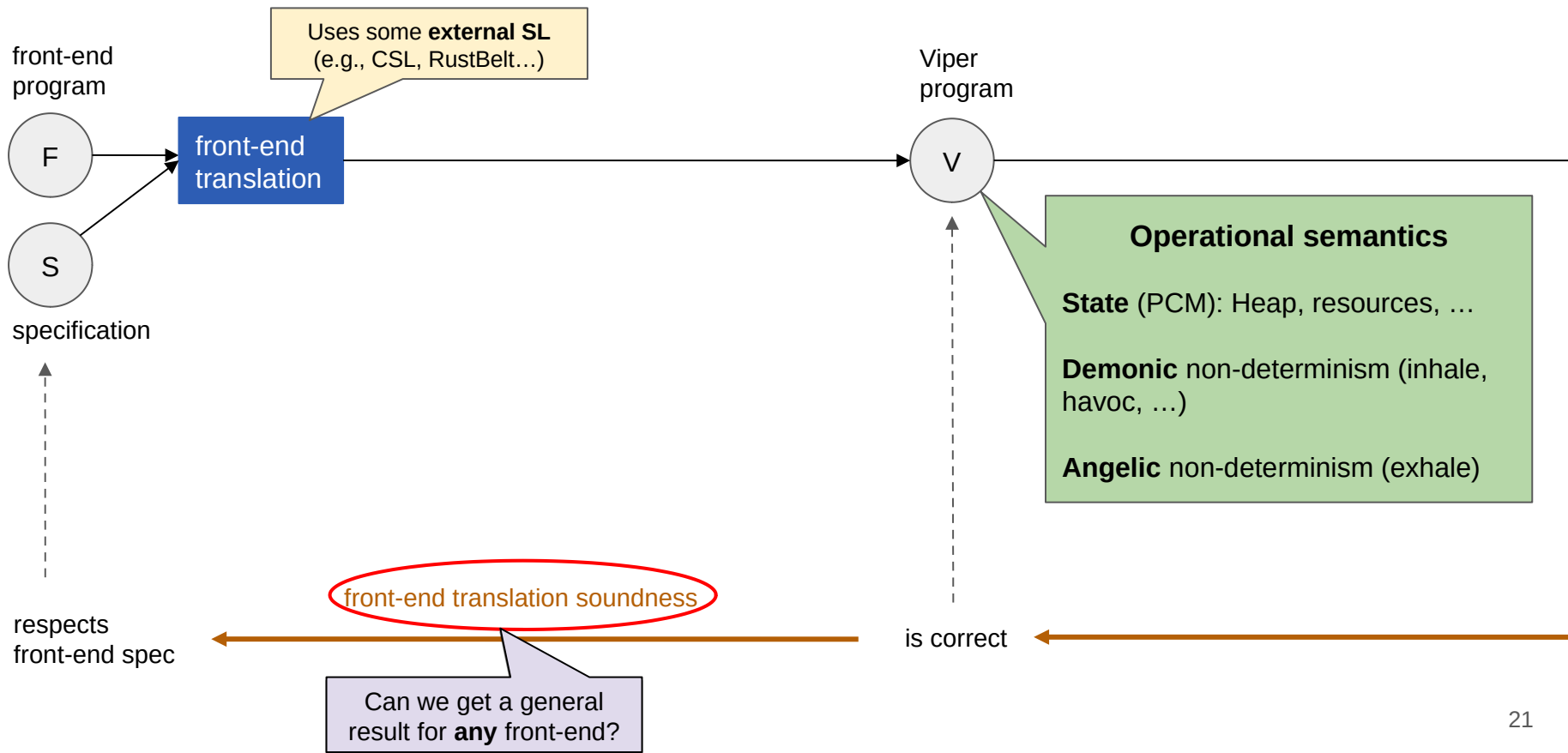
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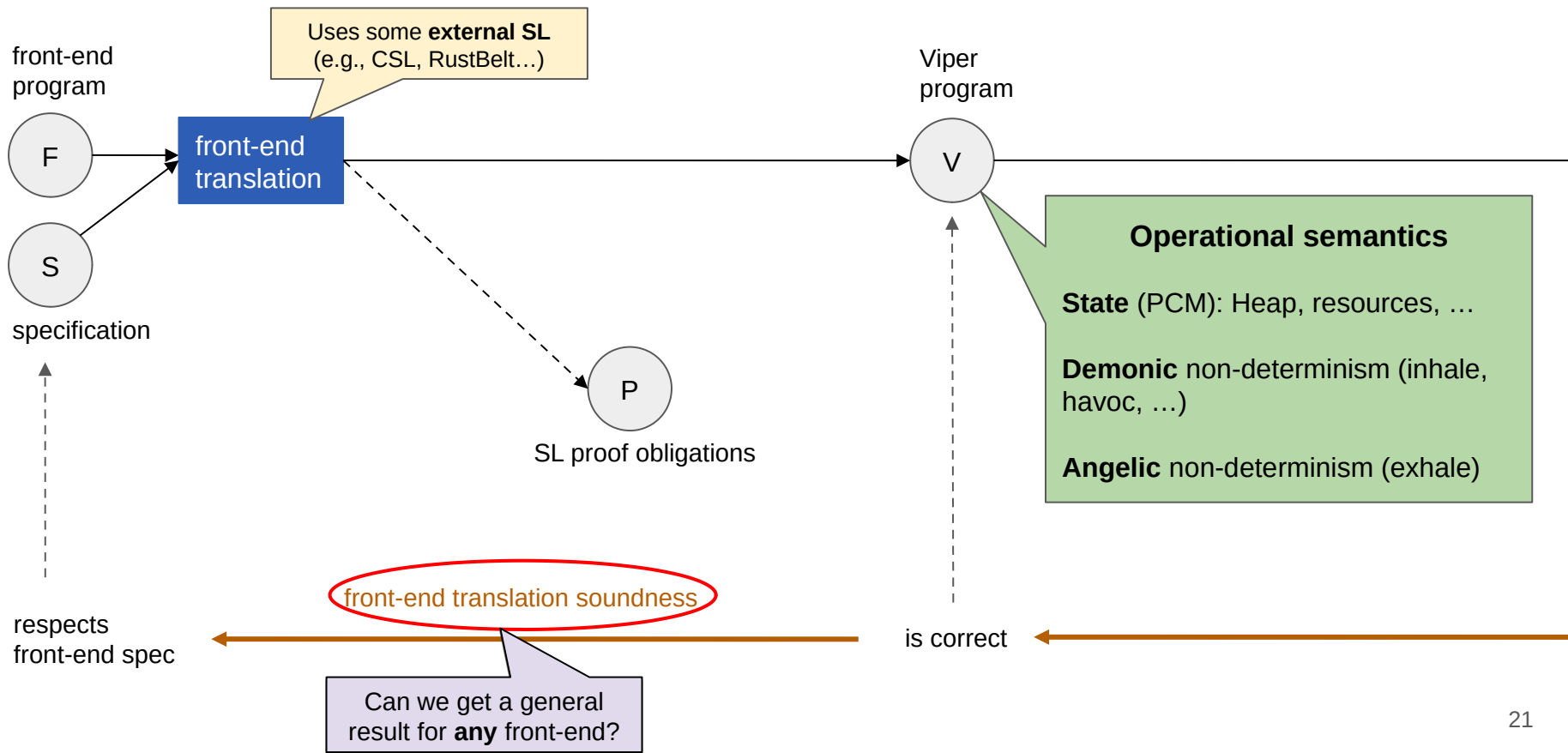
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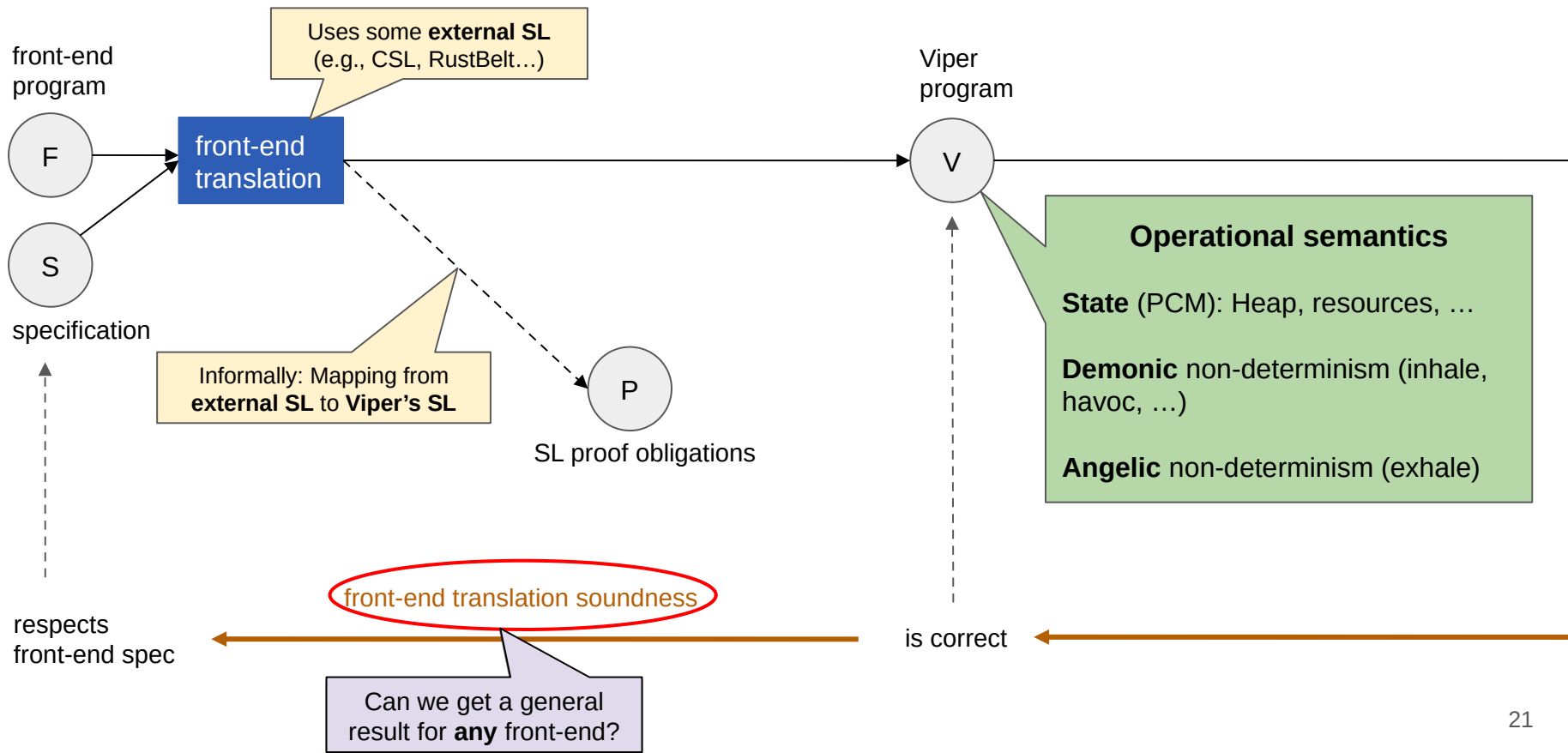
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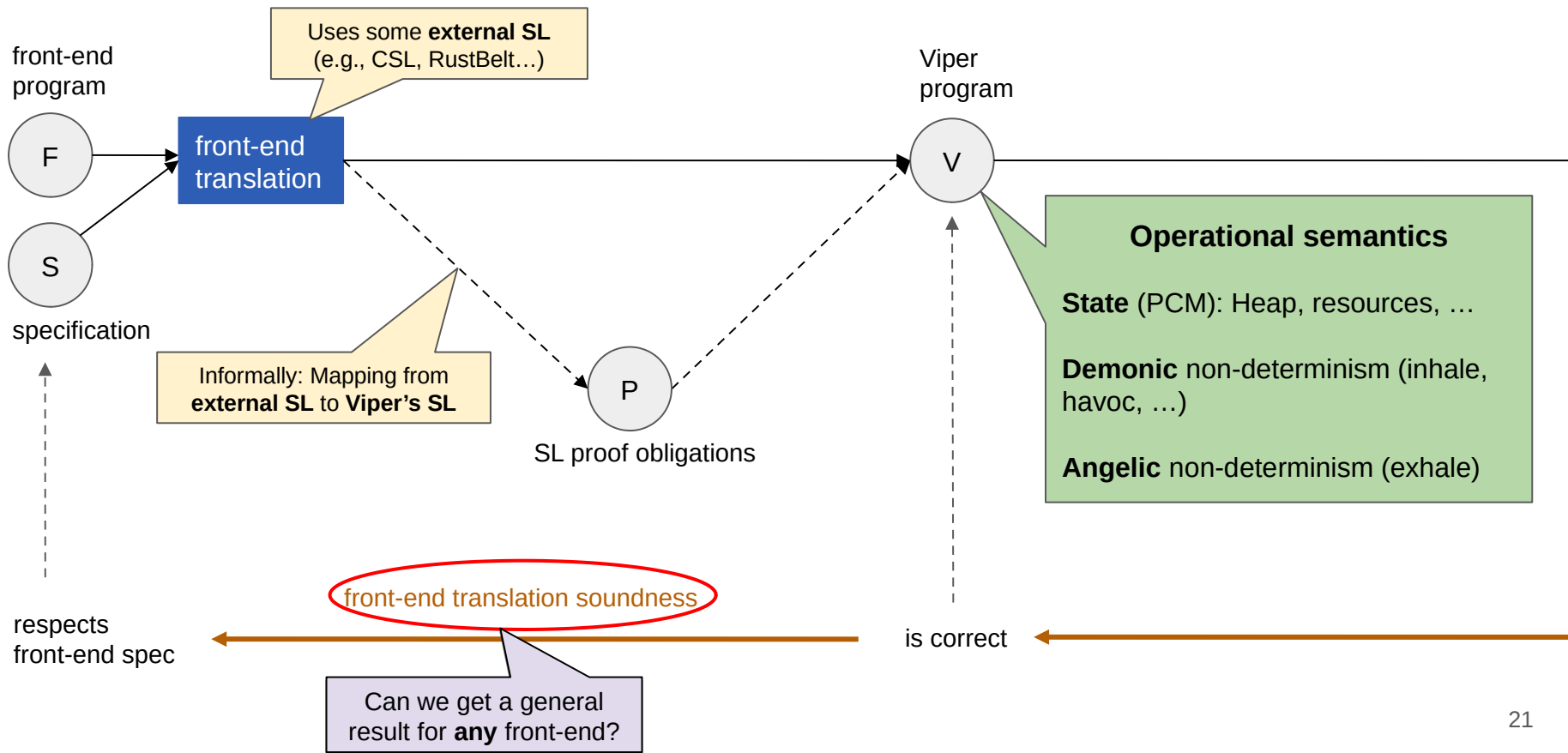
Operational Semantics and Adequacy Theorem



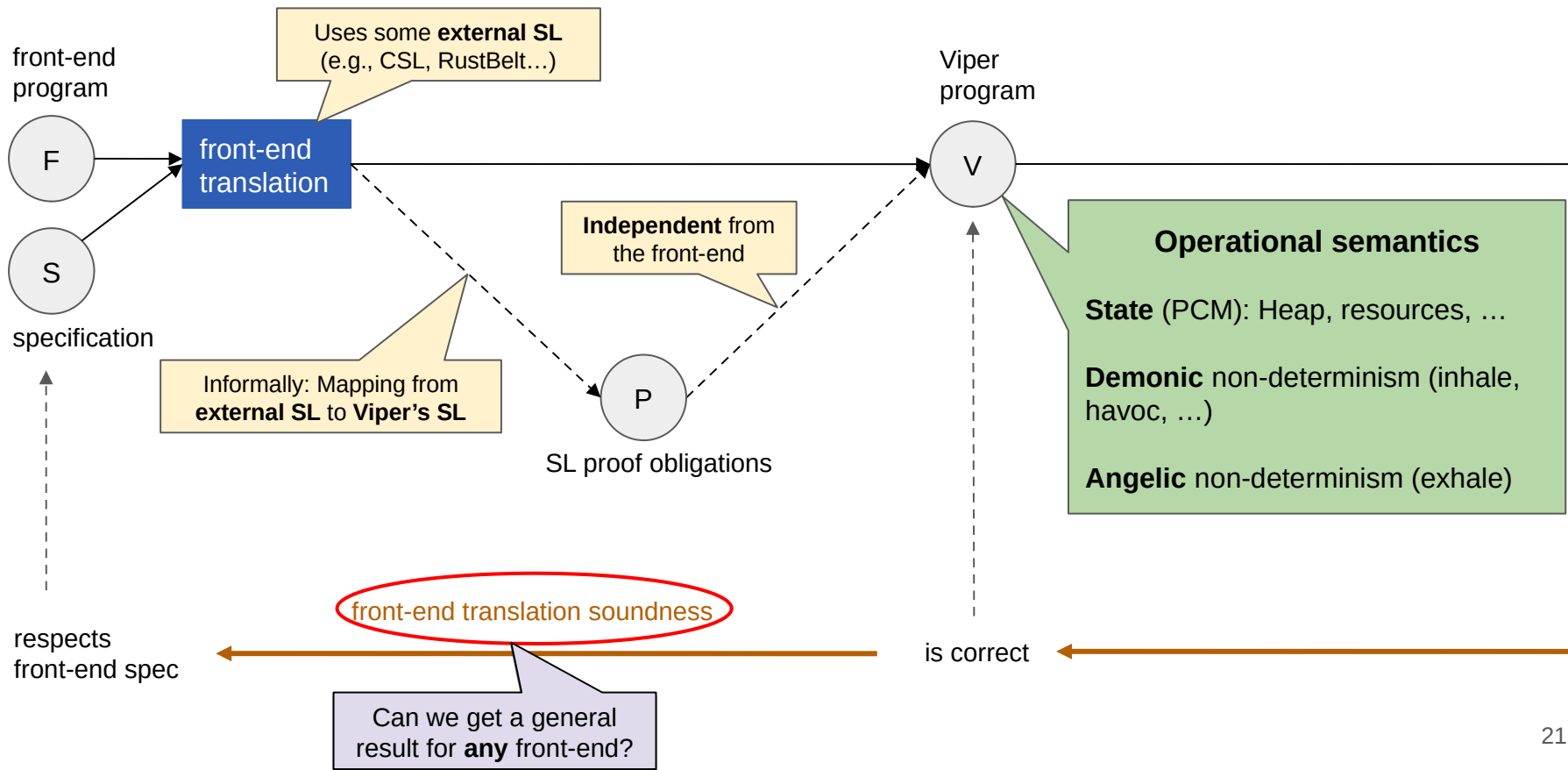
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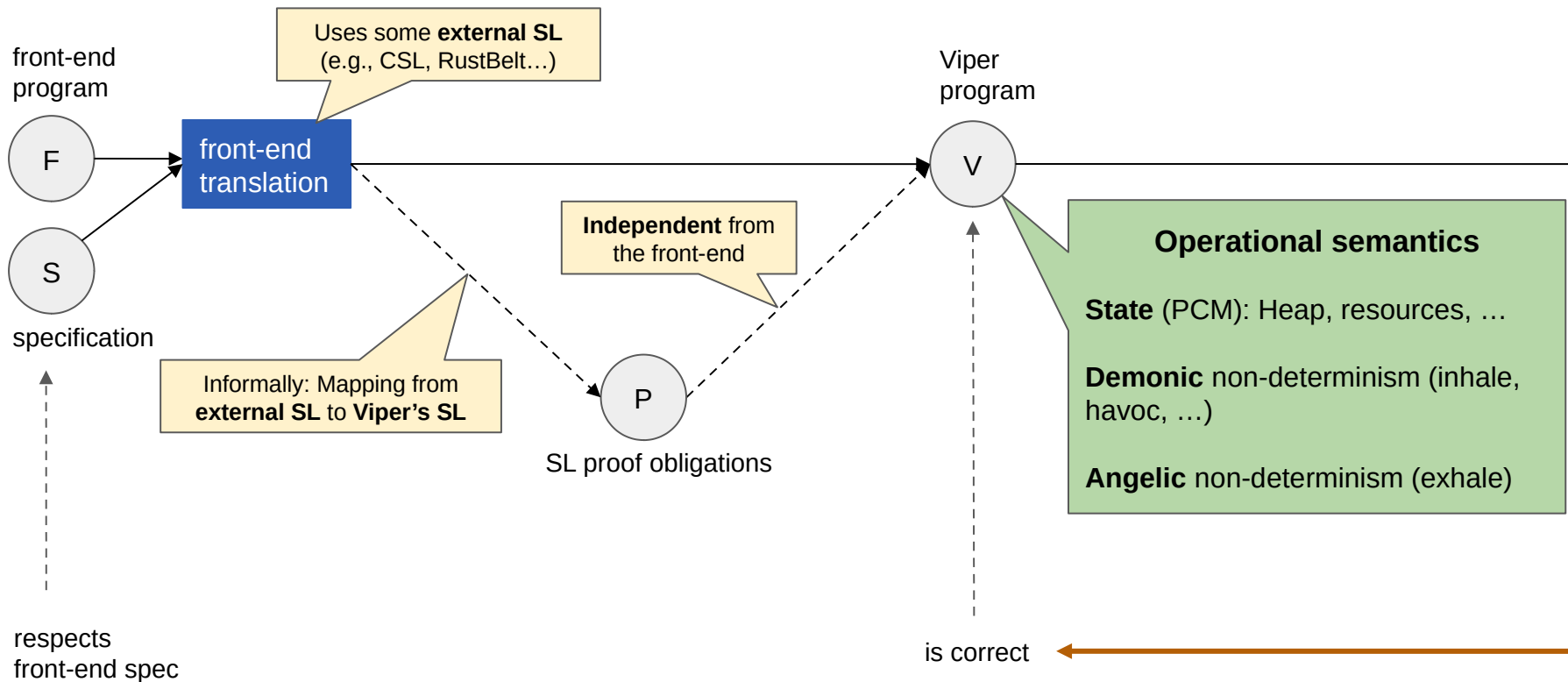
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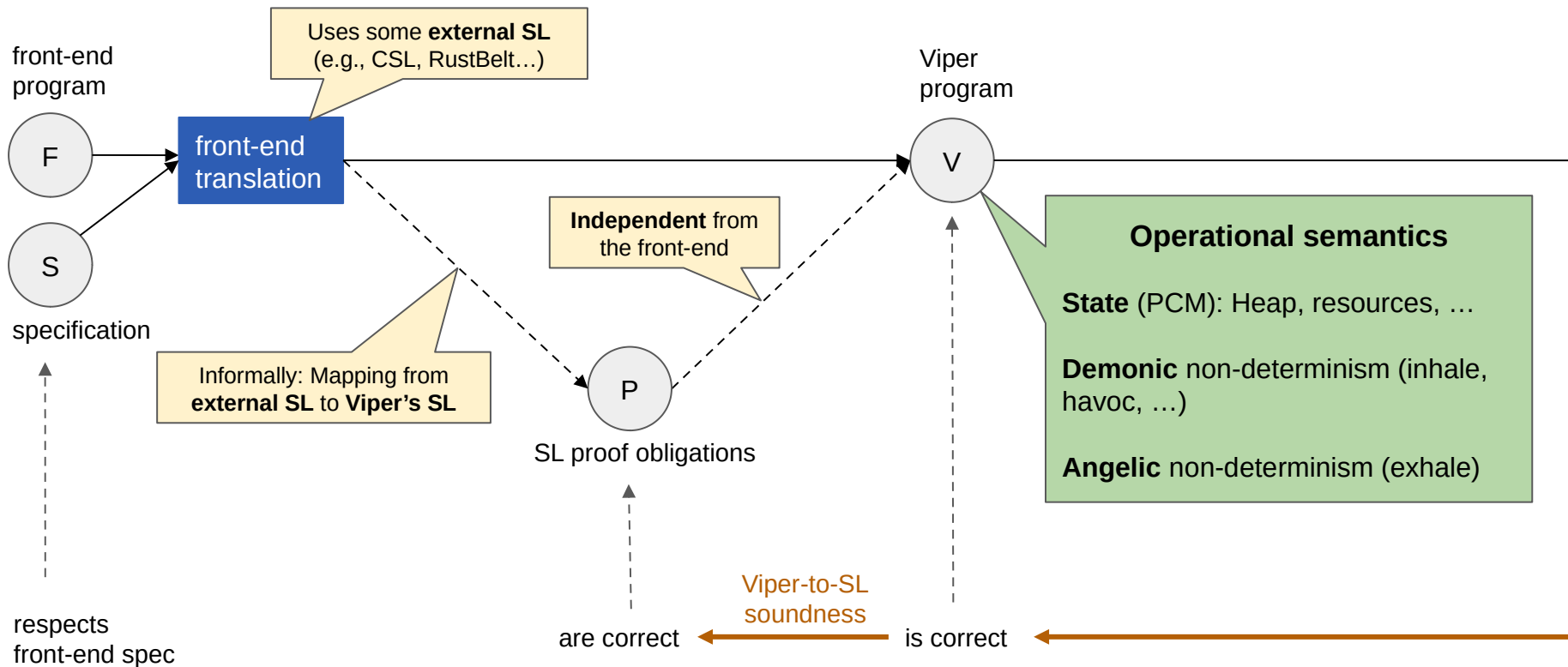
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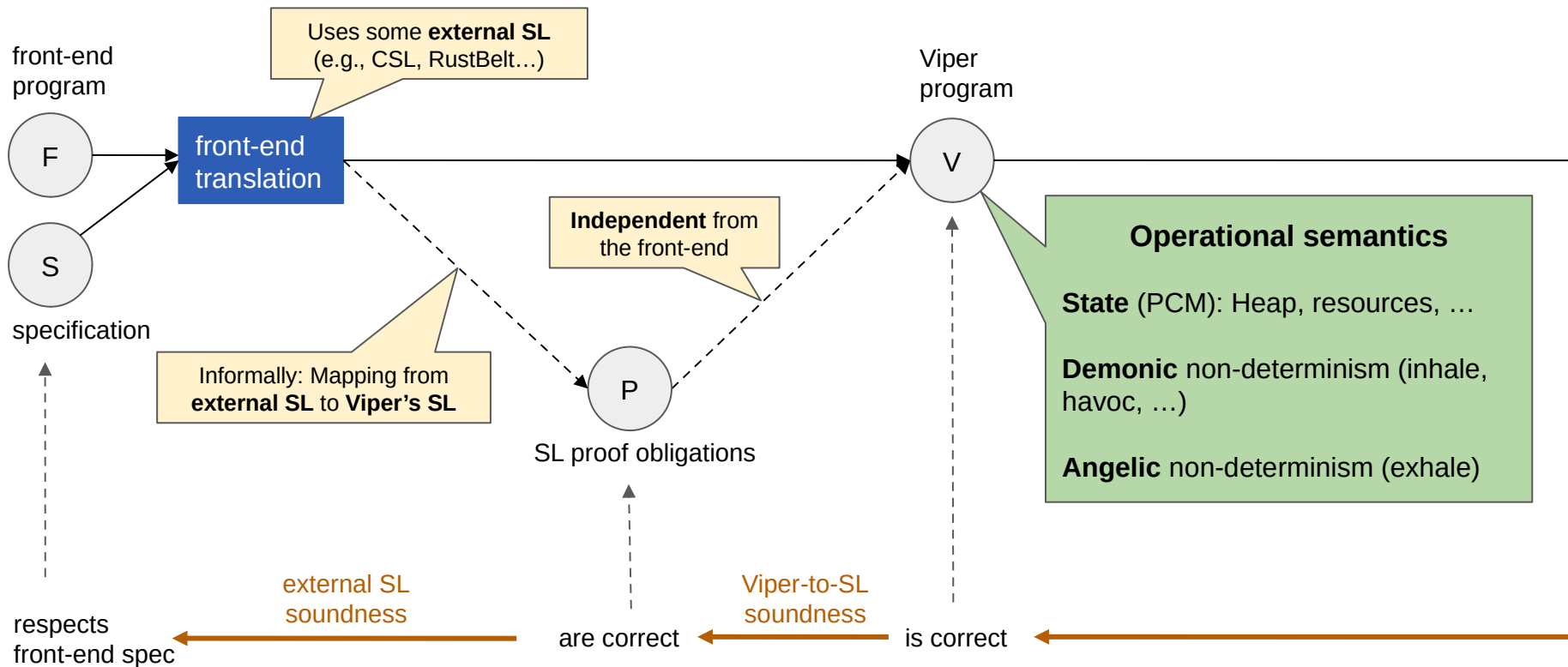
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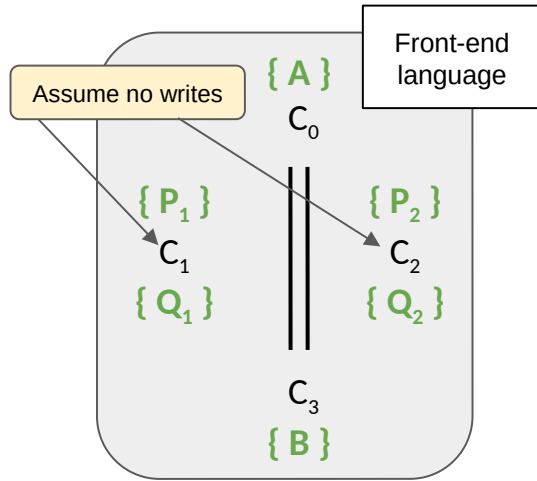
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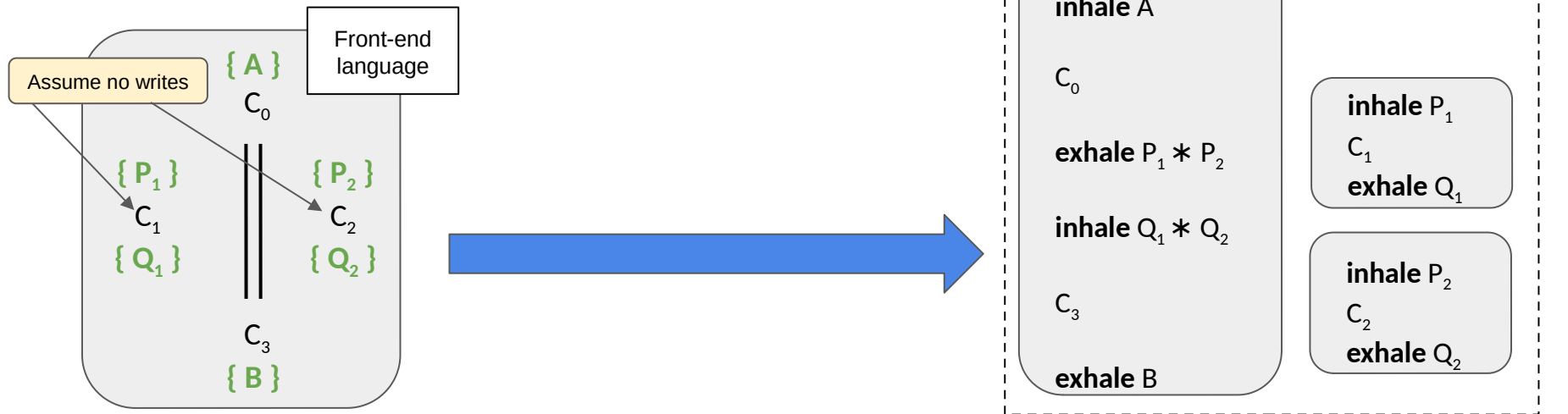
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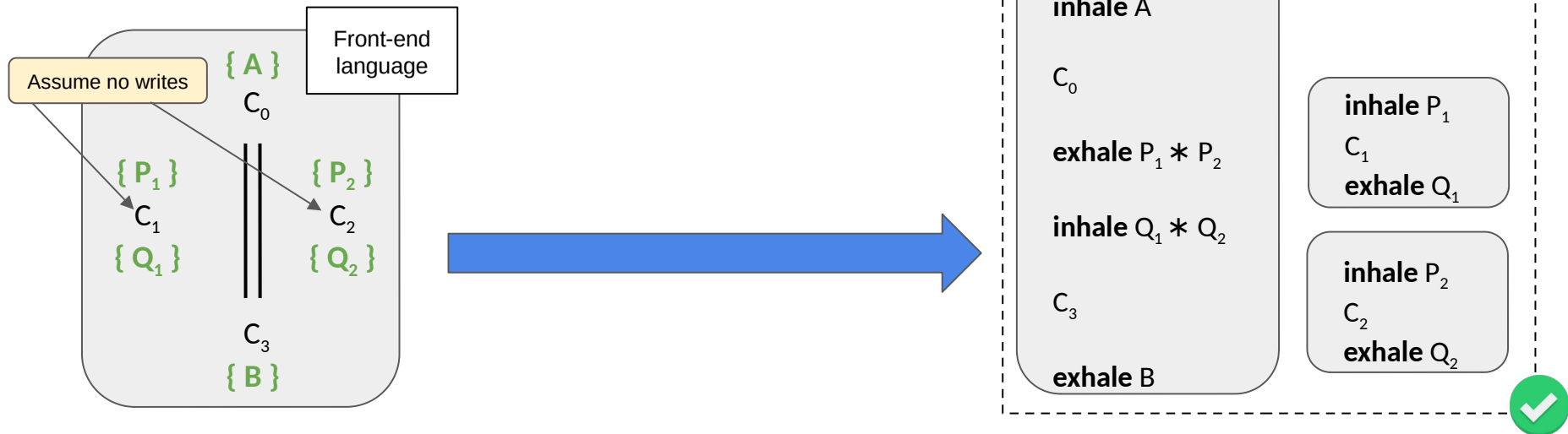
Adequacy Theorem: Viper-to-SL



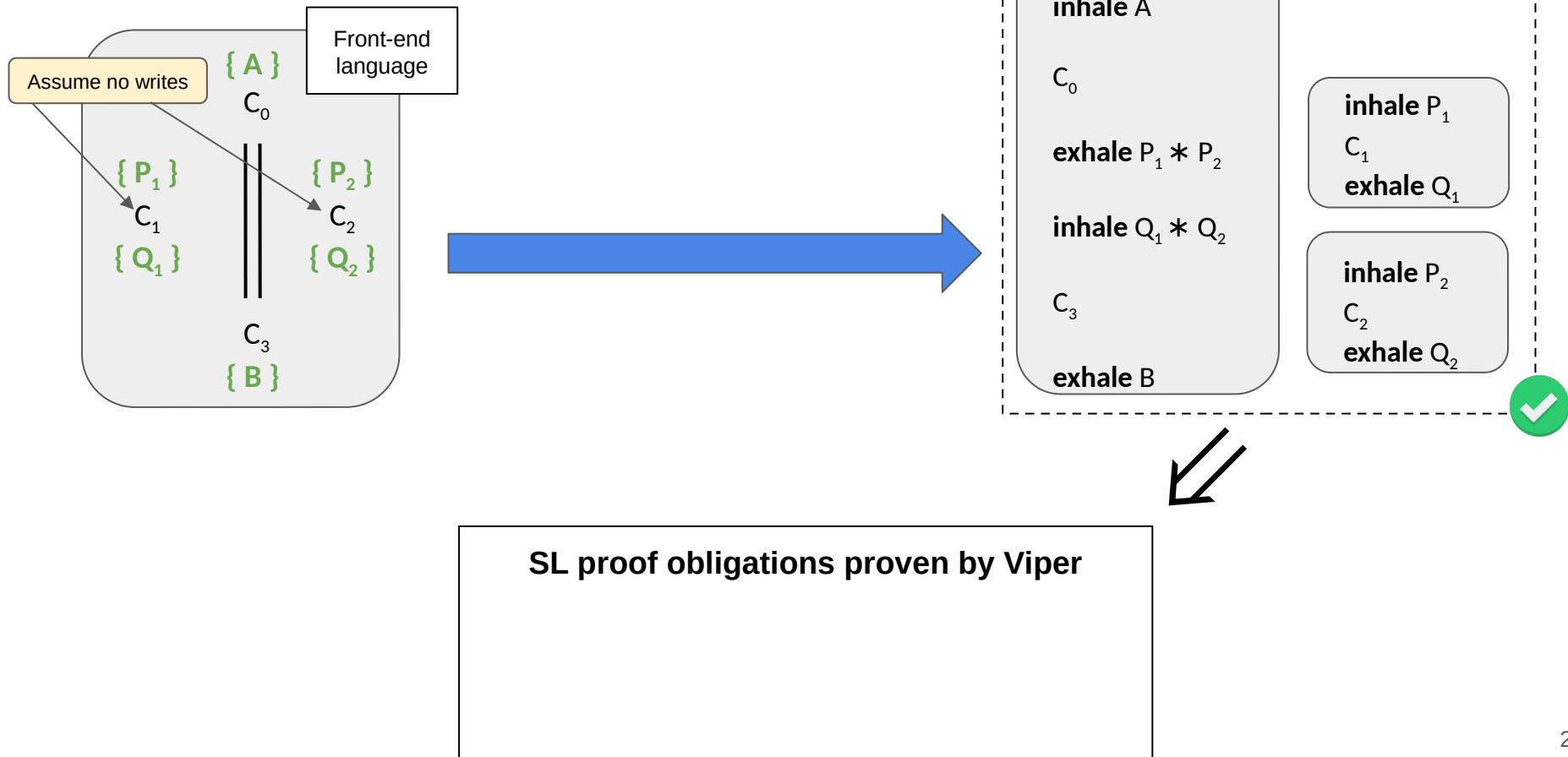
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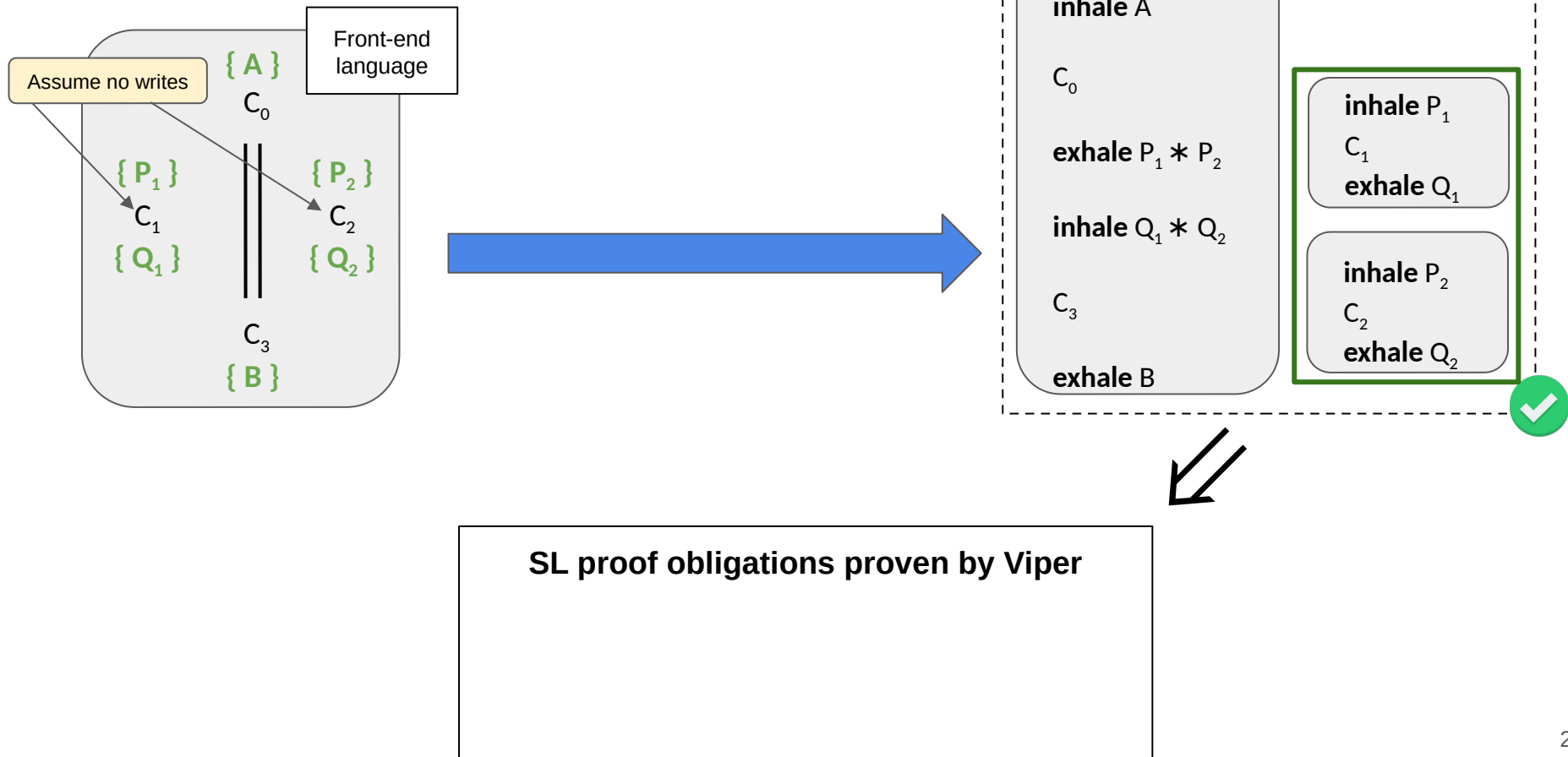
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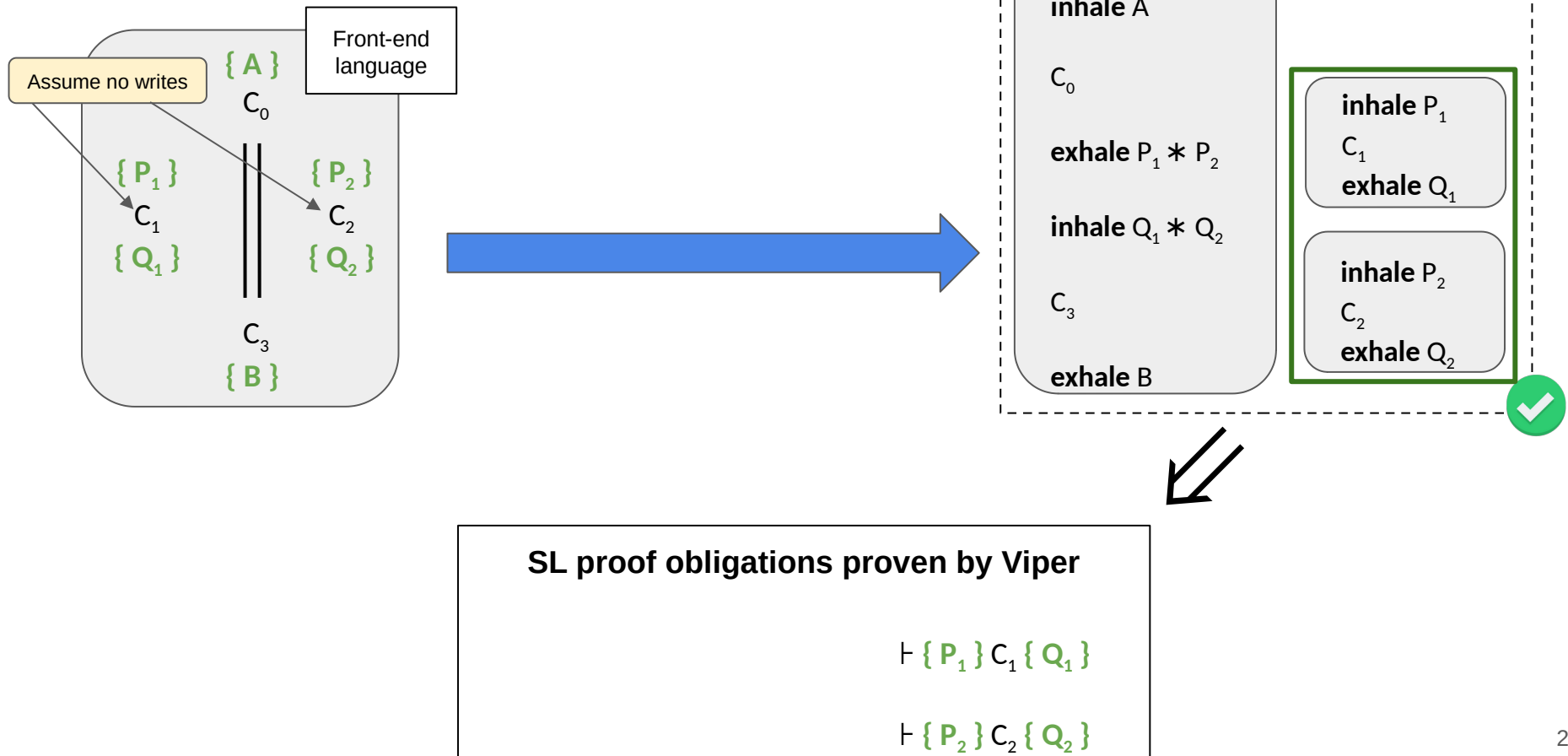
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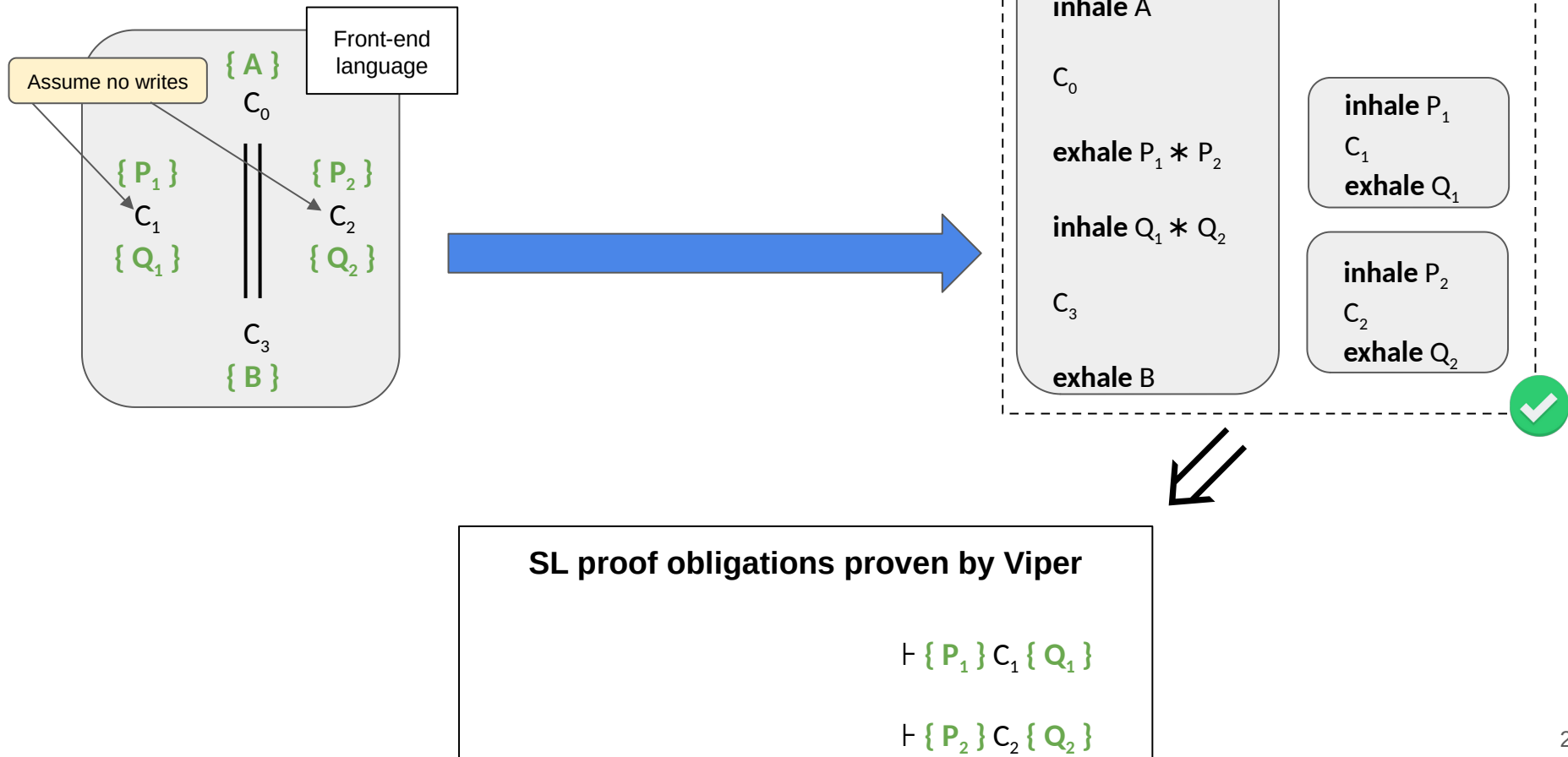
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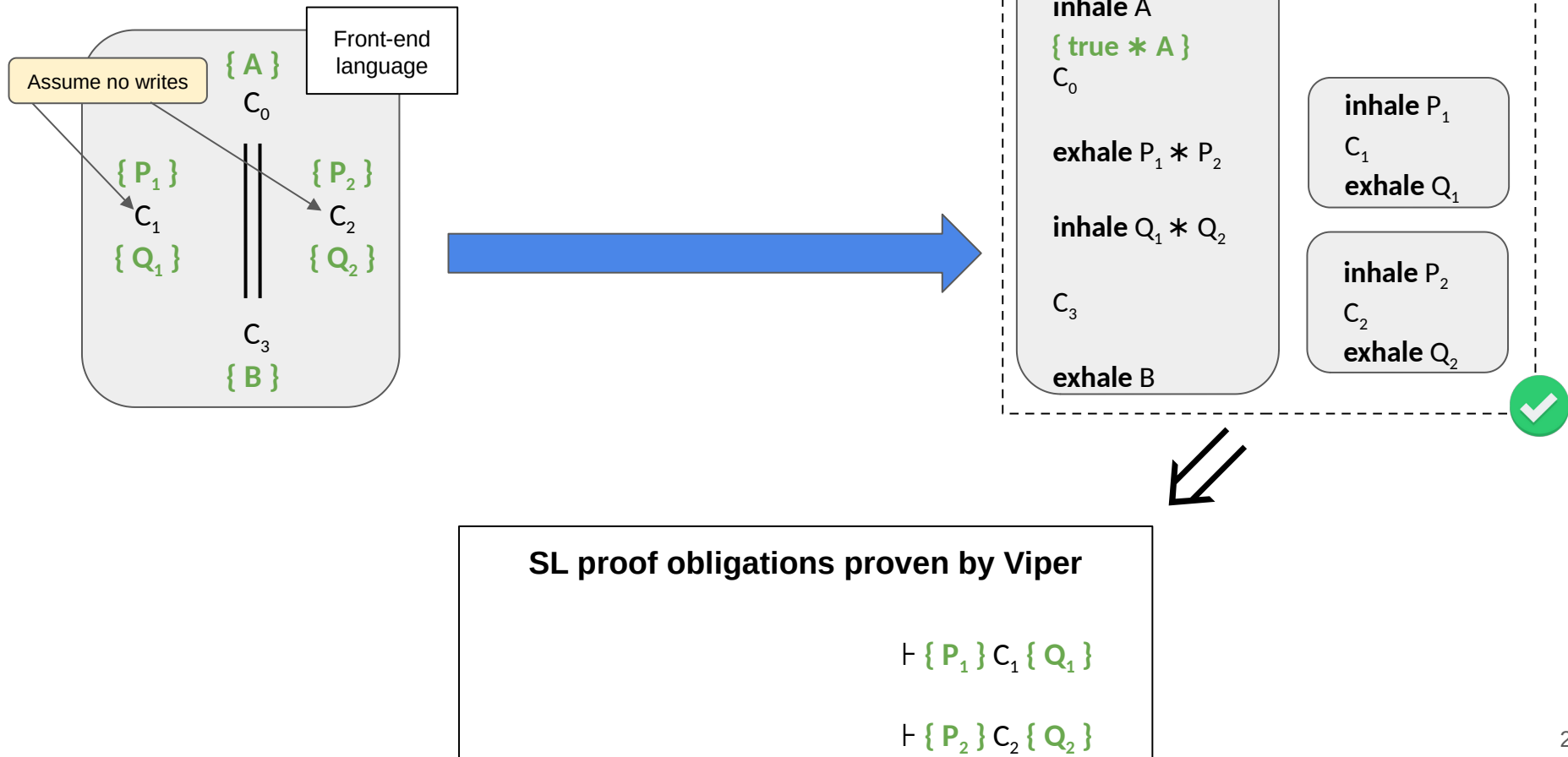
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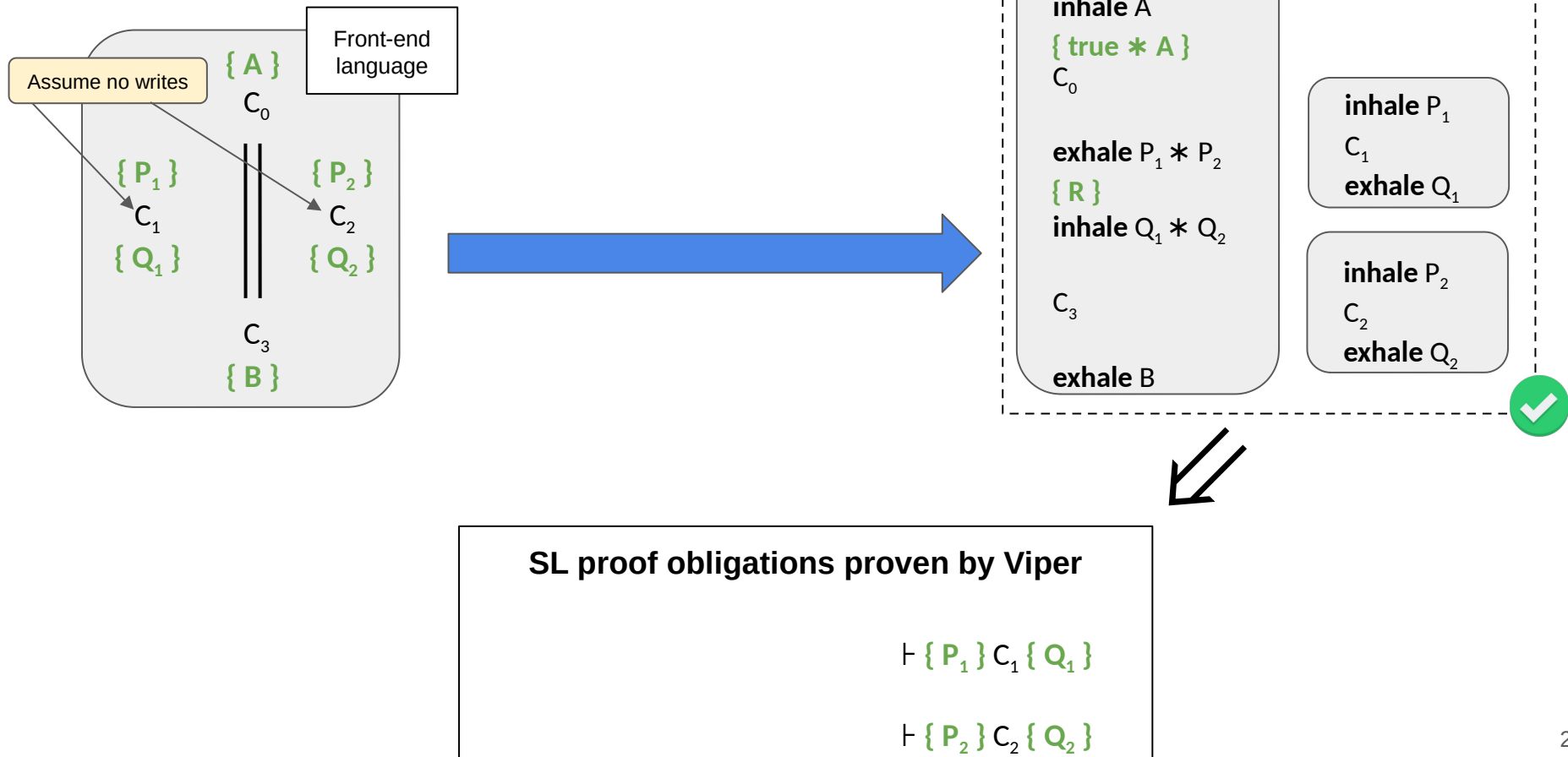
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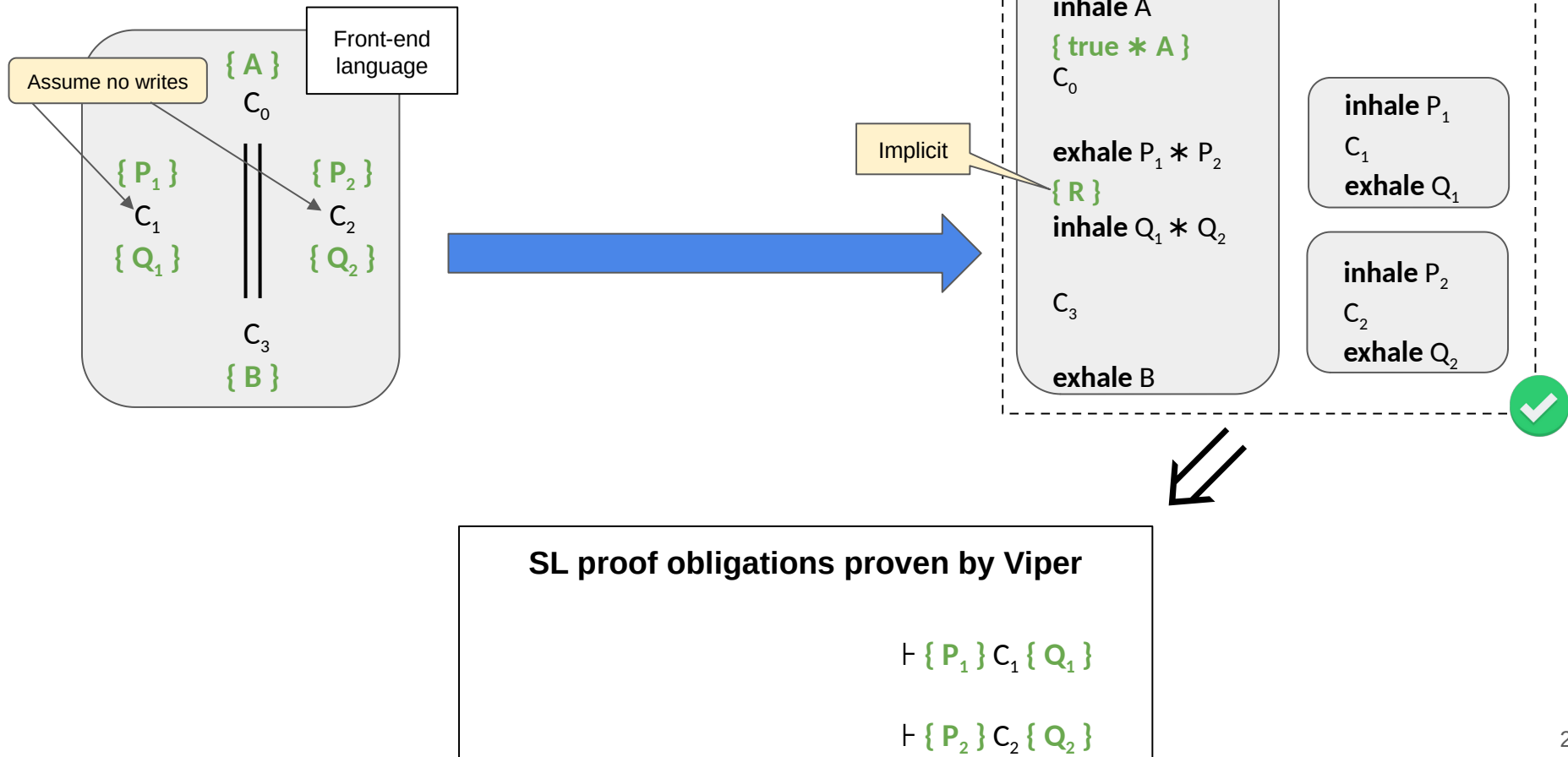
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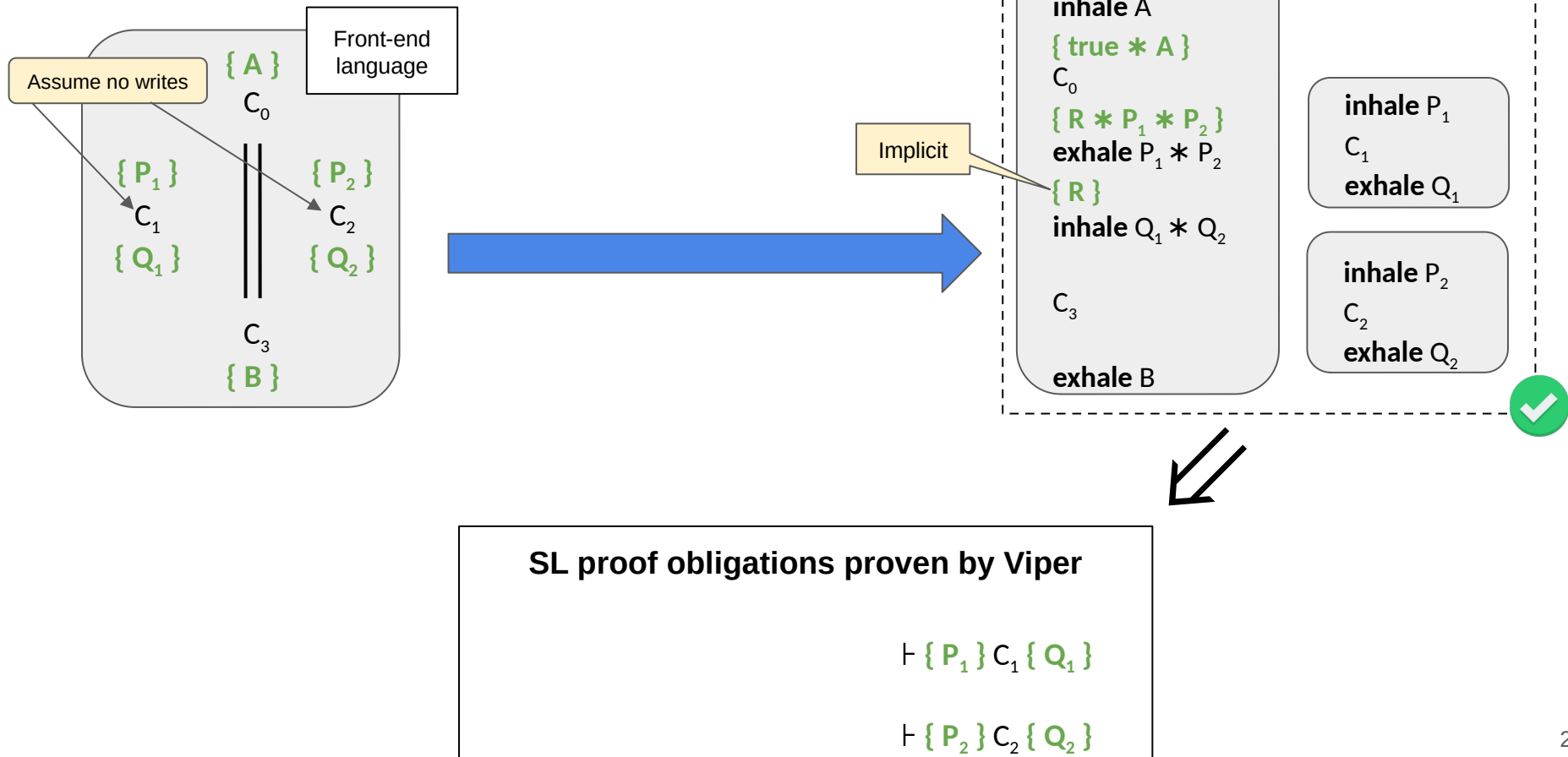
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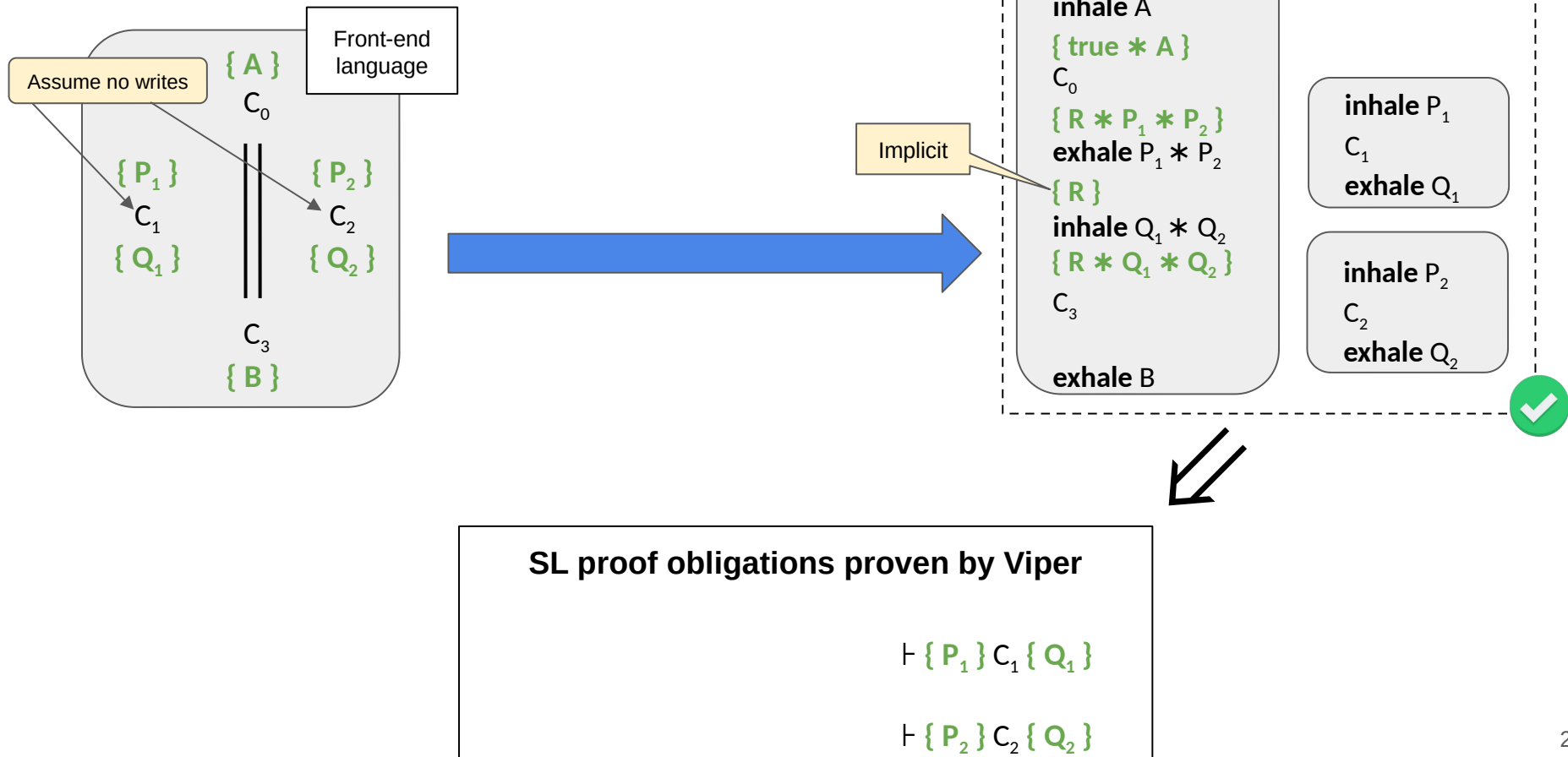
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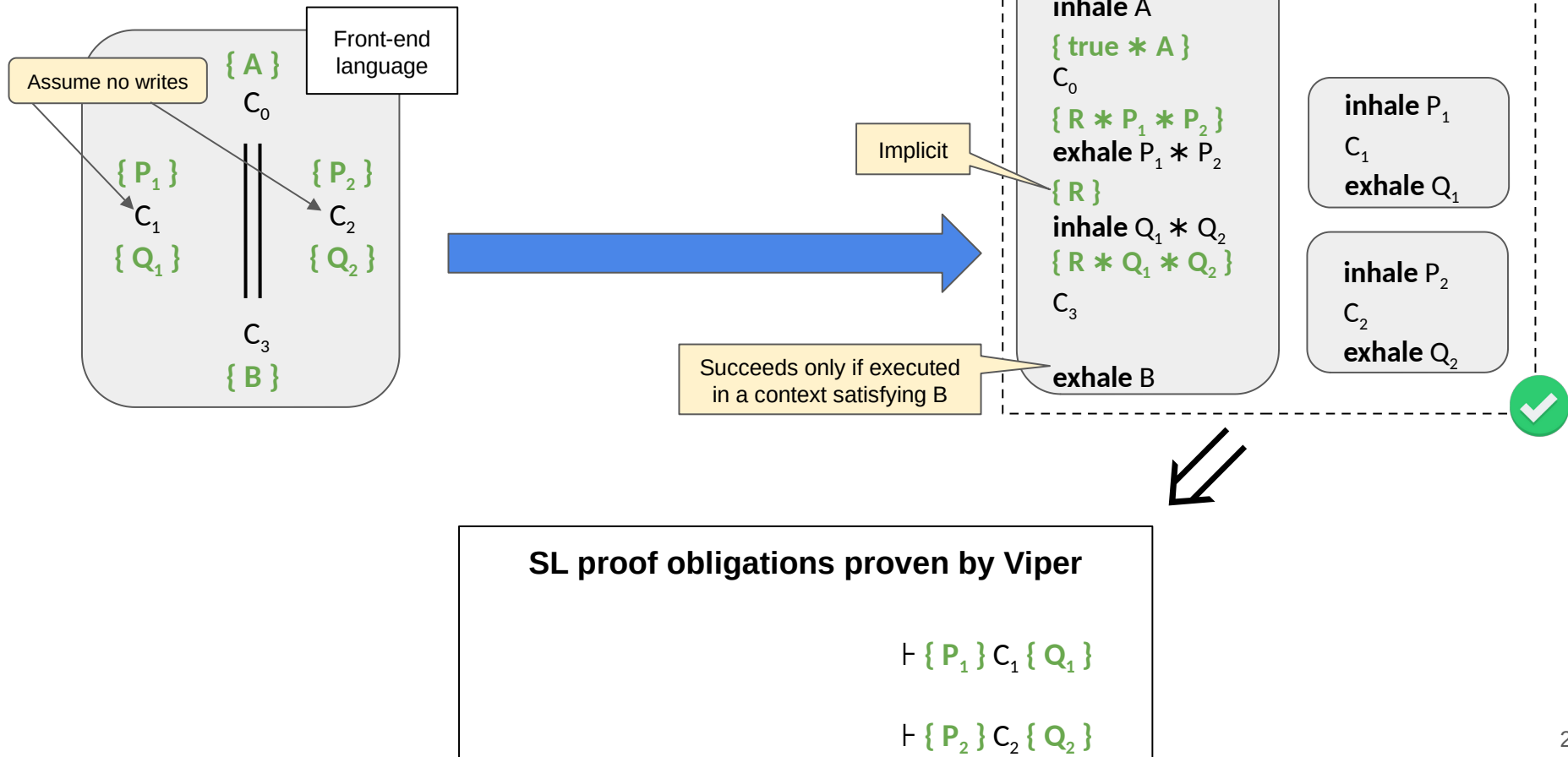
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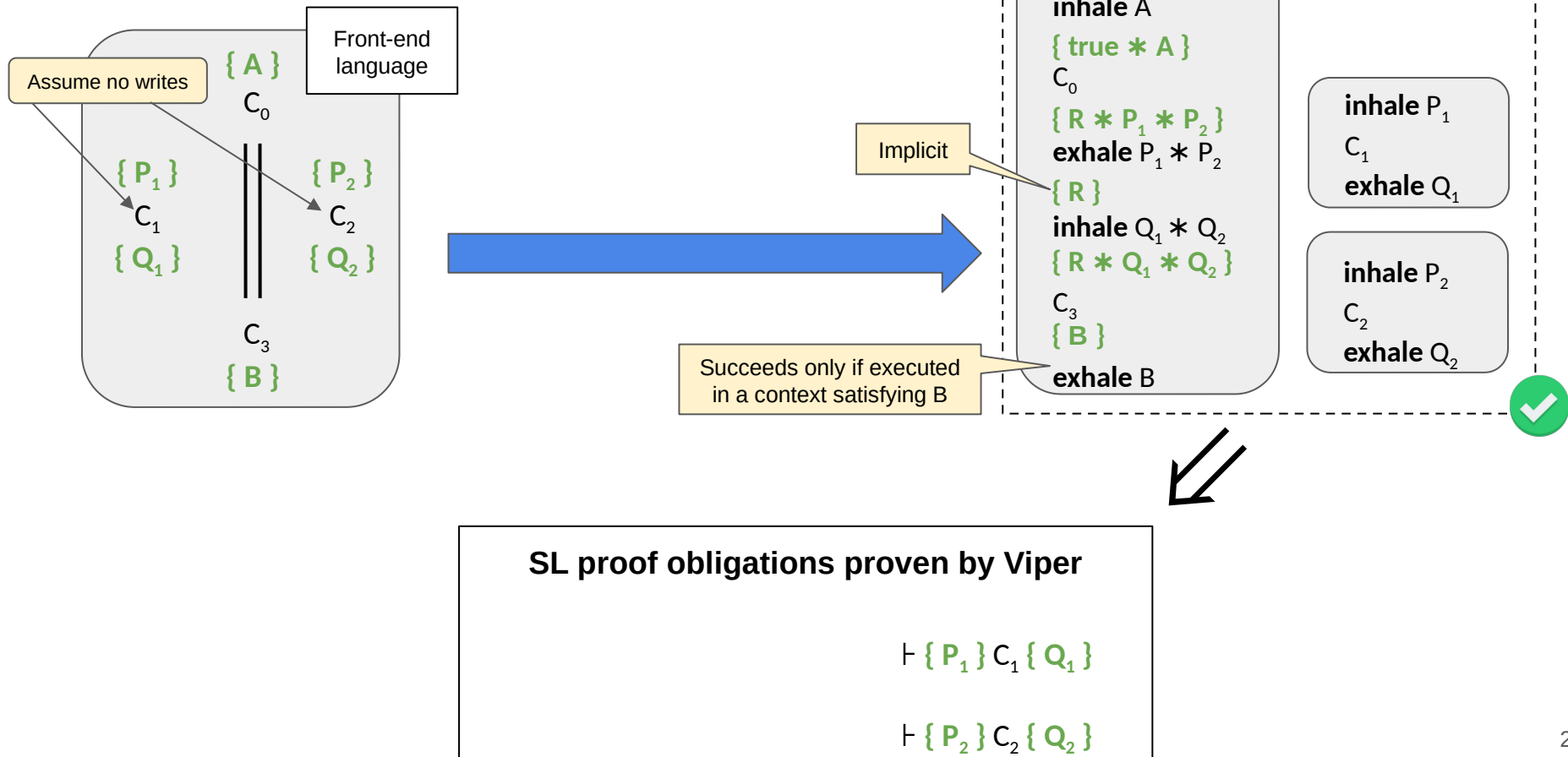
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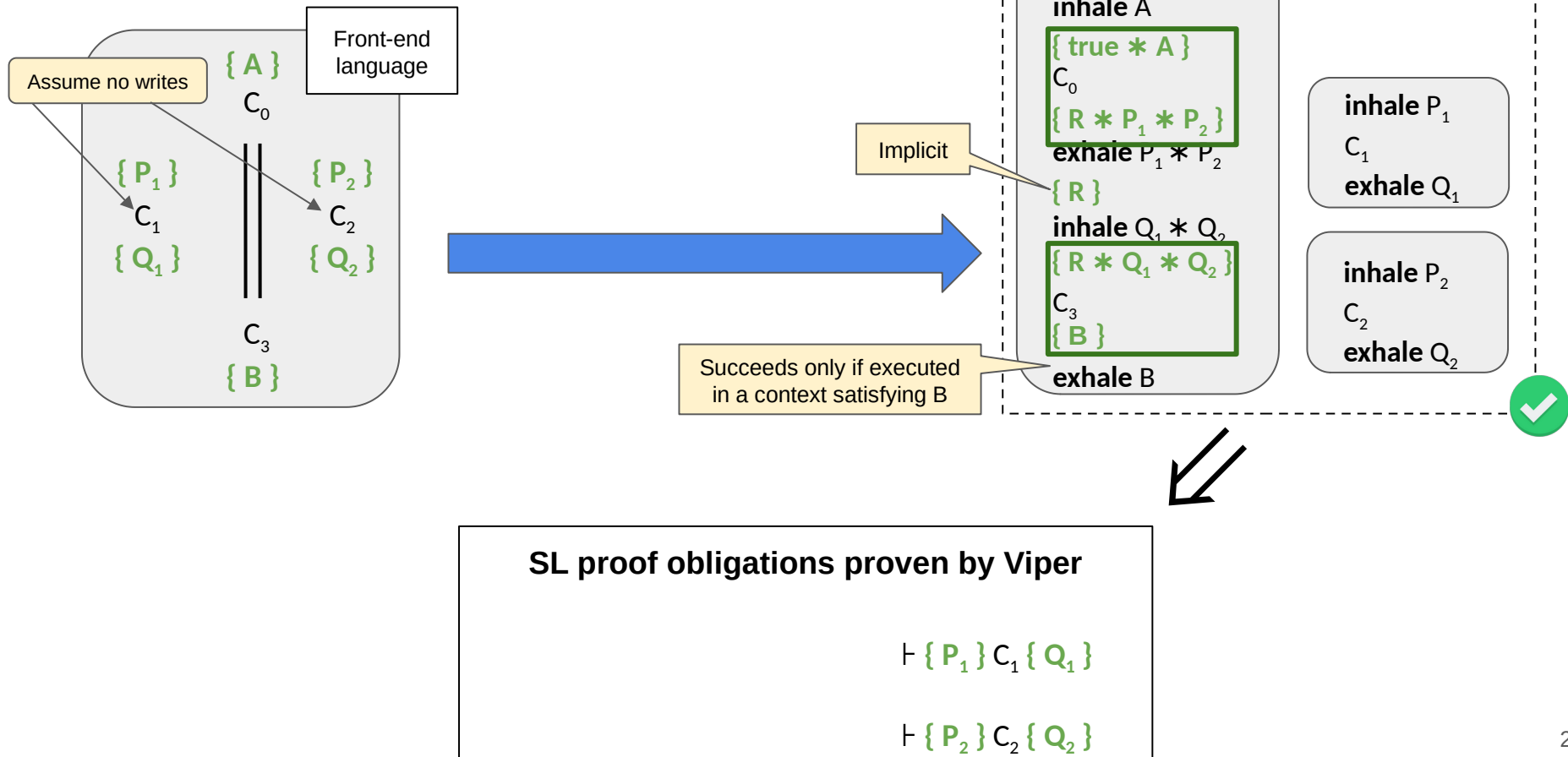
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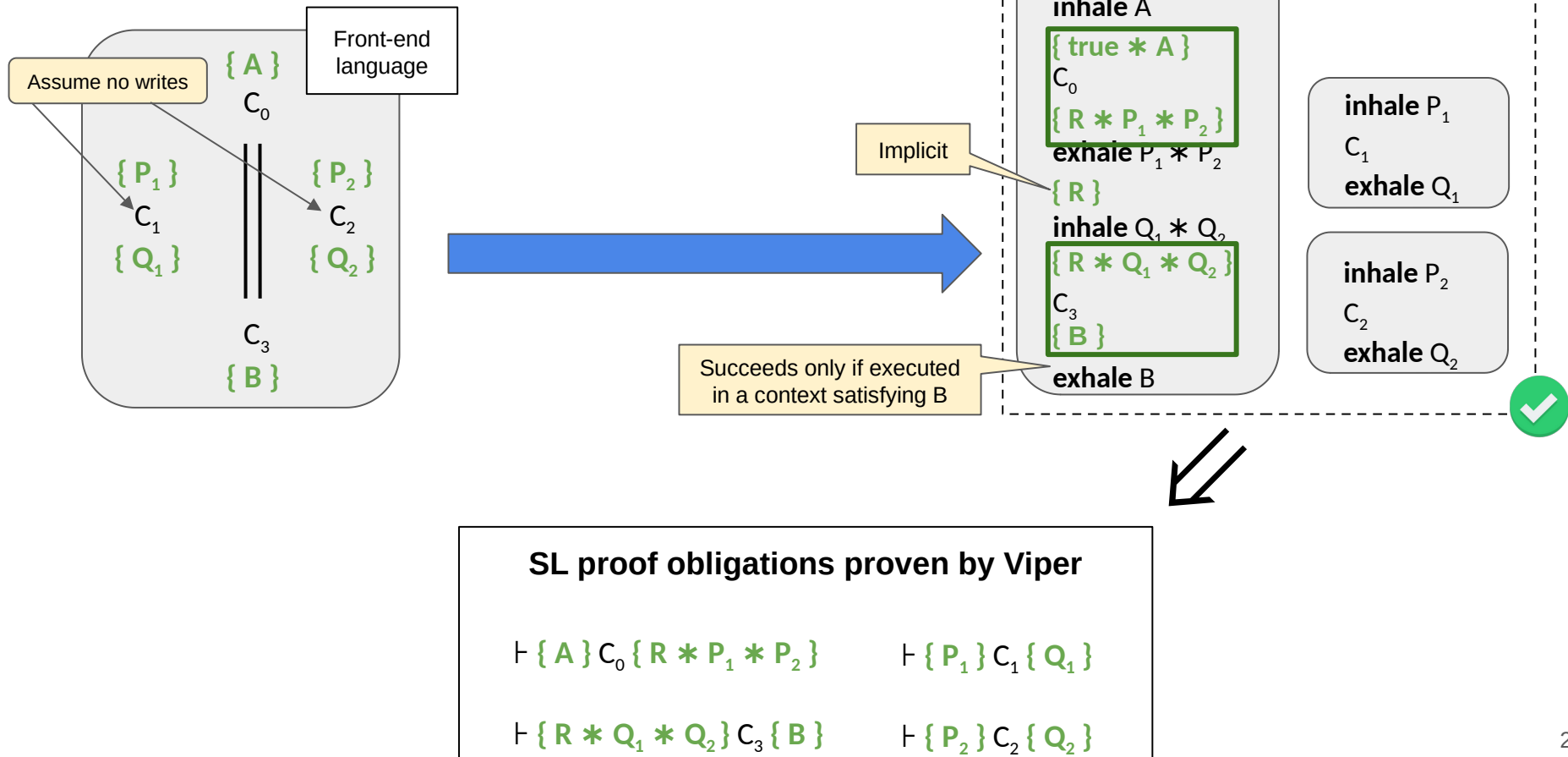
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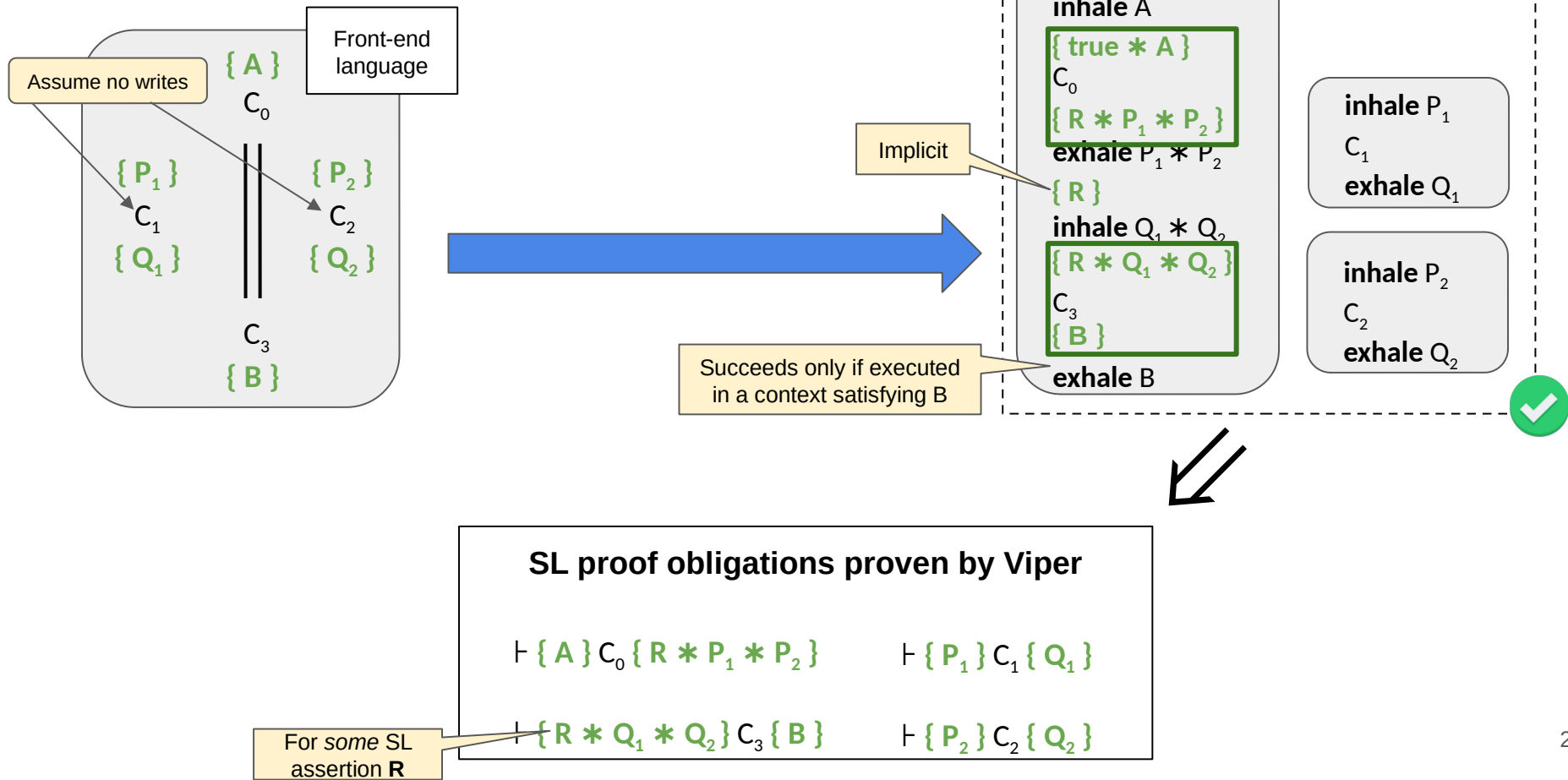
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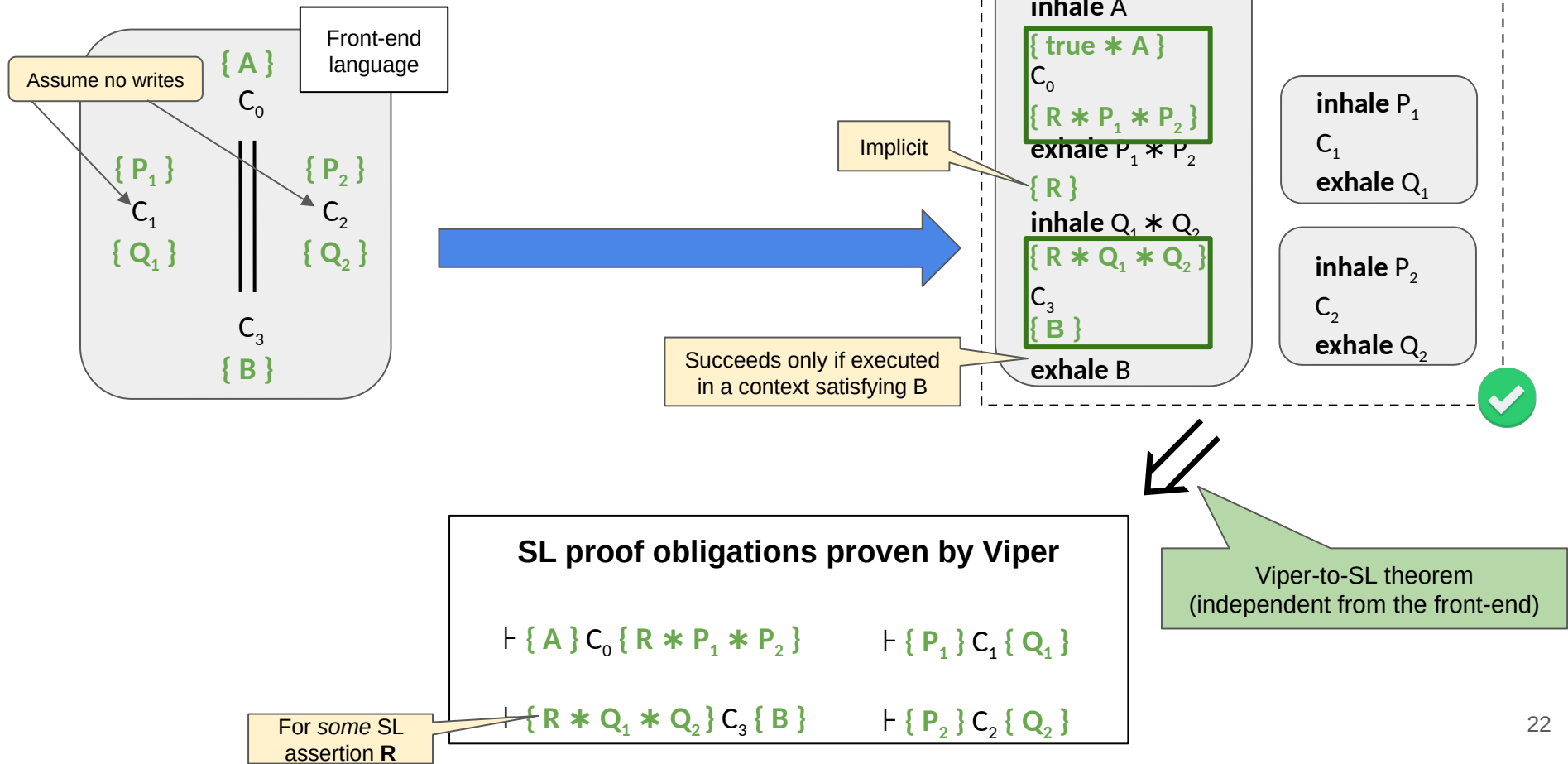
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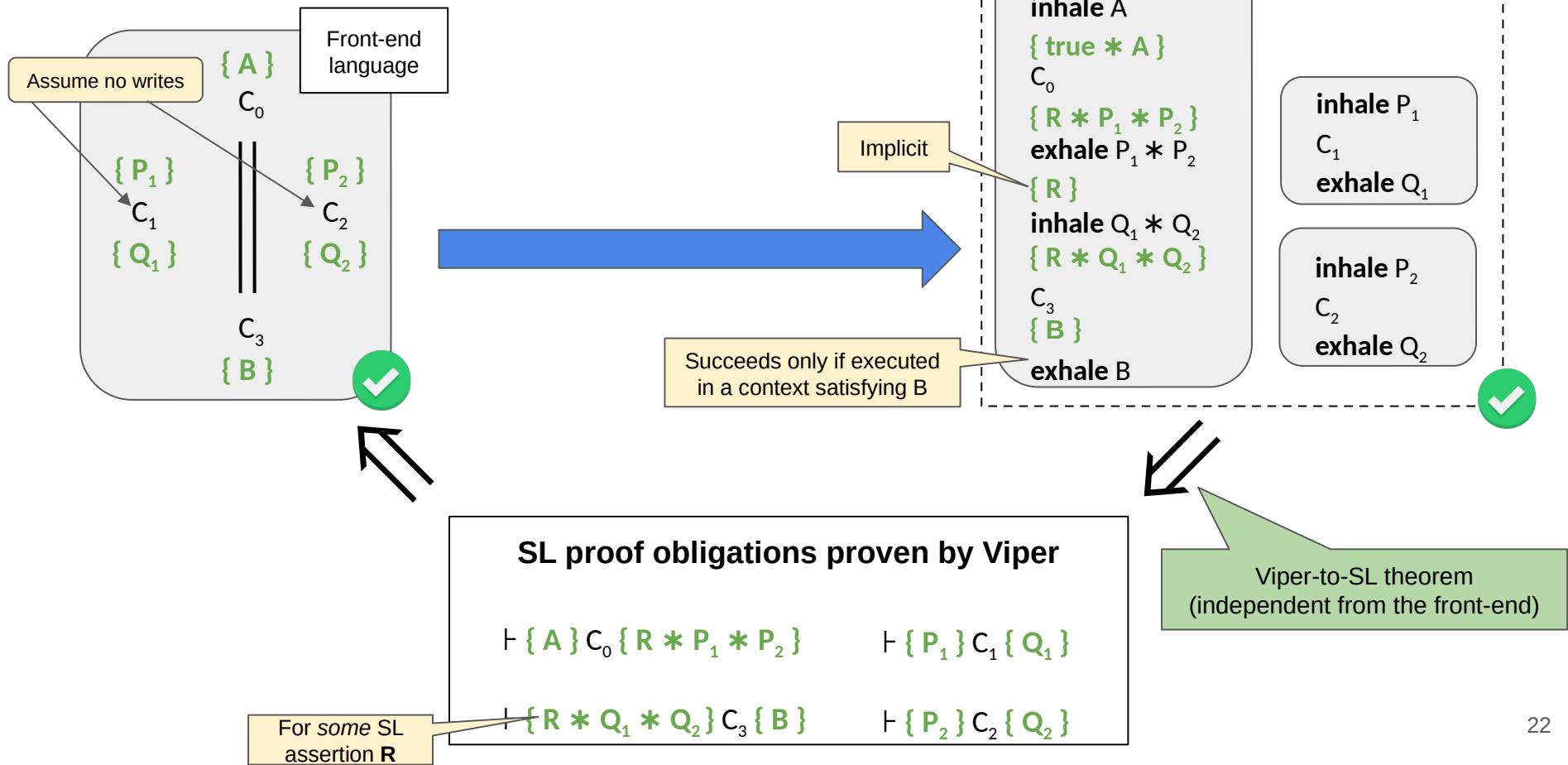
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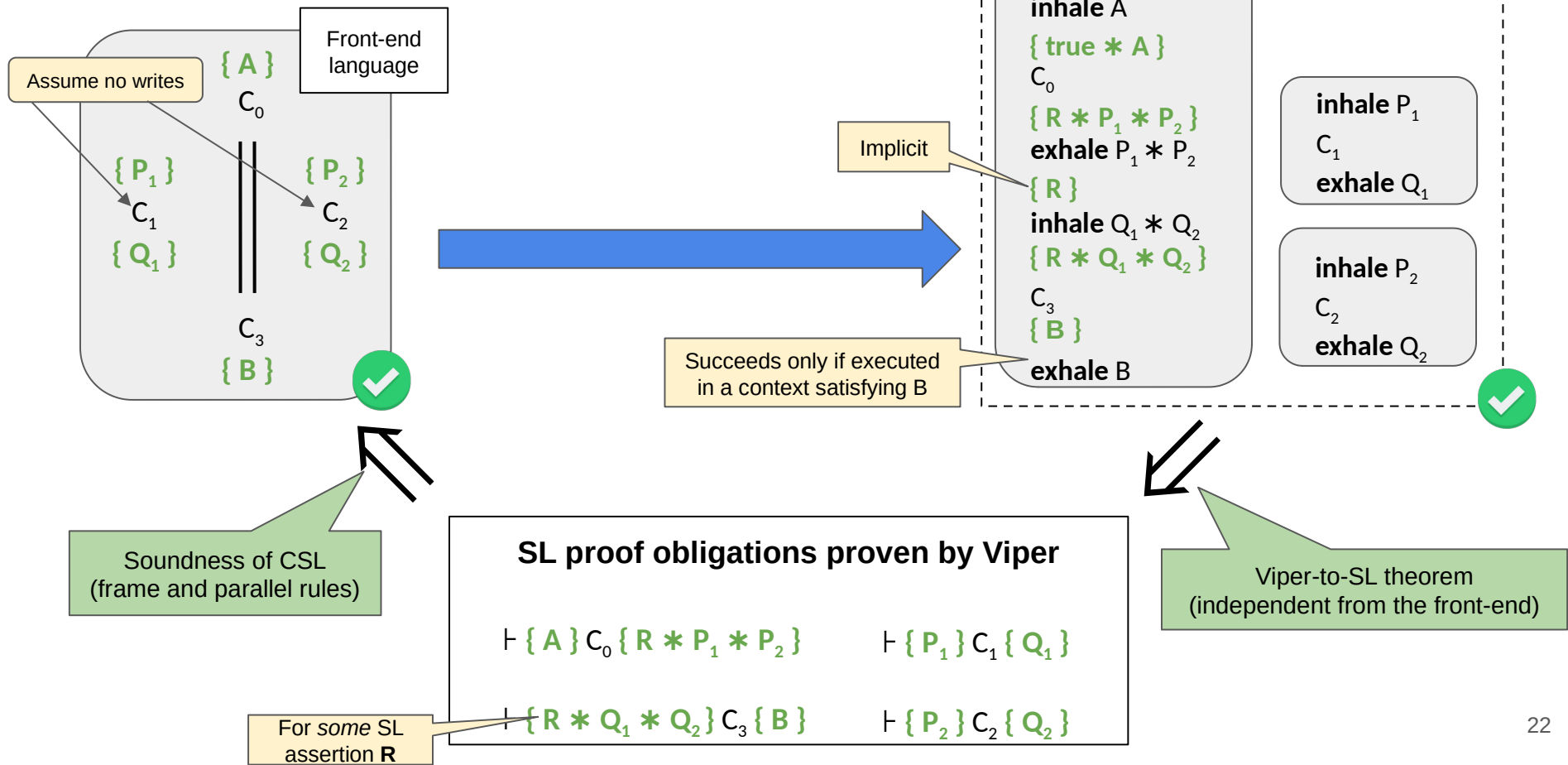
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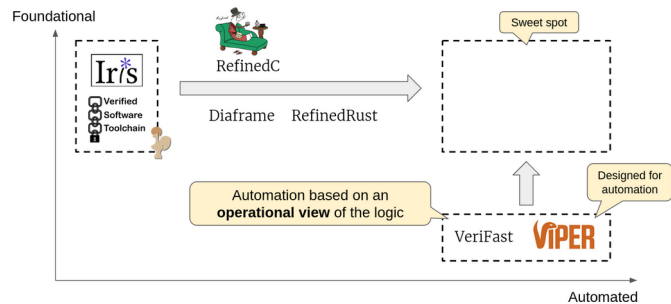
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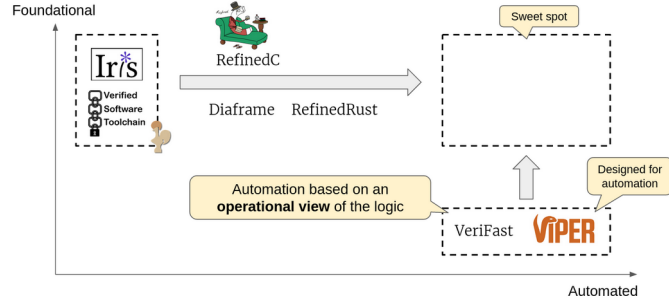
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Program Verifiers Based on Separation Logic



Program Verifiers Based on Separation Logic



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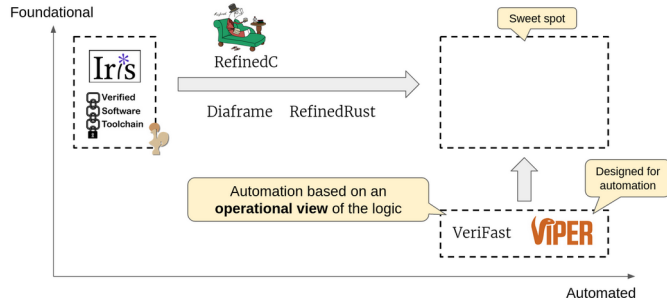
Verification Primitives: Inhale and Exhale

"A Basis for Verifying Multi-Threaded Programs" (Leino and Müller, ESOP 2009)

	inhale A	exhale A
Intuitive meaning	Adds resources specified by A to the current context	Removes resources specified by A from the current context
Logically	$\vdash \{P\} \text{inhale } A \{P * A\}$ $\text{wp}(\text{inhale } A) \{Q\} = A \multimap Q$	$\vdash \{P * A\} \text{exhale } A \{P\}$ $\text{wp}(\text{exhale } A) \{Q\} = A * Q$
Operationally	- All resources required by A are obtained - All logical constraints are assumed	- All resources required by A are removed - All logical constraints are asserted
SL analogue of	assume A	assert A

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Program Verifiers Based on Separation Logic



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Viper's Expression and Assertion Language

Design choice

- No impure existential
- No impure disjunction
- No impure implication
- No impure negation
- No impure logical conjunction

Field access

Heap-dependent functions

$$e ::= e.x \mid f(e_1, \dots, e_n) \mid \text{old}[\!|](e) \mid e_1 + e_2 \mid e_1 / e_2 \mid n \mid v \mid b ? e_1 : e_2 \mid \dots$$

Pure expressions

$$b ::= e_1 = e_2 \mid \neg b \mid b_1 = b_2 \mid b_1 \vee b_2 \mid b_1 \wedge b_2 \mid \forall v. b \mid \dots$$

$$A ::= b \mid \text{acc}(e_1.x, e_2) \mid \text{acc}(P(e_1, \dots, e_n), e) \mid A_1 * A_2 \mid A_1 \multimap A_2 \mid \oplus v. A \mid \boxed{b} \Rightarrow A \mid \dots$$

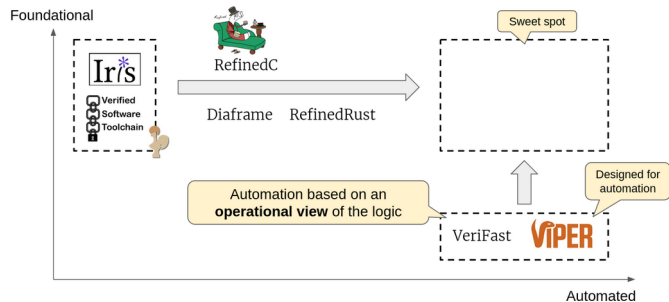
Fractional permissions for heap locations

Recursive predicates with fractional permissions

Iterated separating conjunction

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Program Verifiers Based on Separation Logic



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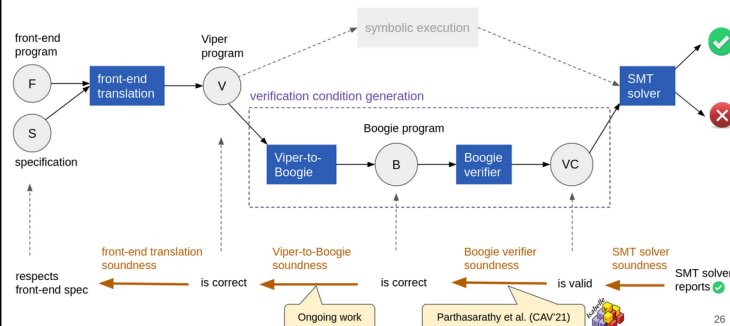
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Soundness: Proof Strategy



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Thank you for your attention!

